

Astro/Phys 224 • Spring 2012

Origin and Evolution of the Universe

Week 9-10

*Cosmic Inflation
& After +
Status of Λ CDM*

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Student Presentations - Thursday June 7

Andrew Marsh:

The Lithium Problem: A Cosmological Conundrum

Srikar Srinath:

The role of Adaptive Optics in resolving the nuclei of merging galaxies at redshifts of 1 or greater and how that is lending support to hierarchical clustering models

Emma Storm:

Indirect Detection of Dark Matter: Effects of Substructure in Galaxy Clusters and Dwarf Galaxies

Basic Predictions of Inflation

1. **Flat universe.** This is perhaps the most fundamental prediction of inflation. Through the Friedmann equation it implies that the total energy density is always equal to the critical energy density; it does not however predict the form (or forms) that the critical density takes on today or at any earlier or later epoch.
2. **Nearly scale-invariant spectrum of Gaussian density perturbations.** These density perturbations (scalar metric perturbations) arise from quantum-mechanical fluctuations in the field that drives inflation; they begin on very tiny scales (of the order of 10^{-23} cm, and are stretched to astrophysical size by the tremendous growth of the scale factor during inflation (factor of e^{60} or greater). Scale invariant refers to the fact that the fluctuations in the gravitational potential are independent of length scale; or equivalently that the horizon-crossing amplitudes of the density perturbations are independent of length scale. While the shape of the spectrum of density perturbations is common to all models, the overall amplitude is model dependent. Achieving density perturbations that are consistent with the observed anisotropy of the CBR and large enough to produce the structure seen in the Universe today requires a horizon crossing amplitude of around 2×10^{-5} .
3. **Nearly scale-invariant spectrum of gravitational waves**, from quantum-mechanical fluctuations in the metric itself. These can be detected as CMB “B-mode” polarization, or using special gravity wave detectors such as LIGO and LISA.

Inflation Summary

The key features of all inflation scenarios are a period of superluminal expansion, followed by (“re-”)heating which converts the energy stored in the inflaton field (for example) into the thermal energy of the hot big bang.

Inflation is generic: it fits into many versions of particle physics, and it can even be made rather natural in modern supersymmetric theories as we have seen. The simplest models have inflated away all relics of any pre-inflationary era and result in a flat universe after inflation, i.e., $\Omega = 1$ (or more generally $\Omega_0 + \Omega_\Lambda = 1$). Inflation also produces scalar (density) fluctuations that have a primordial spectrum

Density fluctuations $\left(\frac{\delta\rho}{\rho}\right)^2 \sim \left(\frac{V^{3/2}}{m_{Pl}^3 V'}\right)^2 \propto k^{n_p}, \quad \text{“tilt”} = 1 - n_p \quad (1.12)$

where V is the inflaton potential and n_p is the primordial spectral index, which is expected to be near unity (near-Zel’dovich spectrum). Inflation also produces tensor (gravity wave) fluctuations, with spectrum

Gravity waves $P_t(k) \sim \left(\frac{V}{m_{Pl}}\right)^2 \propto k^{n_t}, \quad (1.13)$

where the tensor spectral index $n_t \approx (1 - n_p)$ in many models.

The quantity $(1 - n_p)$ is often called the “tilt” of the spectrum; the larger the tilt, the more fluctuations on small spatial scales (corresponding to large k) are suppressed compared to those on larger scales. The scalar and tensor waves are generated by independent quantum fluctuations during inflation, and so their contributions to the CMB temperature fluctuations add in quadrature. The ratio of these contributions to the quadrupole anisotropy amplitude Q is often called $T/S \equiv Q_t^2/Q_s^2$; thus the primordial scalar fluctuation power is decreased by the ratio $1/(1 + T/S)$ for the same COBE normalization, compared to the situation with no gravity waves ($T = 0$). In power-law inflation, $T/S = 7(1 - n_p)$. This is an approximate equality in other popular inflation models such as chaotic inflation with $V(\phi) = m^2\phi^2$ or $\lambda\phi^4$. But note that the tensor wave amplitude is just the inflaton potential during inflation divided by the Planck mass, so the gravity wave contribution is negligible in theories like the supersymmetric model discussed above in which inflation occurs at an energy scale far below m_{Pl} . Because gravity waves just redshift after they come inside the horizon, the tensor contributions to CMB anisotropies corresponding to angular wavenumbers $\ell \gg 20$, which came inside the horizon long ago, are strongly suppressed compared to those of scalar fluctuations.

Joel Primack, in *Formation of Structure in the Universe*, ed. Dekel & Ostriker (Cambridge Univ Press, 1999)

Useful Formulas

Density Fluctuations from Inflation

The relationship between the inflationary potential and the power spectrum of density perturbations today ($P(k) \equiv \langle |\delta_k|^2 \rangle$) is given by

Power Spectrum $P(k) = \frac{1024\pi^3}{75} \frac{k}{H_0^4} \frac{V_*^3}{m_{\text{Pl}}^6 V_*'^2} \left(\frac{k}{k_*}\right)^{n_s-1} T^2(k)$ Transfer function

Tilt $n_s - 1 = -\frac{1}{8\pi} \left(\frac{m_{\text{Pl}} V_*'}{V_*}\right)^2 + \frac{m_{\text{Pl}}}{4\pi} \left(\frac{m_{\text{Pl}} V_*'}{V_*}\right)'$ generally nonzero, ≈ 0.04 according to WMAP7

Running Tilt $\frac{dn}{d \ln k} = -\frac{1}{32\pi^2} \left(\frac{m_{\text{Pl}}^3 V_*'''}{V_*}\right) \left(\frac{m_{\text{Pl}} V_*'}{V_*}\right) + \frac{1}{8\pi^2} \left(\frac{m_{\text{Pl}}^2 V_*''}{V_*}\right) \left(\frac{m_{\text{Pl}} V_*'}{V_*}\right)^2 - \frac{3}{32\pi^2} \left(m_{\text{Pl}} \frac{V_*'}{V_*}\right)^4$

$$T(q) = \frac{\ln(1 + 2.34q) / 2.34q}{[1 + 3.89q + (16.1q)^2 + (5.46q)^3 + (6.71q)^4]^{1/4}}, \quad (4)$$

where $V(\phi)$ is the inflationary potential, prime denotes $d/d\phi$, V_* is the value of the scalar potential when the scale k_* crossed outside the horizon during inflation, $T(k)$ is the transfer function which accounts for the evolution of the mode k from horizon crossing until the present, $q = k/h\Gamma$, and $\Gamma \simeq \Omega_M h$ is the “shape” parameter. The fitting formula (4) isn't accurate enough for precision work; instead, use the website <http://camb.info/>.

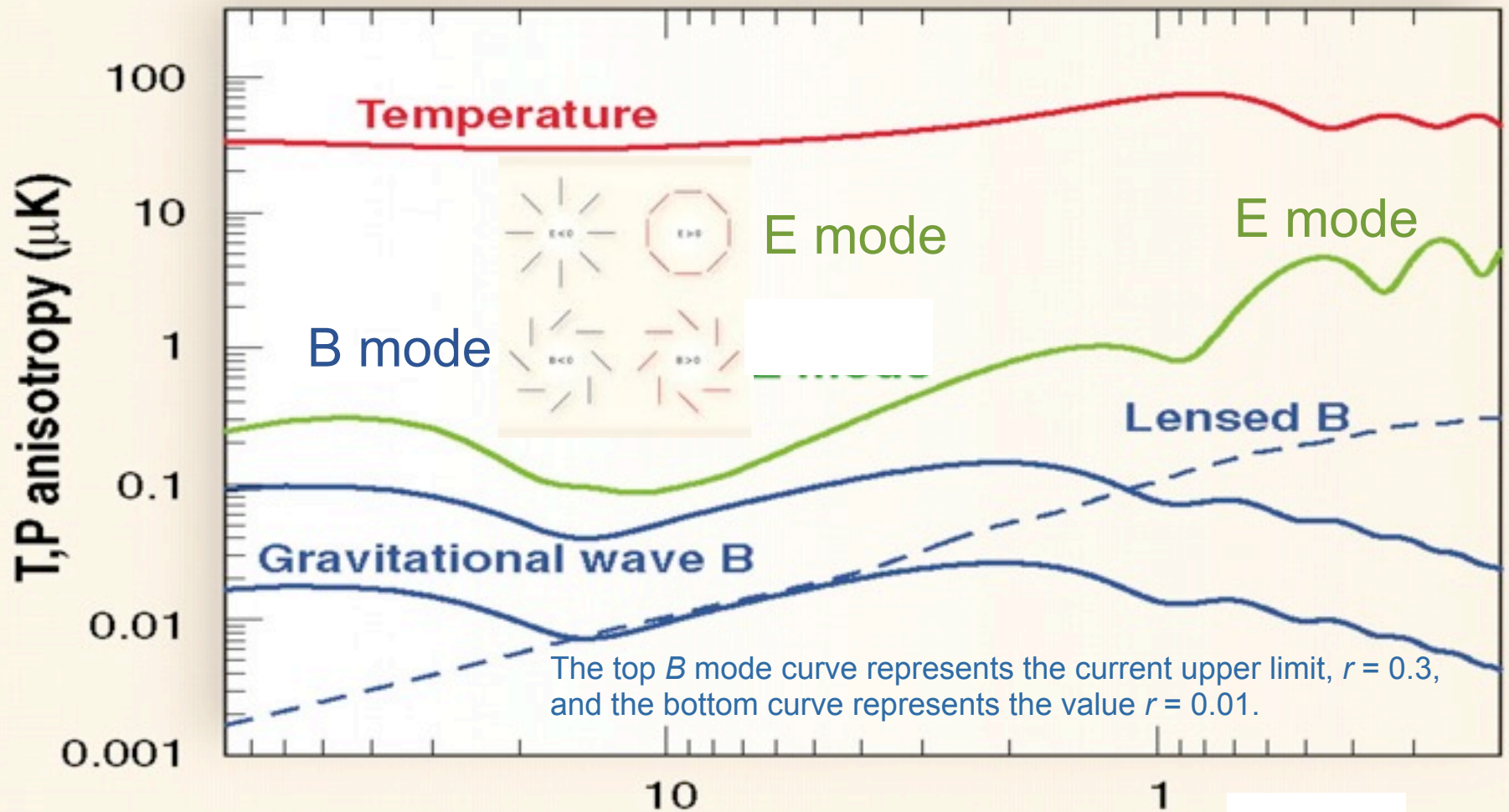
Gravity Waves from Inflation

Unlike the scalar perturbations, which must have an amplitude of around 10^{-5} to seed structure formation, there is an upper but no lower limit on the amplitude of the tensor perturbations. They can be characterized by their power spectrum today

$$\begin{aligned}
 P_T(k) &\equiv \langle |h_k|^2 \rangle = \frac{8}{3\pi} \frac{V_*}{m_{\text{Pl}}^4} \left(\frac{k}{k_*} \right)^{n_T-3} T_T^2(k) \\
 n_T &= -\frac{1}{8\pi} \left(\frac{m_{\text{Pl}} V'_*}{V_*} \right)^2 \\
 \frac{dn_T}{d \ln k} &= \frac{1}{32\pi^2} \left(\frac{m_{\text{Pl}}^2 V''}{V} \right) \left(\frac{m_{\text{Pl}} V'}{V} \right)^2 - \frac{1}{32\pi^2} \left(\frac{m_{\text{Pl}} V'}{V} \right)^4 = -n_T[(n-1) - n_T] \\
 T_T(k) &\simeq \left[1 + \frac{4}{3} \frac{k}{k_{\text{EQ}}} + \frac{5}{2} \left(\frac{k}{k_{\text{EQ}}} \right)^2 \right]^{1/2}, \tag{11}
 \end{aligned}$$

where $T_T(k)$ is the transfer function for gravity waves and describes the evolution of mode k from horizon crossing until the present, $k_{\text{EQ}} = 6.22 \times 10^{-2} \text{ Mpc}^{-1} (\Omega_M h^2 / \sqrt{g_*/3.36})$ is the scale that crossed the horizon at matter-radiation equality, Ω_M is the fraction of critical density in matter, and g_* counts the effective number of relativistic degrees of freedom (3.36 for photons and three light neutrino species). The quantity $k^{3/2} |h_k| / \sqrt{2\pi^2}$ corresponds to the dimensionless strain (metric perturbation) on length scale $\lambda = 2\pi/k$.

Root mean square fluctuations in temperature (T) and polarization (E and B modes) of the CMB predicted by inflation.

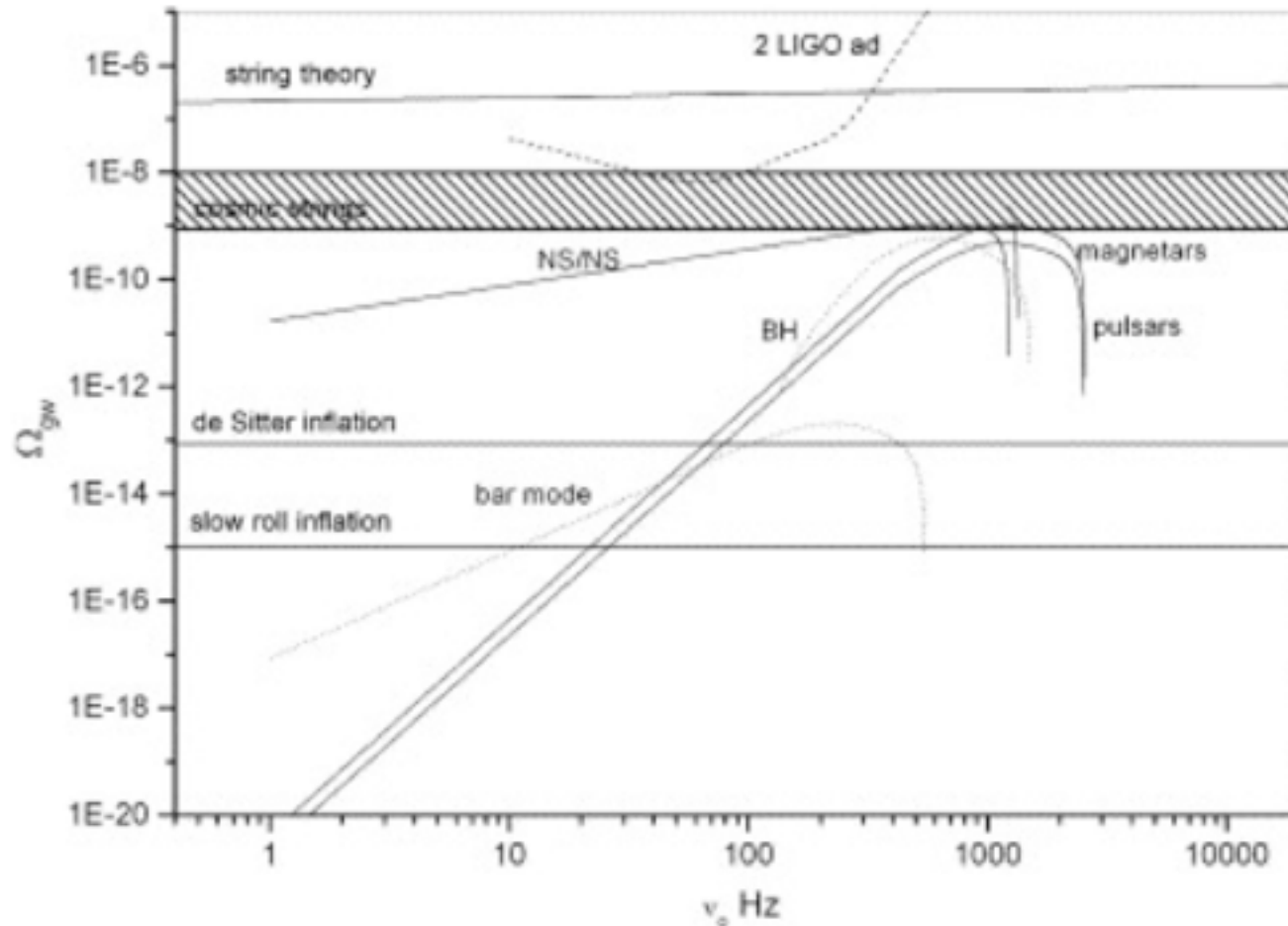


The top B mode curve represents the current upper limit, $r = 0.3$, and the bottom curve represents the value $r = 0.01$.

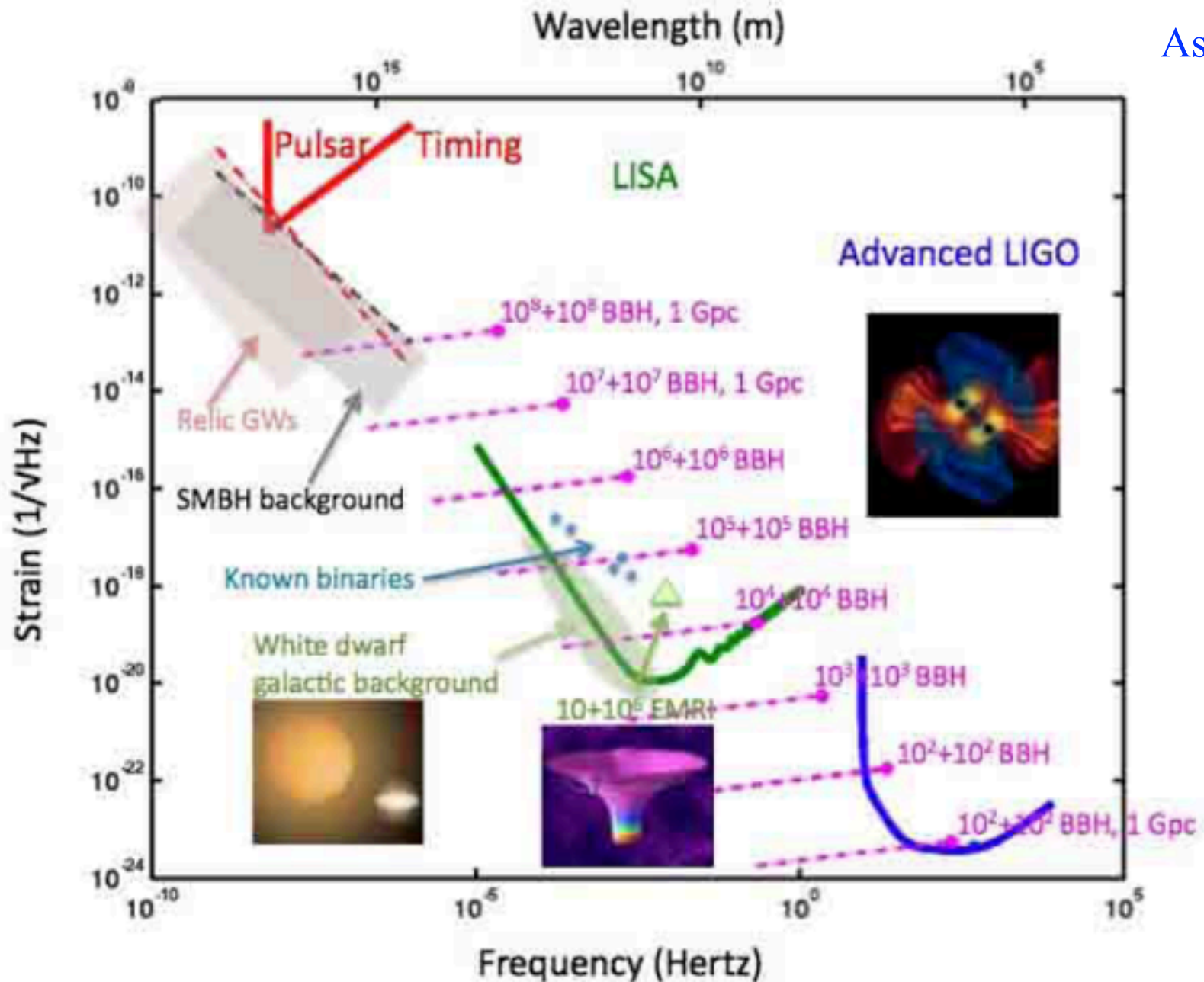
$$V^{1/4} = 1.06 \times 10^{16} \text{ GeV} \left(\frac{r}{0.01} \right) \quad \text{Angular separation (degrees)}$$

$$r \equiv \frac{P_t}{P_s}$$

Gravity Waves: Sources and Strengths

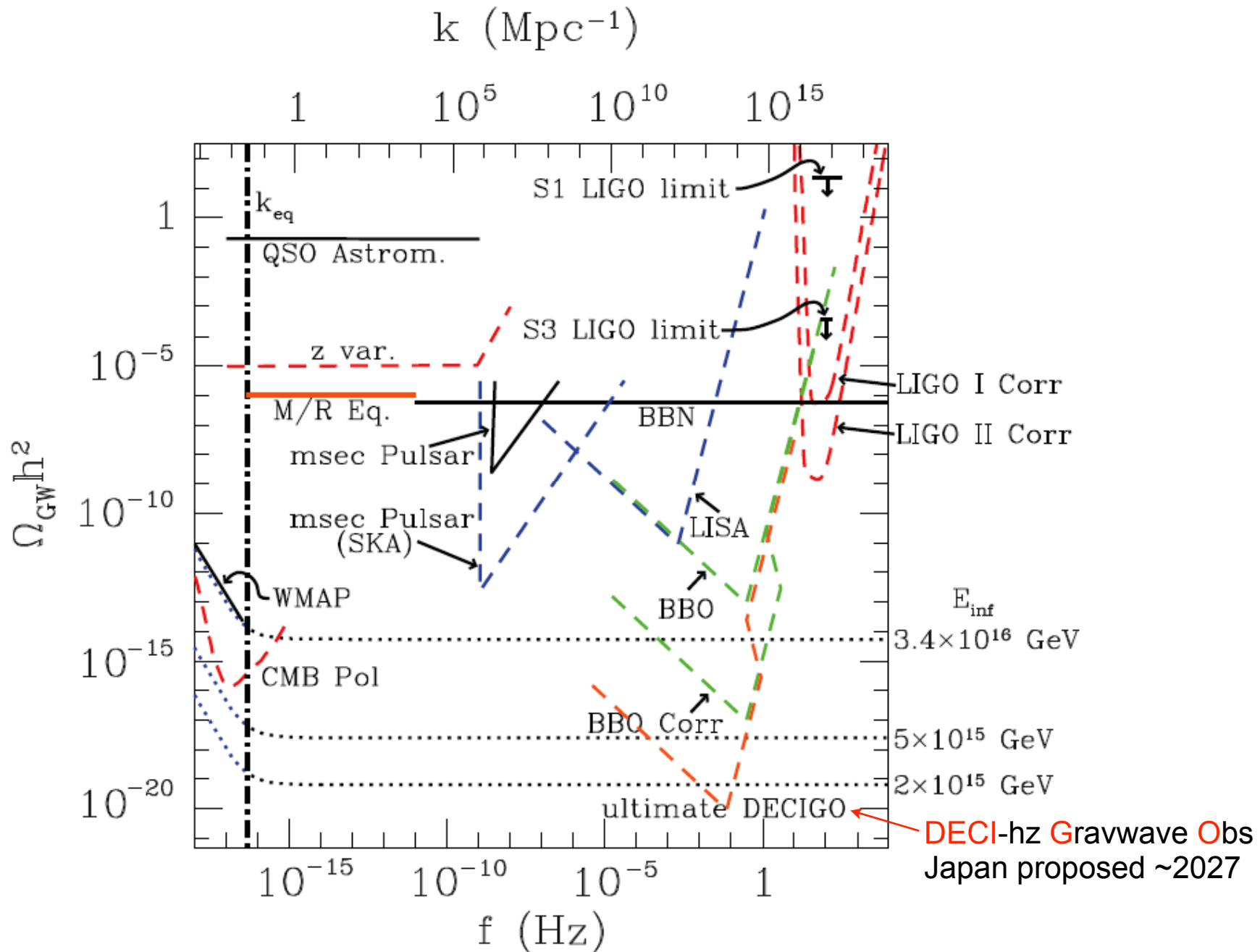


Though it may not be possible to measure the GWB using the advanced LIGO detectors, putting strong upper limit on the background is of great scientific importance.

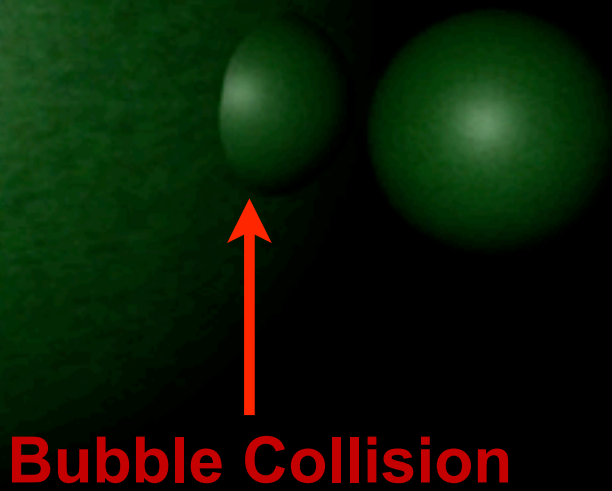


Strain amplitude sensitivity expected for pulsar timing (red), LISA (green), and Advanced LIGO (blue).

Gravity Waves from Inflation



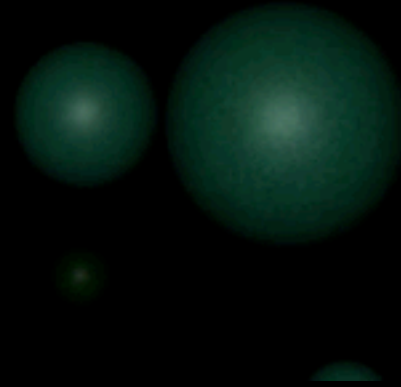
BUBBLE UNIVERSES IN ETERNAL INFLATION



Bubble Collision



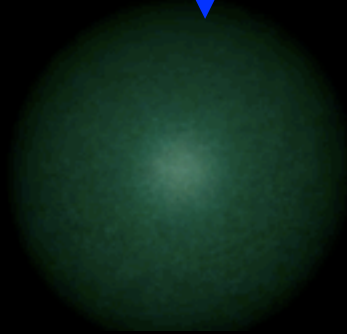
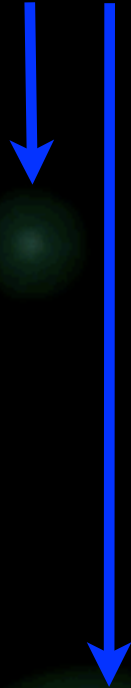
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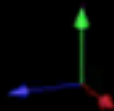


Nancy Abrams
Anthony Aguirre
Nina McCurdy
Joel Primack

**Expanding Bubbles
Getting Dimmer
Are Receding**

**BUBBLE
UNIVERSES
IN ETERNAL
INFLATION**





Post-Inflation

Baryogenesis: generation of excess of baryon (and lepton) number compared to anti-baryon (and anti-lepton) number. In order to create the observed baryon number today

$$\frac{n_B}{n_\gamma} = (6.1^{+0.3}_{-0.2}) \times 10^{-10}$$

it is only necessary to create an excess of about 1 quark and lepton for every $\sim 10^9$ quarks+antiquarks and leptons +antileptons.

Other things that might happen Post-Inflation:

Breaking of Pecci-Quinn symmetry so that the observable universe is composed of many PQ domains.

Formation of cosmic topological defects if their amplitude is small enough not to violate cosmological bounds.

Baryogenesis

There is good evidence that there are **no large regions of antimatter** (Cohen, De Rujula, and Glashow, 1998). It was **Andrei Sakharov** (1967) who first suggested that the baryon density might not represent some sort of initial condition, but might be understandable in terms of microphysical laws. He listed three ingredients to such an understanding:

1. **Baryon number violation** must occur in the fundamental laws. At very early times, if baryon number violating interactions were in equilibrium, then the universe can be said to have “started” with zero baryon number. Starting with zero baryon number, baryon number violating interactions are obviously necessary if the universe is to end up with a non-zero asymmetry. As we will see, apart from the philosophical appeal of these ideas, the success of inflationary theory suggests that, shortly after the big bang, the baryon number was essentially zero.
2. **CP-violation**: If CP (the product of charge conjugation and parity) is conserved, every reaction which produces a particle will be accompanied by a reaction which produces its antiparticle at precisely the same rate, so no baryon number can be generated.
3. **Departure from Thermal Equilibrium** (An Arrow of Time): The universe, for much of its history, was very nearly in thermal equilibrium. The spectrum of the CMBR is the most perfect blackbody spectrum measured in nature. So the universe was certainly in thermal equilibrium 10^5 years after the big bang. The success of the theory of big bang nucleosynthesis (BBN) provides strong evidence that the universe was in equilibrium two-three minutes after the big bang. But if, through its early history, the universe was in thermal equilibrium, then even B and CP violating interactions could not produce a net asymmetry. One way to understand this is to recall that the CPT theorem assures strict equality of particle and antiparticle masses, so at thermal equilibrium, the densities of particles and antiparticles are equal. More precisely, since B is odd under CPT, its thermal average vanishes in an equilibrium situation. This can be generalized by saying that the universe must have an arrow of time.

Following Dine & Kusenko, RMP 2004.

Several mechanisms have been proposed to understand the baryon asymmetry:

1. **GUT Baryogenesis**. Grand Unified Theories unify the gauge interactions of the strong, weak and electromagnetic interactions in a single gauge group. They inevitably violate baryon number, and they have heavy particles, with mass of order $M_{\text{GUT}} \approx 10^{16}$ GeV, whose decays can provide a departure from equilibrium. The main objections to this possibility come from issues associated with inflation. While there does not exist a compelling microphysical model for inflation, in most models, the temperature of the universe after reheating is well below M_{GUT} . But even if it were very large, there would be another problem. Successful unification requires supersymmetry, which implies that the graviton has a spin-3/2 partner, called the gravitino. In most models for supersymmetry breaking, these particles have masses of order TeV, and are very long lived. Even though these particles are weakly interacting, **too many gravitinos are produced unless the reheating temperature is well below the unification scale -- too low for GUT baryogenesis to occur.**

2. **Electroweak baryogenesis**. The Standard Model satisfies all of the conditions for baryogenesis, but any baryon asymmetry produced is far too small to account for observations. In certain extensions of the Standard Model, it is possible to obtain an adequate asymmetry, but in most cases **the allowed region of parameter space is very small.**

3. **Leptogenesis**. The possibility that the weak interactions will convert some lepton number to baryon number means that if one produces a large lepton number at some stage, this will be processed into a net baryon and lepton number at the electroweak phase transition. **The observation of neutrino masses makes this idea highly plausible.** Many but not all of the relevant parameters can be directly measured.

4. **Production by coherent motion of scalar fields (the Affleck-Dine mechanism)**, which can be highly efficient, **might well be operative if nature is supersymmetric.**

1. GUT Baryogenesis. GUTs satisfy all three of Sakharov's conditions.

Baryon number (B) violation is a hallmark of these theories: they typically contain gauge bosons and other fields which mediate B violating interactions such as proton decay.

CP violation is inevitable; necessarily, any model contains at least the Kobayashi-Maskawa (KM) mechanism for violating CP, and typically there are many new couplings which can violate CP.

Departure from equilibrium is associated with the dynamics of the massive, B violating fields. Typically one assumes that these fields are in equilibrium at temperatures well above the grand unification scale. As the temperature becomes comparable to their mass, the production rates of these particles fall below their rates of decay. Careful calculations in these models often lead to baryon densities compatible with what we observe.

Example: SU(5) GUT. Treat all quarks and leptons as left-handed fields. In a single generation of quarks and leptons one has the quark doublet Q , the singlet u -bar and d -bar antiquarks (their antiparticles are the right-handed quarks), and the lepton doublet, L .

$$L = \begin{pmatrix} e \\ \nu \end{pmatrix}$$

Then it is natural to identify fields in the 5-bar as follow:

$$\bar{5}_i = \begin{pmatrix} \bar{d} \\ \bar{d} \\ \bar{d} \\ e \\ \nu \end{pmatrix}$$

The remaining quarks and leptons (e- and e+) are in a 10 of SU(5).

The gauge fields are in the 24 (adjoint) representation:

$$\text{Color SU(3)} \quad T = \begin{pmatrix} \frac{\lambda^a}{2} & 0 \\ 0 & 0 \end{pmatrix} \quad \text{Weak SU(2)} \quad T = \begin{pmatrix} 0 & 0 \\ 0 & \frac{\sigma^i}{2} \end{pmatrix}$$

The U(1) generator is

$$Y' = \frac{1}{\sqrt{60}} \begin{pmatrix} 2 & & & & \\ & 2 & & & \\ & & 2 & & \\ & & & -3 & \\ & & & & -3 \end{pmatrix}$$

SU(5) is a broken symmetry, and it can be broken by a scalar Higgs field proportional to Y' . The unbroken symmetries are generated by the operators that commute with Y' , namely SU(3)xSU(2)xU(1). The vector bosons X that correspond to broken generators, for example

$$\begin{pmatrix} 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

gain mass $\sim 10^{16}$ GeV by this GUT Higgs mechanism.

The X bosons carry color and electroweak quantum numbers and mediate processes which violate baryon number. For example, there is a coupling of the X bosons to a d-bar quark and an electron.

In the GUT picture of baryogenesis, it is usually assumed that at temperatures well above the GUT scale, the universe was in thermal equilibrium. As the temperature drops below the mass of the X bosons, the reactions which produce the X bosons are not sufficiently rapid to maintain equilibrium. The decays of the X bosons violate baryon number; they also violate CP. So all three conditions are readily met: **B violation, CP violation, and departures from equilibrium.**

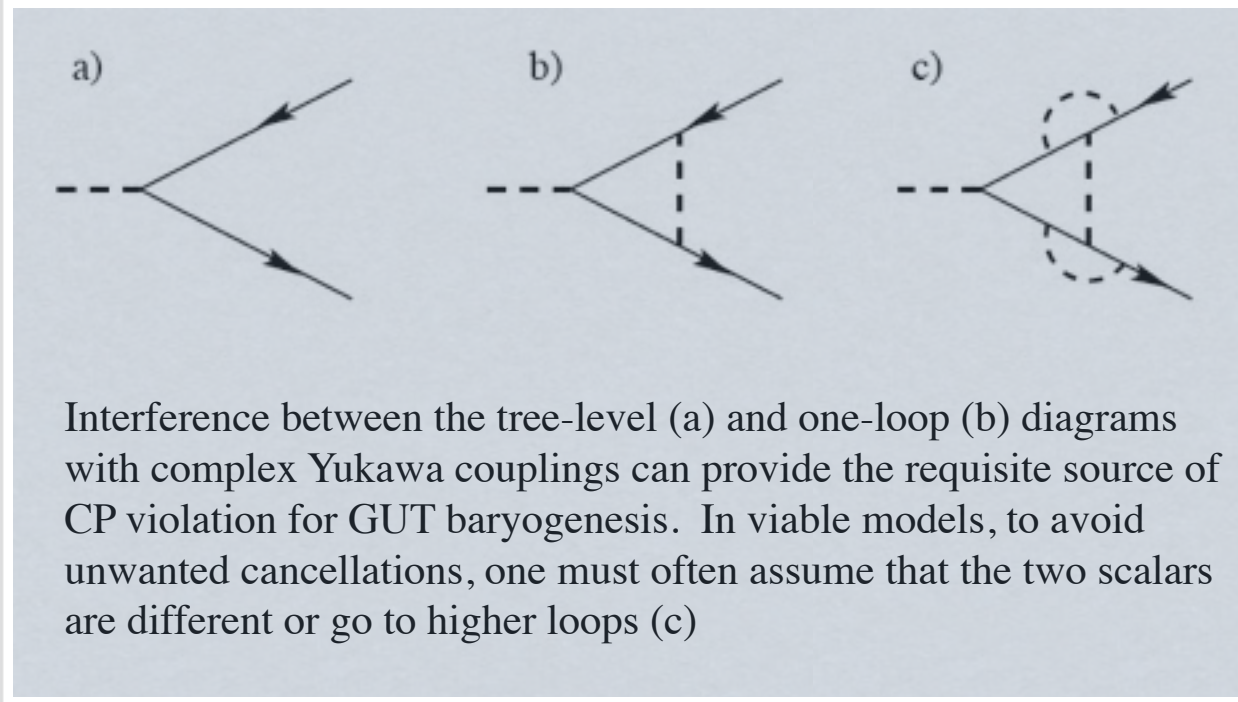
CPT requires that the total decay rate of X is the same as that of its antiparticle X-bar. But it does not require equality of the decays to particular final states (partial widths). So starting with equal numbers of X and X-bar particles, there can be a slight asymmetry between the processes

$$X \rightarrow dL; X \rightarrow \bar{Q}\bar{u}$$

and

$$\bar{X} \rightarrow \bar{d}\bar{L}; \bar{X} \rightarrow Qu.$$

This can result in a slight excess of matter over anti-matter. **But reheating to $T > 10^{16}$ GeV after inflation will overproduce gravitinos -- so GUT baryogenesis is now disfavored.**



2. Electroweak baryogenesis.

Below the electroweak scale of ~ 100 GeV, the **sphaleron** quantum tunneling process that violates B and L conservation (but preserves B - L) in the Standard Model is greatly suppressed, by $\sim \exp(-2\pi/\alpha_W) \sim 10^{-65}$. But at $T \sim 100$ GeV this process can occur. It can satisfy all three Sakharov conditions, but it cannot produce a large enough B and L. However, it can easily convert L into a mixture of B and L (Leptogenesis).

When one quantizes the Standard Model, one finds that the baryon number current is not exactly conserved, but rather satisfies

$$\partial_\mu j_B^\mu = \frac{3}{16\pi^2} F_{\mu\nu}^a \tilde{F}_{\mu\nu}^a = \frac{3}{8\pi^2} \text{Tr} F_{\mu\nu} \tilde{F}_{\mu\nu}.$$

The same parity-violating term occurs in the divergence of the lepton number current, so the difference (the B - L current) is exactly conserved. The parity-violating term is a total divergence

$$\text{Tr} F_{\mu\nu} \tilde{F}_{\mu\nu} = \partial_\mu K^\mu \quad \text{where} \quad K^\mu = \epsilon^{\mu\nu\rho\sigma} \text{tr} [F_{\nu\rho} A_\sigma + \frac{2}{3} A_\nu A_\rho A_\sigma] \quad , \quad \text{so}$$

$\tilde{j} = j_B^\mu - \frac{3g^2}{8\pi^2} K^\mu$ is conserved. In perturbation theory (i.e. Feynman diagrams)

K^μ falls to zero rapidly at infinity, so B and L are conserved.

In abelian -- i.e. $U(1)$ -- gauge theories, this is the end of the story. In non-abelian theories, however, there are non-perturbative field configurations, called instantons, which lead to violations of B and L. They correspond to calculation of a tunneling amplitude. To understand what the tunneling process is, one must consider more carefully the ground state of the field theory. Classically, the ground states are field configurations for which the energy vanishes. The trivial solution of this condition is $A = 0$, where A is the vector potential, which is the only possibility in $U(1)$. But a “pure gauge” is also a solution, where

$$\vec{A} = \frac{1}{i} g^{-1} \vec{\nabla} g,$$

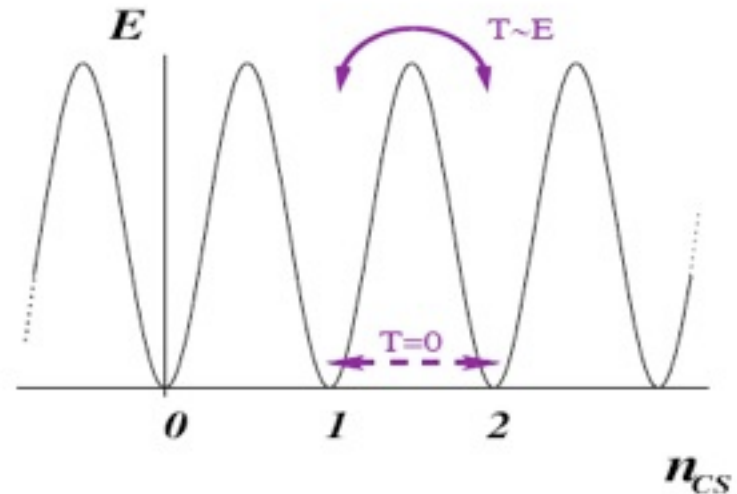
where g is a gauge transformation matrix. There is a class of gauge transformations g , labeled by a discrete index n , which must also be considered. These have the form

$$g_n(\vec{x}) = e^{i n f(\vec{x}) \hat{x} \cdot \tau / 2} \text{ where } f(x) \rightarrow 2\pi \text{ as } \vec{x} \rightarrow \infty, \text{ and } f(\vec{x}) \rightarrow 0 \text{ as } \vec{x} \rightarrow 0.$$

The ground states are labeled by the index n . If we evaluate the integral of the current K^μ we obtain a quantity known as the Chern-Simons number

$$n_{CS} = \frac{1}{16\pi^2} \int d^3x K^0 = \frac{2/3}{16\pi^2} \int d^3x \epsilon_{ijk} \text{Tr}(g^{-1} \partial_i g g^{-1} \partial_j g g^{-1} \partial_k g). \text{ For } g = g_n, n_{CS} = n.$$

Schematic Yang-Mills vacuum structure. At zero temperature, the instanton transitions between vacua with different Chern-Simons numbers are suppressed. At finite temperature, these transitions can proceed via sphalerons.



In tunneling processes which change the Chern-Simons number, because of the anomaly, the baryon and lepton numbers will change. The exponential suppression found in the instanton calculation is typical of tunneling processes, and in fact the instanton calculation is nothing but a field-theoretic WKB calculation. The probability that a single proton has decayed through this process in the history of the universe is infinitesimal. But this picture suggests that, at finite temperature, the rate should be larger. One can determine the height of the barrier separating configurations of different n_{CS} by looking for the field configuration which corresponds to sitting on top of the barrier. This is a solution of the static equations of motion with finite energy. It is known as a “[sphaleron](#)”. It follows that when the temperature is of order the ElectroWeak scale ~ 100 GeV, B and L violating (but B - L conserving) processes can proceed rapidly.

This result leads to three remarks:

1. If in the early universe, one creates baryon and lepton number, but no net $B - L$, B and L will subsequently be lost through sphaleron processes.
2. If one creates a net $B - L$ (e.g. creates a lepton number) the sphaleron process will leave both baryon and lepton numbers comparable to the original $B - L$. This realization is crucial to the idea of Leptogenesis.
3. The Standard Model satisfies, by itself, all of the conditions for baryogenesis. However, detailed calculations show that in the Standard Model the size of the baryon and lepton numbers produced are much too small to be relevant for cosmology, both because the Higgs boson is more massive than ~ 80 GeV and because the CKM CP violation is much too small. In supersymmetric extensions of the Standard Model it is possible that a large enough matter-antimatter asymmetry might be generated, but the parameter space for this is extremely small. (See Dine and Kusenko for details and references.)

This leaves Leptogenesis and Affleck-Dine baryogenesis as the two most promising possibilities. What is exciting about each of these is that, if they are operative, they have consequences for experiments which will be performed at accelerators over the next few years.

3. Leptogenesis.

There is now compelling experimental evidence that neutrinos have mass, both from solar and atmospheric neutrino experiments and accelerator and reactor experiments. The masses are tiny, fractions of an eV. The “see-saw mechanism” is a natural way to generate such masses. One supposes that in addition to the neutrinos of the Standard Model, there are some SU(2)xU(1)-singlet neutrinos, N. Nothing forbids these from obtaining a large mass. This could be of order M_{GUT} , for example, or a bit smaller. These neutrinos could also couple to the left handed doublets ν_L , just like right handed charged leptons. Assuming that these couplings are not particularly small, one would obtain a mass matrix, in the $\{N, \nu_L\}$ basis, of the form

$$M_\nu = \begin{pmatrix} M & M_W \\ M_W^T & 0 \end{pmatrix}$$

This matrix has an eigenvalue $\frac{M_W^2}{M}$.

The latter number is of the order needed to explain the neutrino anomaly for $M \sim 10^{13}$ or so, i.e. not wildly different than the GUT scale and other scales which have been proposed for new physics. For **leptogenesis** (Fukugita and Yanagida, 1986), what is important in this model is that the couplings of N break lepton number. N is a heavy particle; it can decay both to $h + \nu$ and $h + \bar{\nu}$, for example. The partial widths to each of these final states need not be the same. CP violation can enter through phases in the Yukawa couplings and mass matrices of the N's.

As the universe cools through temperatures of order the of masses of the N 's, they drop out of equilibrium, and their decays can lead to an excess of neutrinos over antineutrinos. Detailed predictions can be obtained by integrating a suitable set of Boltzmann equations. These decays produce a net lepton number, but not baryon number (and hence a net $B - L$). The resulting lepton number will be further processed by sphaleron interactions, yielding a net lepton and baryon number (recall that sphaleron interactions preserve $B - L$, but violate B and L separately). [Reasonable values of the neutrino parameters give asymmetries of the order we seek to explain.](#)

It is interesting to ask: assuming that these processes are the source of the observed asymmetry, how many parameters which enter into the computation can be measured, i.e. can we relate the observed number to microphysics. It is likely that, over time, many of the parameters of the light neutrino mass matrices, including possible CP-violating effects, will be measured. But while these measurements determine some of the couplings and masses, they are not, in general, enough. In order to give a precise calculation, analogous to the calculations of nucleosynthesis, of the baryon number density, one needs additional information about the masses of the fields N . One either requires some other (currently unforeseen) experimental access to this higher scale physics, or a compelling theory of neutrino mass in which symmetries, perhaps, reduce the number of parameters.

4. Production by coherent motion of scalar fields (the Affleck-Dine mechanism)

The formation of an AD condensate can occur quite generically in cosmological models. Also, the AD scenario potentially can give rise simultaneously to the ordinary matter and the dark matter in the universe. This can explain why the amounts of luminous and dark matter are surprisingly close to each other, within one order of magnitude. If the two entities formed in completely unrelated processes (for example, the baryon asymmetry from leptogenesis, while the dark matter from freeze-out of neutralinos), the observed relation $\Omega_{\text{DARK}} \sim \Omega_{\text{baryon}}$ is fortuitous.

In supersymmetric theories, the ordinary quarks and leptons are accompanied by scalar fields. These scalar fields carry baryon and lepton number. A coherent field, i.e., a large classical value of such a field, can in principle carry a large amount of baryon number. As we will see, it is quite plausible that such fields were excited in the early universe. To understand the basics of the mechanism, consider first a model with a single complex scalar field. Take the Lagrangian to be

$$\mathcal{L} = |\partial_\mu \phi|^2 - m^2 |\phi|^2$$

This Lagrangian has a symmetry, $\phi \rightarrow e^{i\alpha\phi}$, and a corresponding conserved current, which we will refer to as baryon current:

$$j_B^\mu = i(\phi^* \partial^\mu \phi - \phi \partial^\mu \phi^*).$$

It also possesses a “CP” symmetry: $\phi \leftrightarrow \phi^*$. With supersymmetry in mind, we will think of m as of order M_W .

Let us add interactions in the following way, which will closely parallel what happens in the supersymmetric case. Include a set of quartic couplings:

$$\mathcal{L}_I = \lambda|\phi|^4 + \epsilon\phi^3\phi^* + \delta\phi^4 + c.c.$$

These interactions clearly violate B. For general complex ϵ and δ , they also violate CP. In supersymmetric theories, as we will shortly see, the couplings will be extremely small. In order that these tiny couplings lead to an appreciable baryon number, it is necessary that the fields, at some stage, were very large.

To see how the cosmic evolution of this system can lead to a non-zero baryon number, first note that at very early times, when the Hubble constant, $H \gg m$, the mass of the field is irrelevant. It is thus reasonable to suppose that at this early time $\phi = \phi_0 \gg 0$. How does the field then evolve? First ignore the quartic interactions. In the expanding universe, the equation of motion for the field is as usual

$$\ddot{\phi} + 3H\dot{\phi} + \frac{\partial V}{\partial \phi} = 0.$$

At very early times, $H \gg m$, and so the system is highly overdamped and essentially frozen at ϕ_0 . At this point, $B = 0$.

Once the universe has aged enough that $H \ll m$, ϕ begins to oscillate. Substituting $H = 1/2t$ or $H = 2/3t$ for the radiation and matter dominated eras, respectively, one finds that

$$\phi = \begin{cases} \frac{\phi_o}{(mt)^{3/2}} \sin(mt) & \text{(radiation)} \\ \frac{\phi_o}{(mt)} \sin(mt) & \text{(matter)}. \end{cases}$$

In either case, the energy behaves, in terms of the scale factor, $R(t)$, as

$$E \approx m^2 \phi_o^2 \left(\frac{R_o}{R} \right)^3$$

Now let's consider the effects of the quartic couplings. Since the field amplitude damps with time, their significance will decrease with time. Suppose, initially, that $\phi = \phi_o$ is real. Then the imaginary part of ϕ satisfies, in the approximation that ϵ and δ are small,

$$\ddot{\phi}_i + 3H\dot{\phi}_i + m^2\phi_i \approx \text{Im}(\epsilon + \delta)\phi_r^3.$$

For large times, the right hand falls as $t^{-9/2}$, whereas the left hand side falls off only as $t^{-3/2}$. As a result, baryon number violation becomes negligible. The equation goes over to the free equation, with a solution of the form

$$\phi_i = a_r \frac{\text{Im}(\epsilon + \delta)\phi_o^3}{m^2(mt)^{3/4}} \sin(mt + \delta_r) \quad \text{(radiation)}, \quad \phi_i = a_m \frac{\text{Im}(\epsilon + \delta)\phi_o^3}{m^3t} \sin(mt + \delta_m) \quad \text{(matter)},$$

The constants can be obtained numerically, and are of order unity

$$a_r = 0.85 \quad a_m = 0.85 \quad \delta_r = -0.91 \quad \delta_m = 1.54.$$

But now we have a non-zero baryon number; substituting in the expression for the current,

$$n_B = 2a_r \text{Im}(\epsilon + \delta) \frac{\phi_o^2}{m(mt)^2} \sin(\delta_r + \pi/8) \quad (\text{radiation})$$

$$n_B = 2a_m \text{Im}(\epsilon + \delta) \frac{\phi_o^2}{m(mt)^2} \sin(\delta_m) \quad (\text{matter}).$$

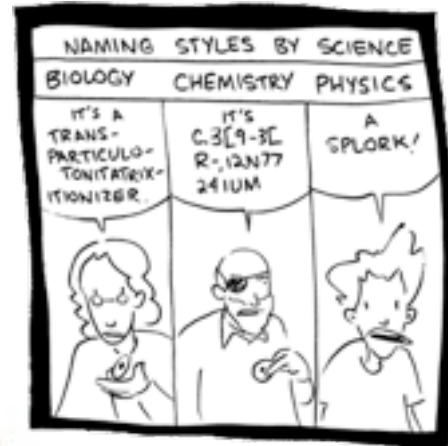
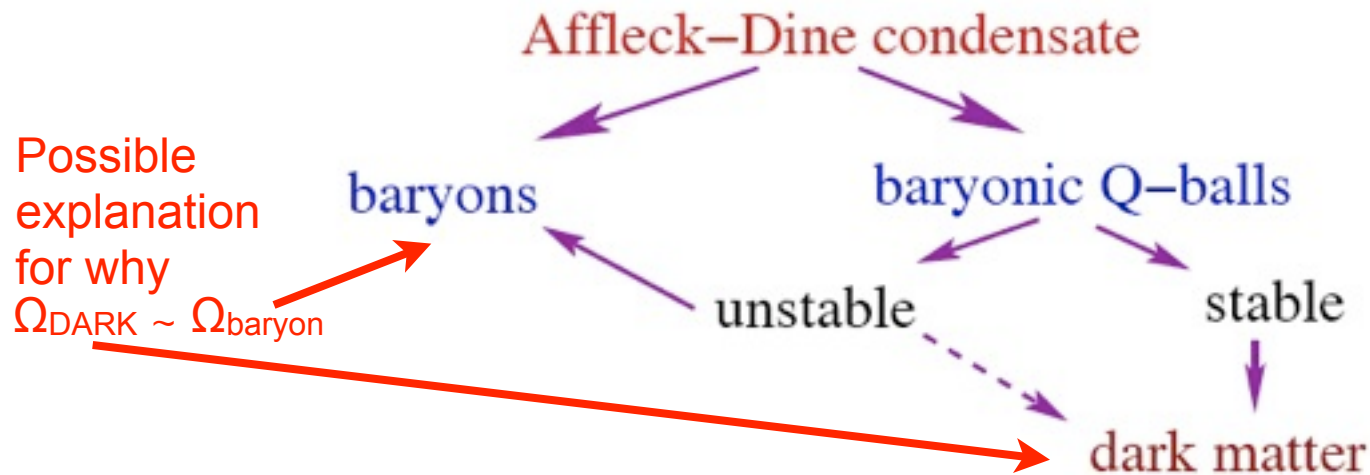
Two features of these results should be noted. First, if ϵ and δ vanish, n_B vanishes. If they are real, and ϕ_o is real, n_B vanishes. It is remarkable that the Lagrangian parameters can be real, and yet ϕ_o can be complex, still giving rise to a net baryon number. Supersymmetry breaking in the early universe can naturally lead to a very large value for a scalar field carrying B or L. Finally, as expected, n_B is conserved at late times.

This mechanism for generating baryon number could be considered without supersymmetry. In that case, it begs several questions:

- What are the scalar fields carrying baryon number?
- Why are the ϕ^4 terms so small?
- How are the scalars in the condensate converted to more familiar particles?

In the context of supersymmetry, there is a natural answer to each of these questions. First, there are scalar fields (squarks and sleptons) carrying baryon and lepton number. Second, in the limit that supersymmetry is unbroken, there are typically directions in the field space in which the quartic terms in the potential vanish. Finally, the scalar quarks and leptons will be able to decay (in a baryon and lepton number conserving fashion) to ordinary quarks.

In addition to topologically stable solutions to the field equations such as strings or monopoles, it is sometimes also possible to find non-topological solutions, called Q-balls, which can form as part of the Affleck-Dine condensate. These are usually unstable and could decay to the dark matter, but in some theories they are stable and could be the dark matter. The various possibilities are summarized as follows:



The parameter space of the MSSM consistent with LSP dark matter is very different, depending on whether the LSPs froze out of equilibrium or were produced from the evaporation of AD baryonic Q-balls. If supersymmetry is discovered, one will be able to determine the properties of the LSP experimentally. This will, in turn, provide some information on the how the dark-matter SUSY particles could be produced. The discovery of a Higgsino-like LSP would be a evidence in favor of Affleck-Dine baryogenesis. This is a way in which we might be able to establish the origin of matter-antimatter asymmetry.

Review of mechanisms that have been proposed to generate the baryon asymmetry:

1. **GUT Baryogenesis.** Grand Unified Theories unify the gauge interactions of the strong, weak and electromagnetic interactions in a single gauge group. They inevitably violate baryon number, and they have heavy particles, with mass of order $M_{\text{GUT}} \approx 10^{16}$ GeV, whose decays can provide a departure from equilibrium. The main objections to this possibility come from issues associated with inflation. While there does not exist a compelling microphysical model for inflation, in most models, the temperature of the universe after reheating is well below M_{GUT} . But even if it were very large, there would be another problem. Successful unification requires supersymmetry, which implies that the graviton has a spin-3/2 partner, called the gravitino. In most models for supersymmetry breaking, these particles have masses of order TeV, and are very long lived. Even though these particles are weakly interacting, **too many gravitinos are produced unless the reheating temperature is well below the unification scale -- too low for GUT baryogenesis to occur.**

2. **Electroweak baryogenesis.** The Standard Model satisfies all of the conditions for baryogenesis, but any baryon asymmetry produced is far too small to account for observations. In certain extensions of the Standard Model, it is possible to obtain an adequate asymmetry, but in most cases **the allowed region of parameter space is very small.**

3. **Leptogenesis.** The possibility that the weak interactions will convert some lepton number to baryon number means that if one produces a large lepton number at some stage, this will be processed into a net baryon and lepton number at the electroweak phase transition. **The observation of neutrino masses makes this idea highly plausible.** Many but not all of the relevant parameters can be directly measured.

4. **Production by coherent motion of scalar fields (the Affleck-Dine mechanism),** which can be highly efficient, **might well be operative if nature is supersymmetric.**

SPACE

Do Invisible Galaxies Swirl Around the Milky Way?

By MICHAEL D. LEMONICK Thursday, Jan. 19, 2012

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Invisible galaxy said likely made of dark matter

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What's The Matter?: Cold Dark Matter and the Milky Way's Missing Satellites

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Thanks to Piero Madau!

small scale issues

Angular momentum

The Eris simulation shows that Λ CDM simulations are increasingly able to form realistic spiral galaxies, as resolution improves and feedback becomes more realistic.

Cusps

WDM doesn't resolve cusp issues. New observations and simulations suggest that observed velocity structure of LSB, dSpiral, dSph galaxies may be consistent with cuspy Λ CDM halos. But the "too big to fail" problem needs solution.

Satellites and Subhalos

The discovery of many faint Local Group dwarf galaxies is consistent with Λ CDM predictions. Satellites, reionization, lensing flux anomalies, gaps in stellar streams, and Ly α forest data imply that **WDM** must be **Tepid** or **Cooler**.

Cusps

WDM doesn't resolve cusp issues. New observations and simulations suggest that observed velocity structure of LSB and dSpiral galaxies may be consistent with cuspy Λ CDM halos. But the “too big to fail” problem needs solution.

New Developments

- New observations undermine some previous evidence for dark matter cores in dwarf galaxies
- The properties of density cores of dwarf spiral galaxies are inconsistent with expectations from **WDM**
- New simulations show that gas blowout during evolution of dwarf spiral galaxies can remove cusps
- But the biggest subhalos in MVy size dark matter simulations may be too dense to host the observed satellites

Beware of darkness: A cuspy dark matter halo from stellar kinematics where gas shows a core

NGC 2976 presented in ApJ, Vol. 745, 92, 2012; 10 more galaxies coming in future papers

Joshua J. Adams¹, Joshua D. Simon¹, Karl Gebhardt², Guillermo A. Blanc¹, Maximilian H. Fabricius³, Gary J. Hill⁴,
Jeremy D. Murphy², Remco C.E. van den Bosch⁵, Glenn van de Ven⁵

We here present measurements and anisotropic Jeans models for late-type dwarfs obtained from stellar kinematics. Until recently, DM mass profiles in such systems have been obtained exclusively from atomic or ionized gas. The nearby member of the M81 group, NGC 2976 (SAc), has been measured in ionized gas to have a DM core with a strong constraint on the DM power law index of $0.01 < \alpha < 0.17$ (Simon et al. 2003), where $\alpha=1$ corresponds to the center of an NFW profile. **In our first work on NGC 2976, we confirm that the simplest models from gas kinematics reveal a cored DM halo but find that the stellar kinematics are most consistent with an NFW profile. We advocate the stellar kinematics as more robust due to the tracer's collisionless nature while the gas is subject to more uncertainties from radial motion, warped disks, and pressure support.** We are making an ongoing study by which the type, strength, and conditions of feedback can be constrained from new measurements and comparison to simulations.

Joshua Adams poster at KITP Conference “First Light and Faintest Dwarfs” February 2012

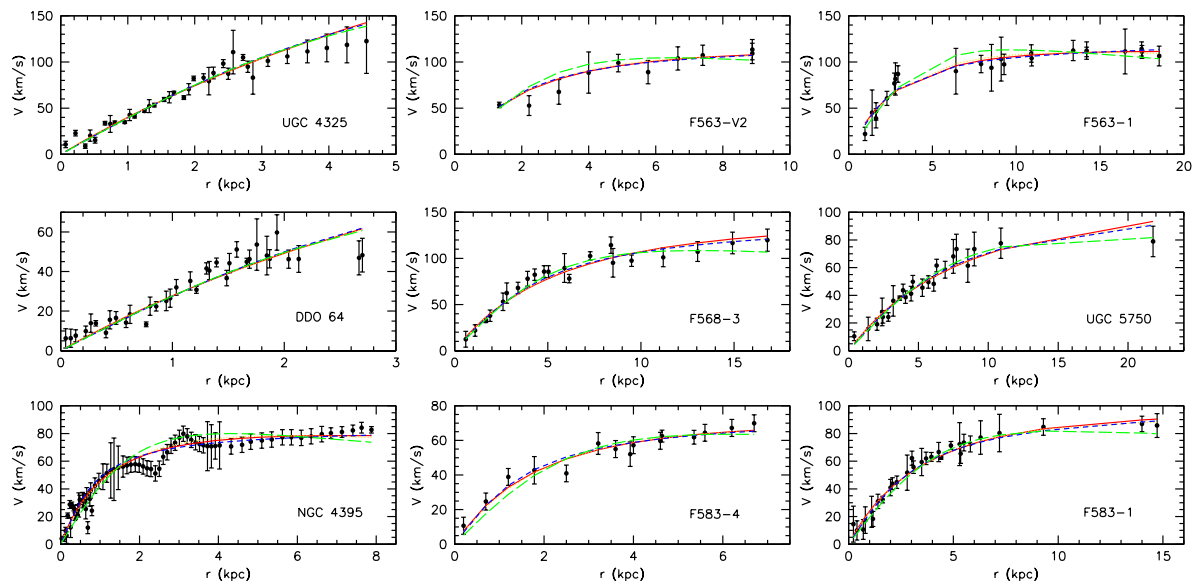
The Case Against Warm or Self-Interacting Dark Matter as Explanations for Cores in Low Surface Brightness Galaxies

2010, ApJ, 710L, 161

[Rachel Kuzio de Naray, Gregory D. Martinez, James S. Bullock, Manoj Kaplinghat](#)

Warm dark matter (WDM) and self-interacting dark matter (SIDM) are often motivated by the inferred cores in the dark matter halos of low surface brightness (LSB) galaxies. We test thermal WDM, non-thermal WDM, and SIDM using high-resolution rotation curves of nine LSB galaxies. If the core size is set by WDM particle properties, then **even the smallest cores we infer would require primordial phase space density values that are orders of magnitude smaller than lower limits obtained from the Lyman alpha forest power spectra**. We also find that the dark matter halo core densities vary by a factor of about 30 while showing no systematic trend with the maximum rotation velocity of the galaxy. This strongly argues against the core size being directly set by large self-interactions (scattering or annihilation) of dark matter. **We therefore conclude that the inferred cores do not provide motivation to prefer WDM or SIDM over other dark matter models.**

We fit these dark matter models to the data and determine the halo core radii and central densities. While the minimum core size in WDM models is predicted to **decrease** with halo mass, we find that the inferred core radii **increase** with halo mass and also cannot be explained with a single value of the primordial phase space density.



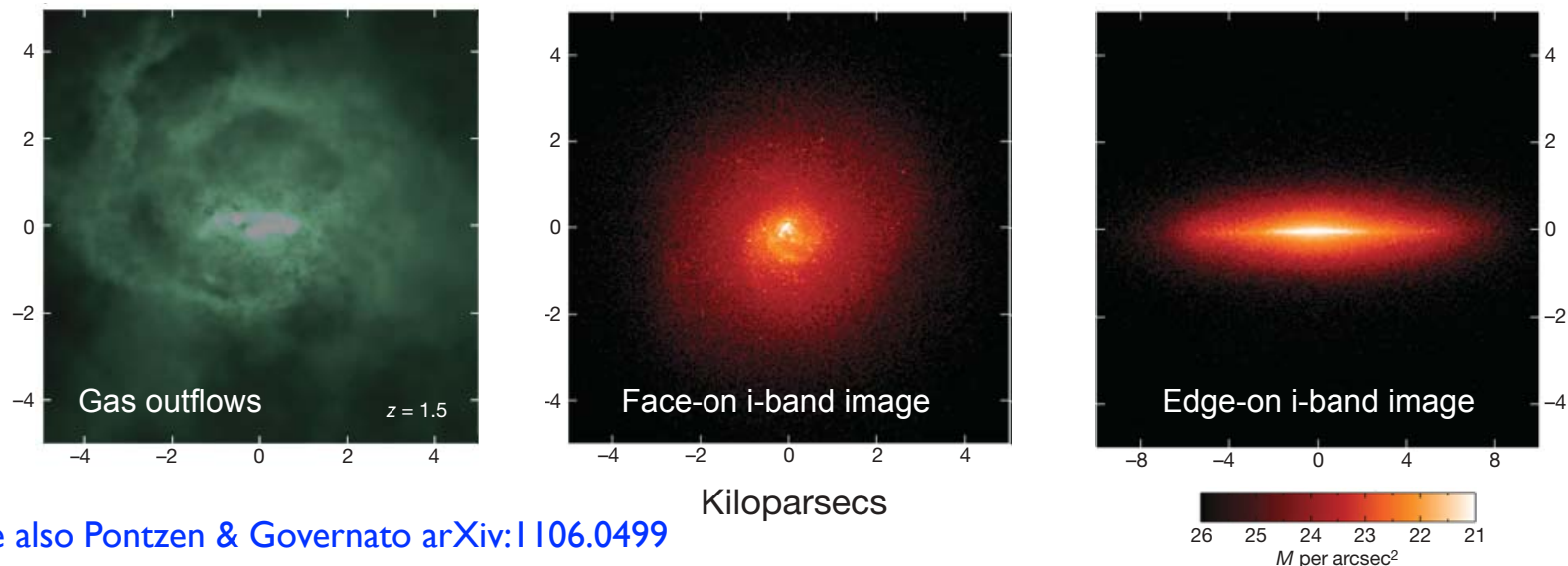
New simulations show that several episodes of gas blowout during evolution of dwarf spiral galaxies can remove cusps

Bulgeless dwarf galaxies and dark matter cores from supernova-driven outflows

F. Governato, C. Brook, L. Mayer, A. Brooks, G. Rhee, J. Wadsley, P. Jonsson, B. Willman, G. Stinson, T. Quinn & P. Madau

Nature 463, 203 (Jan 2010)

Most observed dwarf galaxies consist of a rotating stellar disk embedded in a massive dark-matter halo with a near-constant-density core. Models based on CDM, however, invariably form galaxies with dense spheroidal stellar bulges and steep central dark-matter profiles, because low-angular-momentum baryons and dark matter sink to the centers of galaxies through accretion and repeated mergers. Here we report hydrodynamical simulations in which the inhomogeneous interstellar medium is resolved. **Strong outflows from supernovae remove low-angular-momentum gas, which inhibits the formation of bulges and decreases the dark-matter density to less than half of what it would otherwise be within the central kiloparsec. The analogues of dwarf galaxies—bulgeless and with shallow central dark-matter profiles—arise naturally in these simulations.** Simulations using the same implementation of star formation and feedback reproduce some global scaling properties of observed galaxies across a range of masses and redshifts.



See also Pontzen & Governato arXiv:1106.0499

Cuspy No More: How Outflows Affect the Central Dark Matter and Baryon Distribution in Λ CDM Galaxies.

F.Governato^{1*}, A.Zolotov², A.Pontzen³, C.Christensen⁴, S.H.Oh^{5,6}, A.M.Brooks⁷, T.Quinn¹, S.Shen⁸, J.Wadsley⁹, MNRAS in press 2012

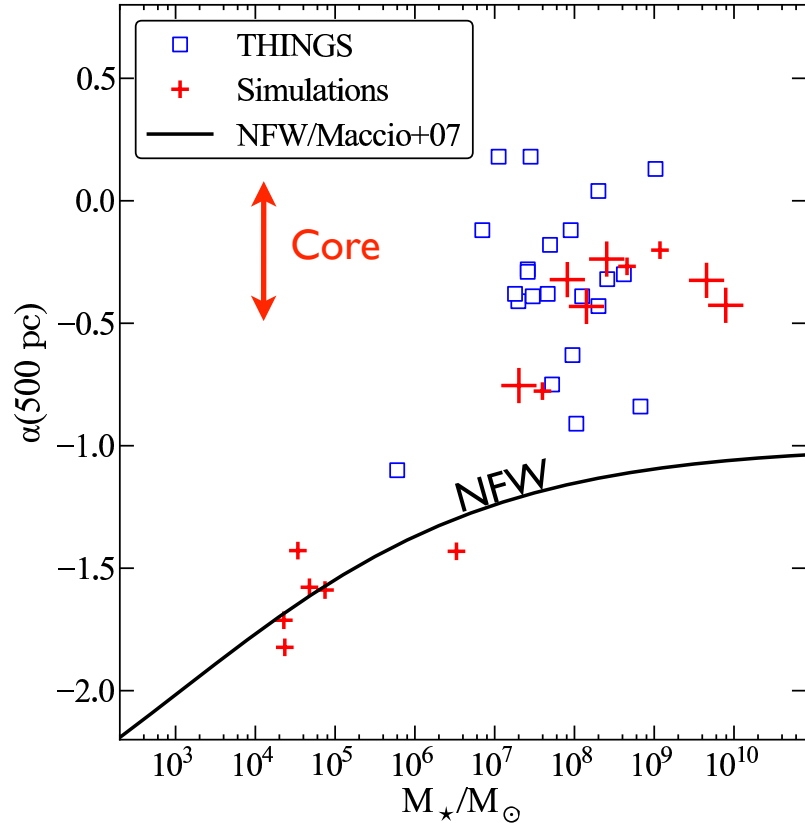


Figure 1. The slope of the dark matter density profile α vs stellar mass measured at 500 pc and $z=0$ for all the resolved halos in our sample. The Solid 'DM-only' line is the slope predicted for the same CDM cosmological model assuming i) the NFW concentration parameter trend given by Macció et al (2007) and ii) the same stellar mass vs halo mass relation as measured in our simulations to convert from halo masses. Large Crosses: haloes resolved with more than 0.5×10^6 DM particles within R_{vir} . Small crosses: more than 5×10^4 DM particles. The small squares represent 22 observational data points measured from galaxies from the THINGS and LITTLE THINGS surveys.

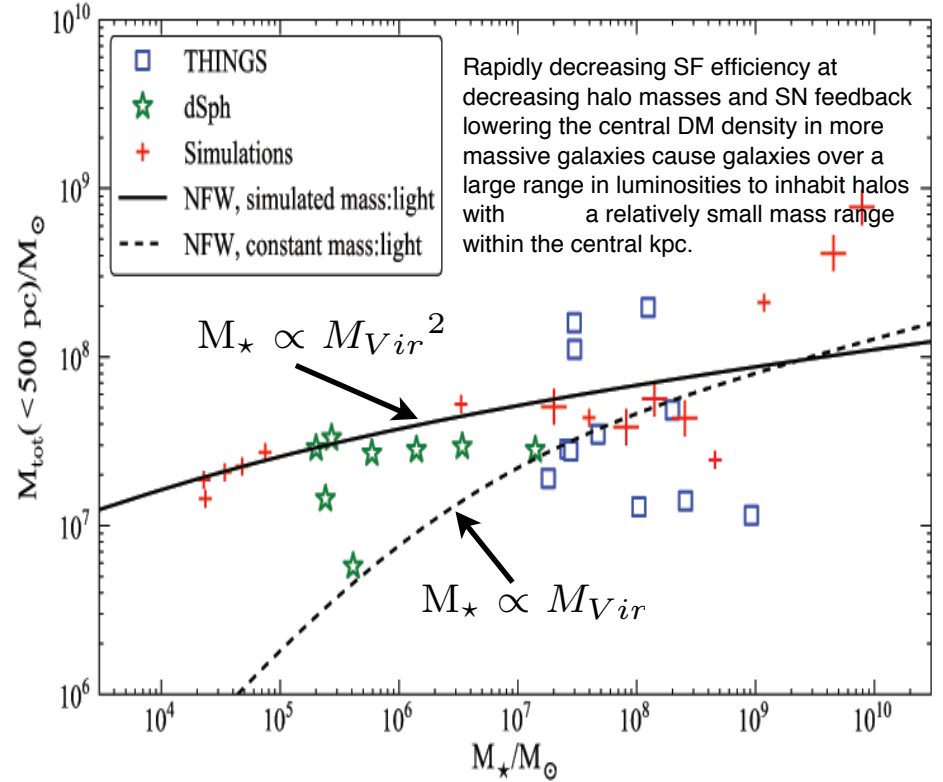


Figure 4. The total mass (baryons and DM) within the central 500 pc as a function of stellar mass: Large and small crosses: simulations. Open squares: galaxies from THINGS (Oh et al. in prep). Stars: dSph from Walker (priv. comm.). Theoretical predictions reproduce the observed flat trend from 10^5 to $10^9 M_\odot$. This is largely due to the large drop in SF efficiency at small halo masses, that stretches the range of galaxy luminosities over a relatively smaller halo mass range. The solid and dashed lines assume different stellar mass - total halo mass relations. A close fit to the simulations as $M^* \sim M_{vir}^2$ (solid) and one showing $M^* \sim M_{vir}$ (dashed). Only when the star formation efficiency is a steep function of halo mass it is possible to reproduce the observed trend, as discussed in §4. More massive galaxies above the solid line have a small bulge component.

Using separately higher metal stars at lower radii plus lower metal stars farther out gives dm radial slope inconsistent with NFW at high confidence for Sculptor and Fornax dwarf spheroidal MWy satellites.

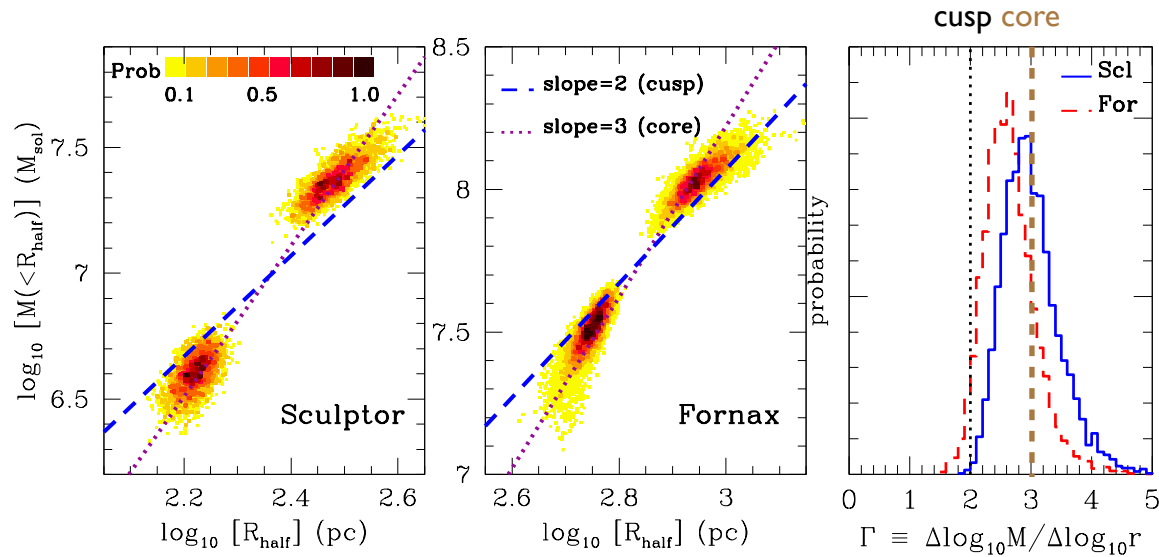


FIG. 10.— *Left, center*: Constraints on half-light radii and masses enclosed therein, for two independent stellar subcomponents in the Fornax and Sculptor dSphs. Plotted points come directly from our final MCMC chains, and color indicates relative likelihood (normalized by the maximum-likelihood value). Overplotted are straight lines indicating the central (and therefore maximum) slopes of cored ($\lim r \rightarrow 0 d \log M/d \log r = 3$) and cusped ($\lim r \rightarrow 0 d \log M/d \log r = 2$) dark matter halos. *Right*: Posterior PDFs for the slope Γ obtained for Fornax and Sculptor. The vertical dotted line marks the maximum (i.e., central) value of an NFW profile (i.e., cusp with $\gamma_{\text{DM}} = 1$, $\lim r \rightarrow 0 [d \log M/d \log r] = 2$). These measurements rule out NFW and/or steeper cusps ($\gamma_{\text{DM}} \geq 1$) with significance $s \geq 96\%$ (Fornax) and $s \geq 99\%$ (Sculptor).

Similar results for Sculptor in Amorisco & Evans 2012 MNRAS. Jardel & Gebhardt present a Schwarzschild model fit to the Fornax dwarf, again favoring core rather than cusp.

Satellites and Subhalos

The discovery of many faint Local Group dwarf galaxies is consistent with Λ CDM predictions. Satellites, reionization, lensing flux anomalies, stellar streams, and Ly α forest data imply that **WDM** must be **Tepid** or **Cooler**.

New Developments

- The “too big to fail” problem appears to be the most serious current challenge for Λ CDM, and may indicate the need for a more complex theory of dark matter.
- High resolution Λ CDM simulation substructure is consistent with quad-lens radio quasar flux and galaxy-galaxy lensing anomalies and indications of substructure by stellar stream gaps.
- Λ CDM predicts that there is a population of low-luminosity stealth galaxies around the Milky Way. Will new surveys with bigger telescopes find them?

The “too big to fail” problem

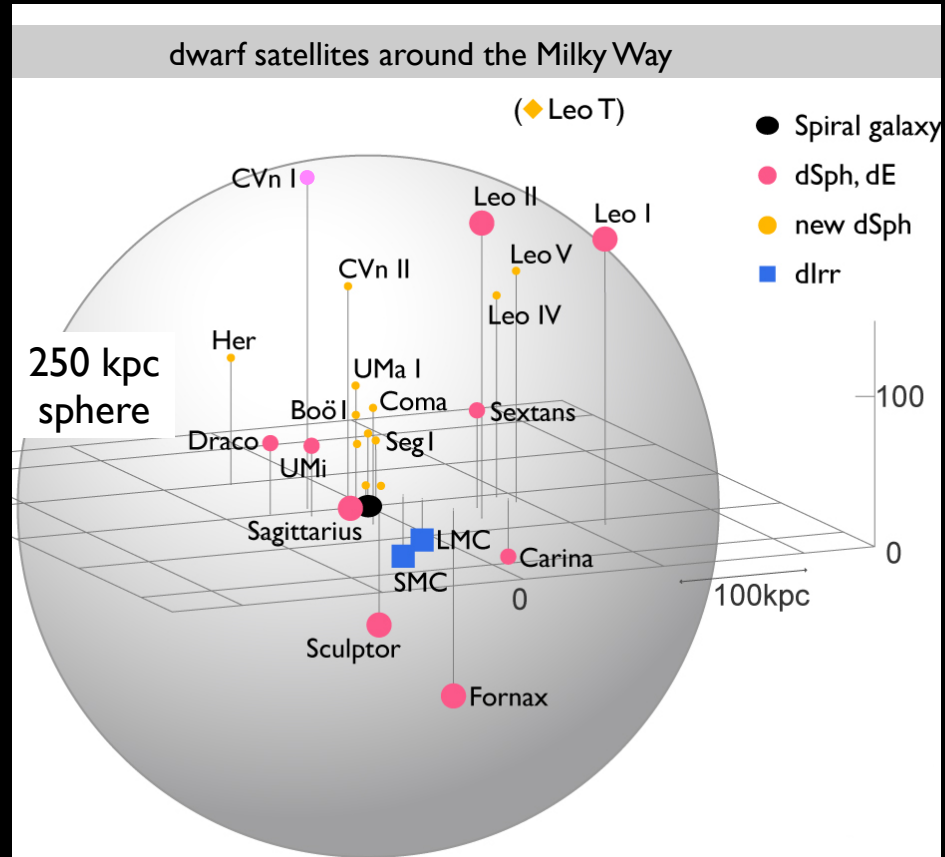
Λ CDM subhalos vs. Milky Way satellites

“Missing satellites”: Klypin et al. 1999, Moore et al. 1999

Aquarius Simulation

$>10^5$ identified subhalos

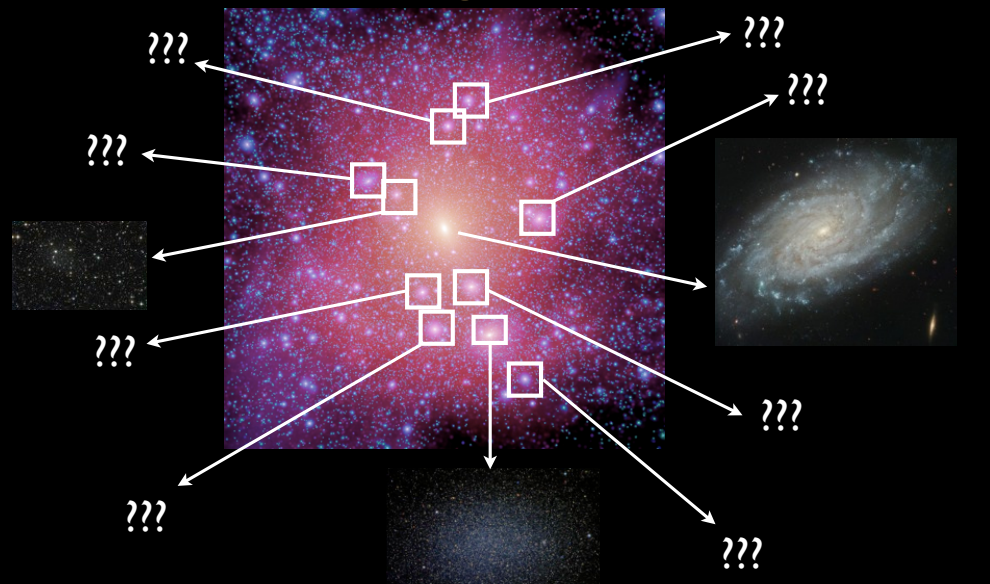
V. Springel / Virgo Consortium



12 bright satellites ($L_V > 10^5 L_\odot$)

S. Okamoto

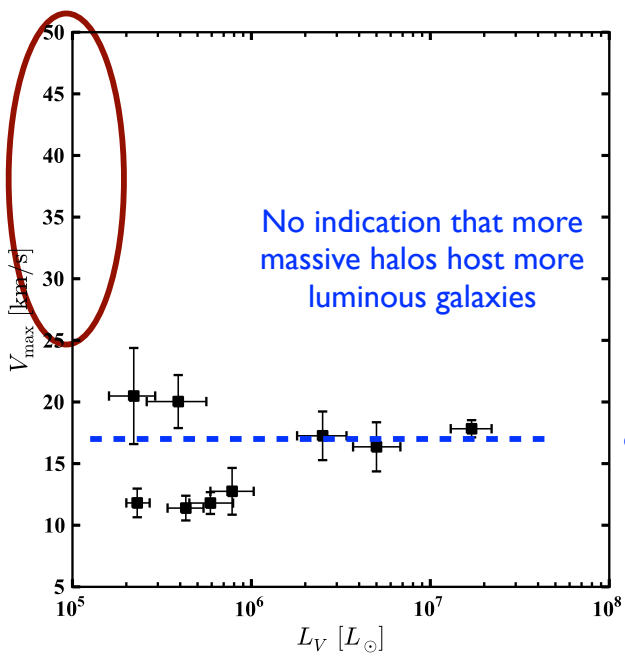
Of the ~10 biggest subhalos, ~8 cannot host any known bright MW satellite



Observed Milky Way Satellites

“massive failures”:
highest resolution LCDM simulations predict ~10 subhalos in this range in the MW, but we don't see **any** such galaxies [except Sagittarius (?)]

All of the bright MW dSphs are consistent with $V_{\text{max}} \lesssim 25$ km/s (see also Strigari, Frenk, & White 2010)



■ LMC
■ SMC

Possible Solutions to “too big to fail”

- Baryons strongly modify the structure of subhalos?
- The Milky Way is anomalous?
- The Milky Way has a low mass dark matter halo?
- Galaxy formation is stochastic at low masses?
- Dark matter is not just **CDM** -- maybe **WDM** or even self-interacting?
- (Or maybe existing high-resolution CDM simulations are being misinterpreted?)

Michael Boylan-Kolchin, Bullock, Kaplinghat 2011, 2012

CDM

Diameter of visible Milky Way
30 kpc = 100,000 light years



Diameter of Milky Way Dark Matter Halo
1.5 million light years



Aquarius simulation. Springel et al. 2008

WDM

Diameter of visible Milky Way
30 kpc = 100,000 light years



Diameter of Milky Way Dark Matter Halo
1.5 million light years



Lovell, Eke, Frenk, et al. arXiv:1104.2929

WDM simulation at right has no “too big to fail” subhalos, but it doesn’t lead to the right systematics to fit dwarf galaxy properties as Kuzio de Naray et al. showed. It also won’t have the subhalos needed to explain radio flux anomalies and gaps in stellar streams.

Possible Solution: Milky-Way-size halos in low-density regions have fewer DM satellites, according to new simulations.

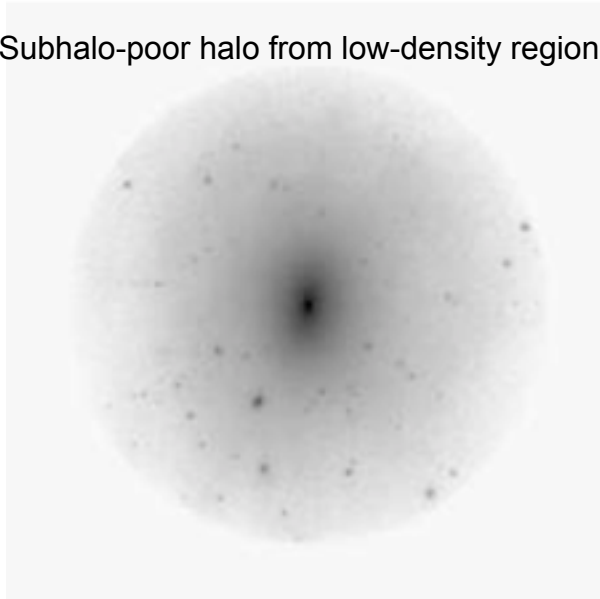
Environmental effect on the subhalo abundance -- a solution to the missing dwarf problem,

Tomoaki Ishiyama, Toshiyuki Fukushige, Junichiro Makino

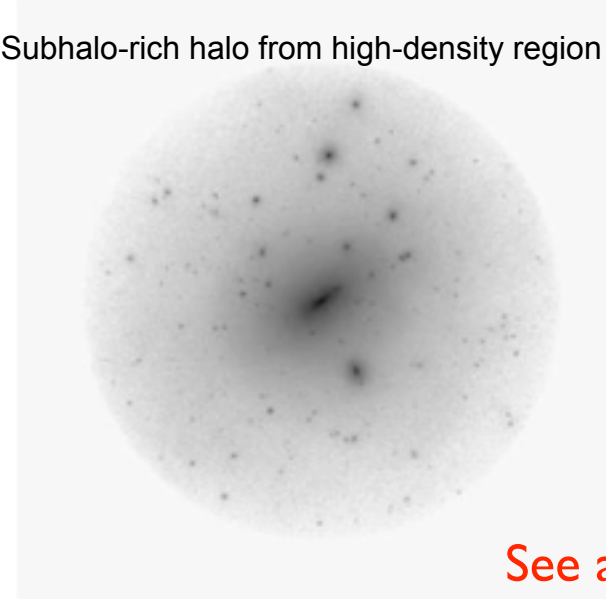
PASJ, 60, 13 (2009a)

We have performed simulation of a single large volume and measured the abundance of subhalos in all massive halos. We found that the variation of the subhalo abundance is very large, and those with largest number of subhalos correspond to simulated halos in previous studies. The subhalo abundance depends strongly on the local density of the background. Halos in high-density regions contain large number of subhalos. Our galaxy is in the low-density region. For our simulated halos in low-density regions, the number of subhalos is within a factor of three to that of our galaxy. We argue that the "missing dwarf problem" is not a real problem but caused by the biased selection of the initial conditions in previous studies, which were not appropriate for field galaxies.

Subhalo-poor halo from low-density region



Subhalo-rich halo from high-density region



See also Ishiyama,
Makino, +
CosmoGrid Sim
arXiv:1101.2020

Ishiyama+09 **Variation of the Subhalo Abundance in Dark Matter Halos**

Halos formed earlier have smaller number of subhalos at present.

ApJ, 696, 2115 (2009)

New miniBolshoi simulation will provide statistics

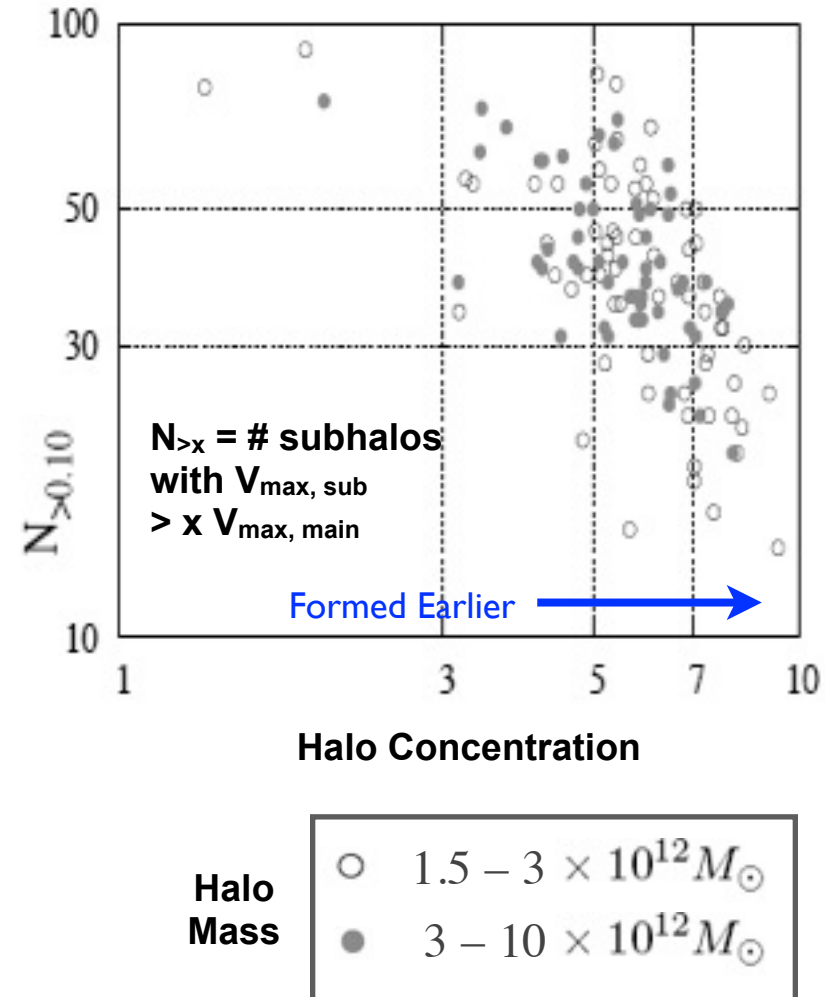
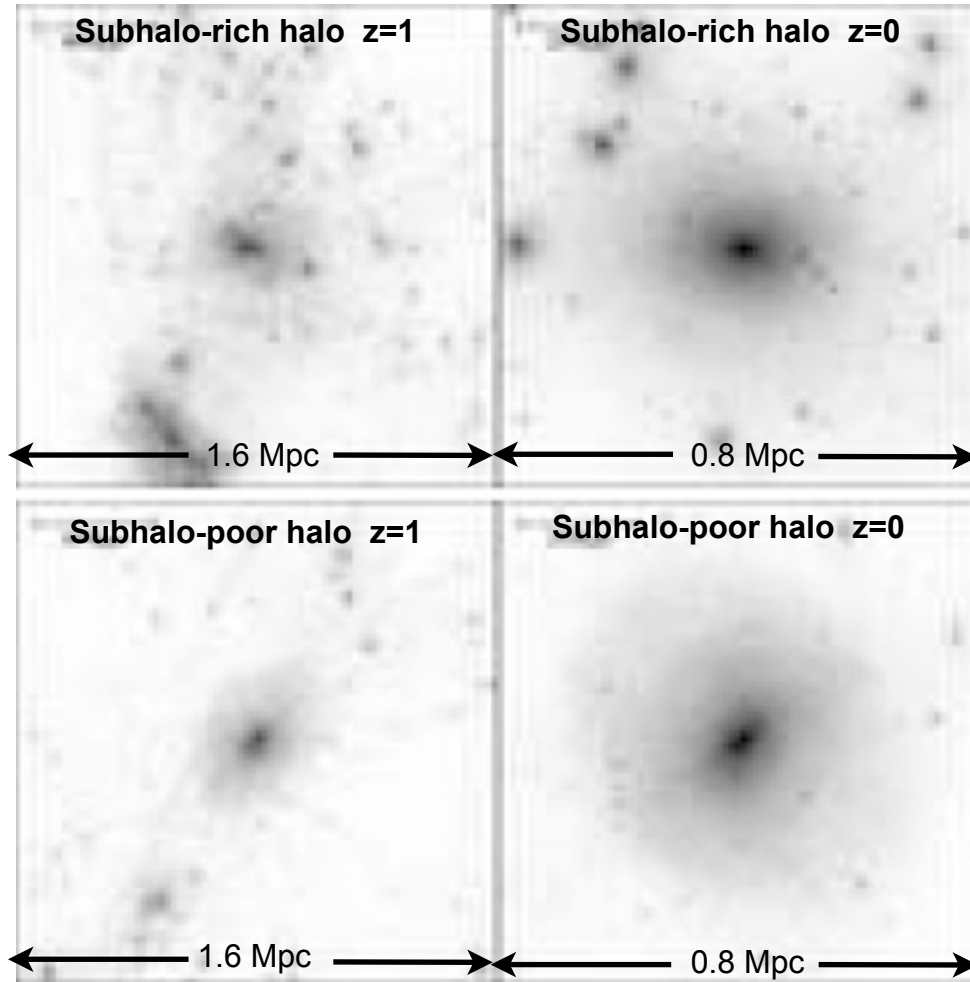
Milky-Way-size halos have large variation in number of DM satellites, according to new simulations.

Ishiyama, Fukushige, and Makino

Variation of the Subhalo Abundance in Dark Matter Halos

ApJ, 696, 2115 (2009b)

Galaxy halos formed earlier have higher concentration and smaller number of subhalos at present .
Mass resolution $1 \times 10^6 M_{\text{sun}}$ (3x better than 2009a). Force resolution 700 pc (2x better than 2009a).



Radio flux-ratio anomalies

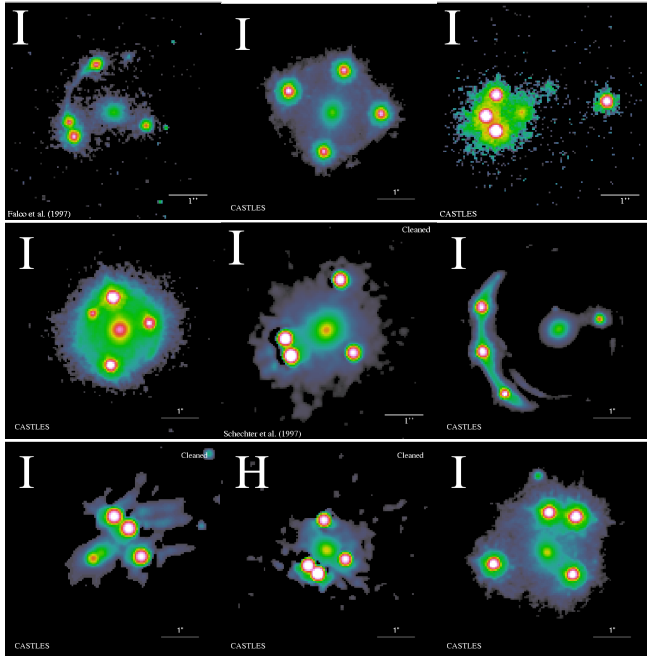
Flux ratio anomalies are generic

Quasar lenses

“Easy” to explain image positions (even to $\sim 0.1\%$ precision)

- ▶ ellipsoidal galaxy
- ▶ tidal forces from environment

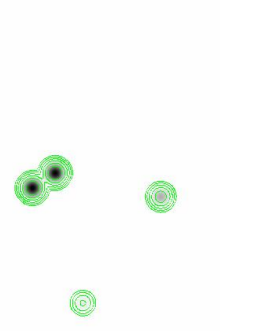
But hard to explain flux ratios!



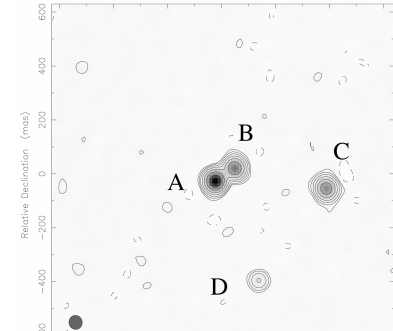
(CASTLES project, <http://www.cfa.harvard.edu/castles>)

**Radio flux-ratio anomalies \Rightarrow
Strong evidence for dark matter
clumps $\sim 10^6 - 10^8$ Msun
as expected in Λ CDM**

expected



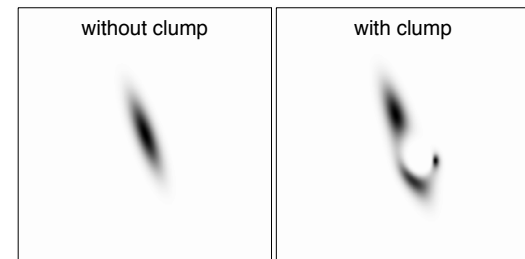
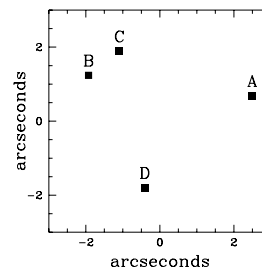
observed (Marlow et al. 1999)



Substructure and lensing

Q) What happens if lens galaxies contain mass clumps?

A) The clumps distort the images on small scales.



(cf. Mao & Schneider 1998; Metcalf & Madau 2001; Chiba 2002)

The Aquarius simulations have not quite enough substructure to explain quad-lens radio quasar flux anomalies -- but perhaps including baryons in simulations will help.

Effects of dark matter substructures on gravitational lensing: results from the Aquarius simulations

D. D. Xu, Shude Mao, Jie Wang, V. Springel, Liang Gao, S. D. M. White, Carlos S. Frenk, Adrian Jenkins, Guoliang Li and Julio F. Navarro MNRAS **398**, 1235–1253 (2009)

We conclude that line-of-sight structures can be as important as intrinsic substructures in causing flux-ratio anomalies. ... This alleviates the discrepancy between models and current data, but a larger observational sample is required for a stronger test of the theory.

Effects of Line-of-Sight Structures on Lensing Flux-ratio Anomalies in a Λ CDM Universe

D. D. Xu, Shude Mao, Andrew Cooper, Liang Gao, Carlos S. Frenk, Raul Angulo, John Helly MNRAS (2012)

We investigate the statistics of flux anomalies in gravitationally lensed QSOs as a function of dark matter halo properties such as substructure content and halo ellipticity. ... The constraints that we are able to measure here with current data are roughly consistent with Λ CDM N-body simulations.

Constraints on Small-Scale Structures of Dark Matter from Flux Anomalies in Quasar Gravitational Lenses

R. Benton Metcalf, Adam Amara MNRAS **419**, 3414 (2012)

Substructure in lens galaxies: first constraints on the mass function

Simona Vegetti (MIT)

Gravitational detection of a low-mass dark satellite galaxy at cosmological distance, 2012 Nature

Talk at KITP conference "First Light and Faintest Dwarfs"

How do we recognise the effect of substructure?



Extended galaxy

Substructure as a truncated pseudo Jaffe

$$M_{sub} = (1.9 \pm 0.1) \times 10^8 M_{\odot}$$

$$M(< 0.6) = (1.15 \pm 0.06) \times 10^8 M_{\odot}$$

$$M(< 0.3) = (7.24 \pm 0.6) \times 10^7 M_{\odot}$$

Substructure as SIS

$$M(< 0.3) = 3.4 \times 10^7 M_{\odot}$$

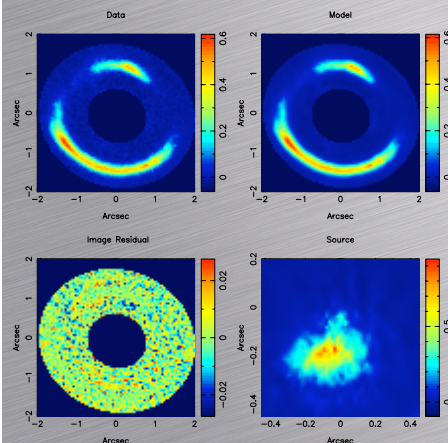
$$\sigma_v \approx 16 \text{ km s}^{-1}$$

$$V_{max} \approx 27 \text{ km s}^{-1}$$

$$\Delta \log E = 65.0 \quad 12 \sigma \text{ detection}$$

J0946+1066 - Double ring

Power-Law smooth model + Power-Law substructure



$$M_{sub} = (3.51 \pm 0.15) \times 10^9 M_{\odot}$$

$$r_t = 1.1 \text{ kpc}$$

$$\Delta \log \mathcal{E} = -128.0$$

equivalent to a $\sim 16\sigma$ detection

$$M_{3D}(< 0.3) = 5.83 \times 10^8 M_{\odot}$$

Conclusions

- Surface brightness anomalies can be used to find low mass galaxies at high z
- Simulations show that with HST quality data, 10 systems are sufficient to constrain the mass function
- Using high resolution adaptive optics data and the gravitational imaging technique we discovered an analogue of the Fornax satellite at redshift about 1
- The first constraints on the mass function are consistent with prediction from CDM (large errors)

Our results are consistent with the predictions from cold dark matter simulations at the 95 per cent confidence level, and therefore agree with the view that galaxies formed hierarchically in a Universe composed of cold dark matter. Vegetti et al. 2012 Nature 481, 341.

CLUMPY STREAMS FROM CLUMPY HALOS: DETECTING MISSING SATELLITES WITH COLD STELLAR STRUCTURES

JOO HEON YOON^{1*}, KATHRYN V. JOHNSTON¹, AND DAVID W. HOGG²

ApJ Accepted

2011 ApJ 731, 58

Dynamically cold stellar streams are ideal probes of the gravitational field of the Milky Way. This paper re-examines the question of how such streams might be used to test for the presence of “missing satellites” — the many thousands of dark-matter subhalos with masses $10^5 - 10^7 M_\odot$ which are seen to orbit within Galactic-scale dark-matter halos in simulations of structure formation in Λ CDM cosmologies. Analytical estimates of the frequency and energy scales of stream encounters indicate that these missing satellites should have a negligible effect on hot debris structures, such as the tails from the Sagittarius dwarf galaxy. However, long cold streams, such as the structure known as GD-1 or those from the globular cluster Palomar 5 (Pal 5) are expected to suffer many tens of direct impacts from missing satellites during their lifetimes. Numerical experiments confirm that these impacts create gaps in the debris’ orbital energy distribution, which will evolve into degree- and sub-degree-scale fluctuations in surface density over the age of the debris. Maps of Pal 5’s own stream contain surface density fluctuations on these scales. The presence and frequency of these inhomogeneities suggests the existence of a population of missing satellites in numbers predicted in the standard Λ CDM cosmologies.

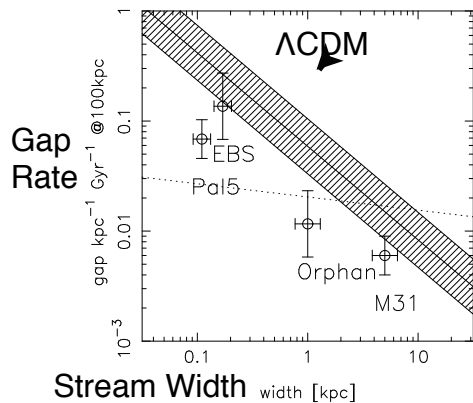


FIG. 11.— The estimated gap rate vs stream width relation for M31 NW, Pal 5, the EBS and the CDM halo prediction. All data have been normalized to 100 kpc. The width of the theoretical relation is evaluated from the dispersion in the length-height relation of Fig. 8. Predictions for an arbitrary alternative mass functions, $N(M) \propto M^{-1.6}$ normalized to have 33 halos above $10^9 M_\odot$ is shown with a dotted line.

DARK MATTER SUB-HALO COUNTS VIA STAR STREAM CROSSINGS

R. G. CARLBERG¹

arXiv:1201.1347

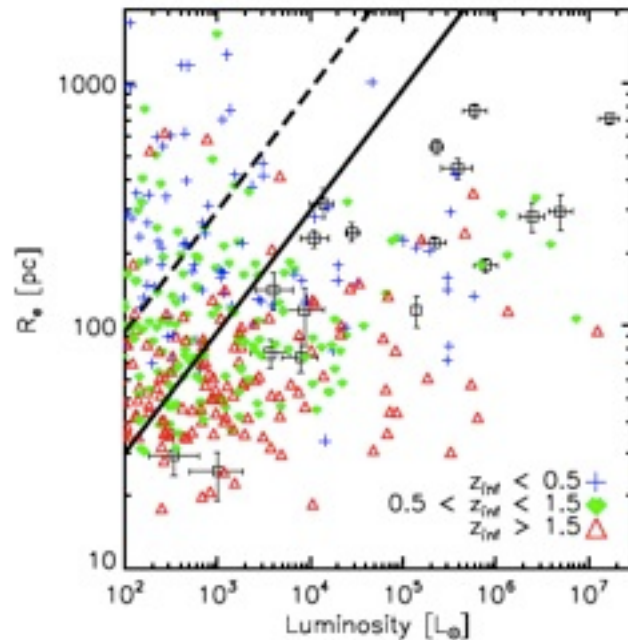
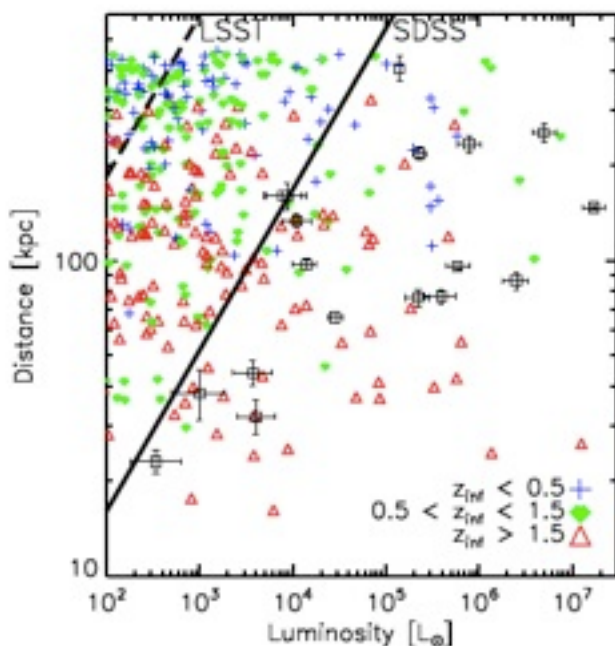
Comparison of the CDM based prediction of the gap rate-width relation with published data for four streams shows generally good agreement within the fairly large measurement errors. **The result is a statistical argument that the vast predicted population of sub-halos is indeed present in the halos of galaxies like M31 and the Milky Way.** The data do tend to be somewhat below the prediction at most points. This could be the result of many factors, such as the total population of sub-halos is expected to vary significantly from galaxy to galaxy, allowing for the stream age would lower the predicted number of gaps for the Orphan stream and possibly others as well, and most importantly these are idealized stream models.

Λ CDM predicts that there is a population of low-luminosity stealth galaxies around the Milky Way. 2010 ApJ

STEALTH GALAXIES IN THE HALO OF THE MILKY WAY

James S. Bullock, Kyle R. Stewart, Manoj Kaplinghat, and Erik J. Tollerud

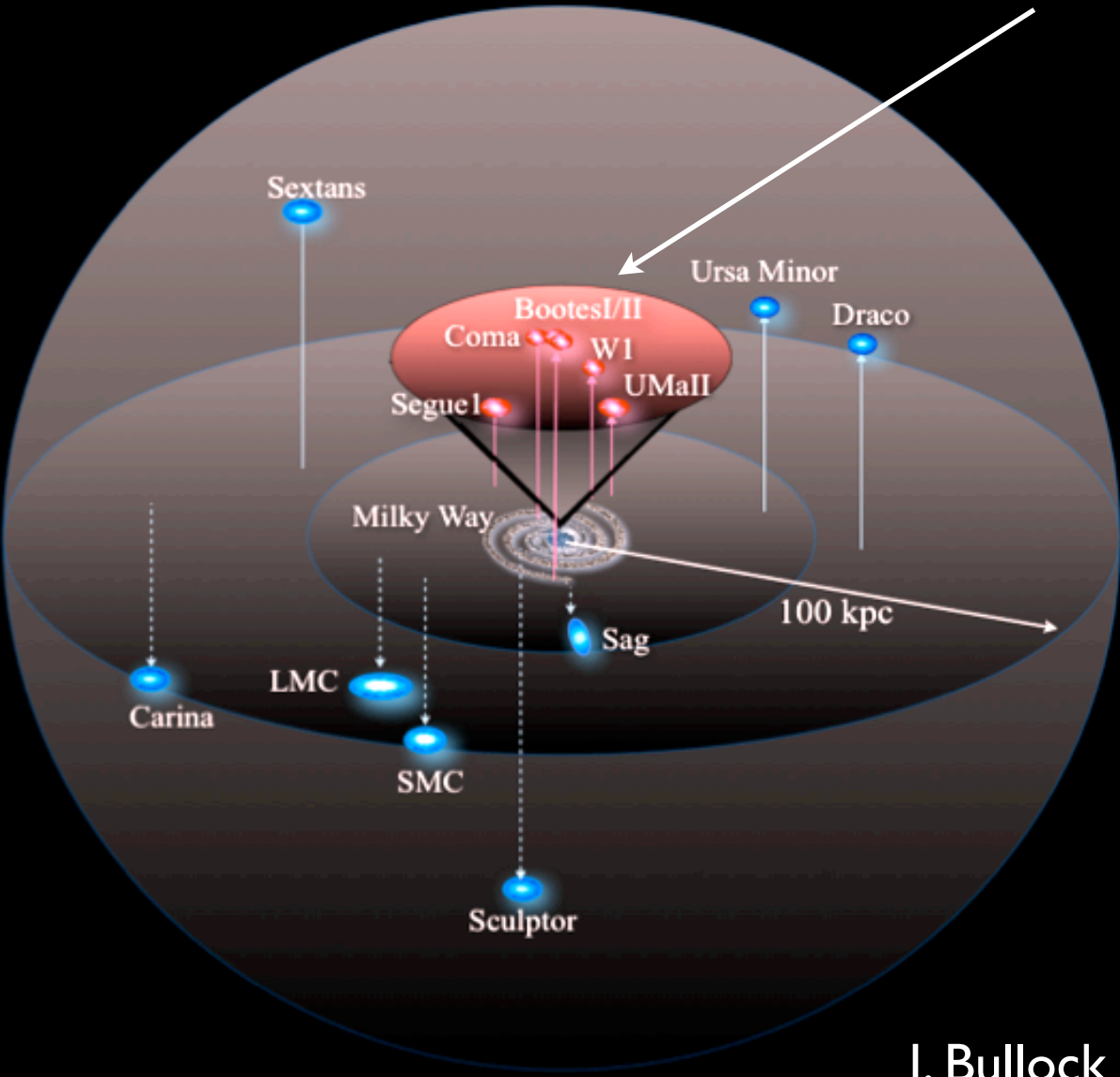
We predict that there is a population of low-luminosity dwarf galaxies with luminosities and stellar velocity dispersions that are similar to those of known ultrafaint dwarf galaxies but they have more extended stellar distributions (half light radii greater than about 100 pc) because they inhabit dark subhalos that are slightly less massive than their higher surface brightness counterparts. One implication is that the inferred common mass scale for Milky Way dwarfs may be an artifact of selection bias. A complete census of these objects will require deeper sky surveys, 30m-class follow-up telescopes, and more refined methods to identify extended, self-bound groupings of stars in the halo.



Satellite
Infall
redshift

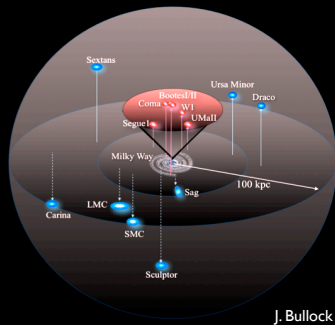
$z_{\text{inf}} < 0.5$ +
 $0.5 < z_{\text{inf}} < 1.5$ ◆
 $z_{\text{inf}} > 1.5$ ▲

SDSS satellite search



J. Bullock

The search for faint Milky Way satellites has just begun



The Dark Energy Survey will cover a larger region of the Southern Sky, and LSST will go much deeper yet

Conclusions

- CMB and large-scale structure predictions of Λ CDM with WMAP5/7 cosmological parameters are in excellent agreement with observations. There are no known discrepancies.
- On galaxy and smaller scales, many of the supposed former challenges to Λ CDM are now at least partially resolved. The “angular momentum catastrophe” in galaxy formation appears to be resolved with better resolution and more realistic feedback. Cusps can be removed by starbursts blowing out central gas.
- Lensing flux anomalies and gaps in cold stellar streams appear to require the sort of substructure seen in Λ CDM simulations. However, the biggest subhalos in Λ CDM MWy-type dark matter halos do not host observed satellites. This “too big to fail” problem appears to be the most serious current challenge for Λ CDM, and may indicate the need for a more complex theory of dark matter -- or perhaps just better understanding of DM simulations and/or of baryonic physics.

Student Presentations - Thursday June 7

Andrew Marsh:

The Lithium Problem: A Cosmological Conundrum

Srikar Srinath:

The role of Adaptive Optics in resolving the nuclei of merging galaxies at redshifts of 1 or greater and how that is lending support to hierarchical clustering models

Emma Storm:

Indirect Detection of Dark Matter: Effects of Substructure in Galaxy Clusters and Dwarf Galaxies