

Physics/Astronomy 224 Spring 2012

Origin and Evolution of the Universe

Week 2 - Part 2

Big Bang Nucleosynthesis

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As the temperature of the universe cools to 1 MeV, the cosmic plasma consists of:

- **Relativistic particles in equilibrium: photons, electrons and positrons.** These are kept in close contact with each other by electromagnetic interactions such as $e^+e^- \leftrightarrow \gamma\gamma$. Besides a small difference due to fermion/boson statistics, these all have the same abundances.
- **Decoupled relativistic particles: neutrinos.** At temperatures a little above 1 MeV, the rate for processes such as $\nu e \leftrightarrow \nu e$ which keep neutrinos coupled to the rest of the plasma drops beneath the expansion rate. Neutrinos therefore share the same temperature as the other relativistic particles, and hence are roughly as abundant, but they do not couple to them.
- **Nonrelativistic particles: baryons.** If there had been no asymmetry in the initial number of baryons and anti-baryons, then both would be completely depleted by 1 MeV. However, such an asymmetry did exist: $(n_b - n_{\bar{b}})/s \sim 10^{-10}$ initially,¹ and this ratio remains constant throughout the expansion. By the time the temperature is of order 1 MeV, all anti-baryons have annihilated away (Exercise 12) so

$$\eta_b \equiv \frac{n_b}{n_\gamma} = 5.5 \times 10^{-10} \left(\frac{\Omega_b h^2}{0.020} \right). \quad (3.11)$$

There are thus many fewer baryons than relativistic particles when $T \sim \text{MeV}$.

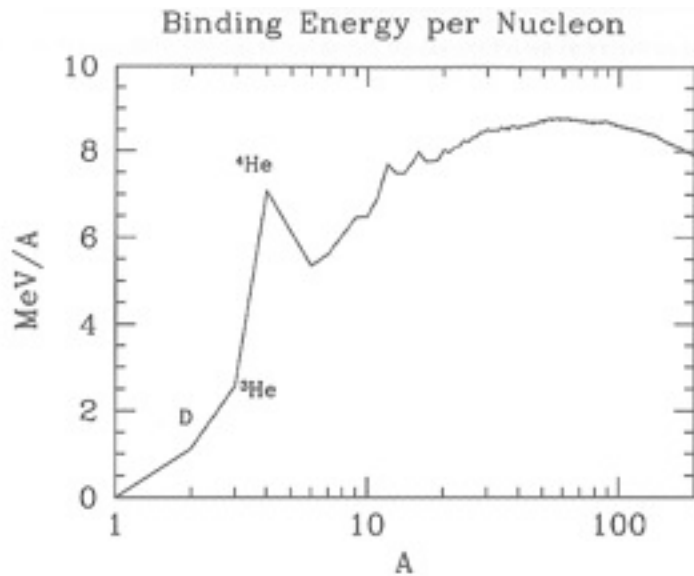


Figure 3.1. Binding energy of nuclei as a function of mass number. Iron has the highest binding energy, but among the light elements, ${}^4\text{He}$ is a crucial local maximum. Nucleosynthesis in the early universe essentially stops at ${}^4\text{He}$ because of the lack of tightly bound isotopes at $A = 5 - 8$. In the high-density environment of stars, three ${}^4\text{He}$ nuclei fuse to form ${}^{12}\text{C}$, but the low baryon number precludes this process in the early universe.

Lightning Introduction to Nuclear Physics

A single proton is a hydrogen nucleus, referred to as ${}^1\text{H}$ or simply p ; a proton and a neutron make up deuterium, ${}^2\text{H}$ or D ; one proton and two neutrons make tritium, ${}^3\text{H}$ or T . Nuclei with two protons are helium; these can have one neutron (${}^3\text{He}$) or two (${}^4\text{He}$). Thus unique elements have a fixed number of protons, and isotopes of a given element have differing numbers of neutrons. The total number of neutrons and protons in the nucleus, the *atomic number*, is a superscript before the name of the element.

The total mass of a nucleus with Z protons and $A - Z$ neutrons differs slightly from the mass of the individual protons and neutrons alone. This difference is called the binding energy, defined as

$$B \equiv Zm_p + (A - Z)m_n - m \quad (3.12)$$

where m is the mass of the nucleus. For example, the mass of deuterium is 1875.62 MeV while the sum of the neutron and proton masses is 1877.84 MeV, so the binding energy of deuterium is 2.22 MeV. Nuclear binding energies are typically in the MeV range, which explains why Big Bang nucleosynthesis occurs at temperatures a bit less than 1 MeV even though nuclear masses are in the GeV range.

Neutrons and protons can interconvert via weak interactions:



where all the reactions can proceed in either direction. The light elements are built up via electromagnetic interactions. For example, deuterium forms from $p + n \rightarrow \text{D} + \gamma$. Then, $\text{D} + \text{D} \rightarrow n + {}^3\text{He}$, after which ${}^3\text{He} + \text{D} \rightarrow p + {}^4\text{He}$ produces ${}^4\text{He}$.

$$\frac{n_D}{n_n n_p} = \frac{n_D^{(0)}}{n_n^{(0)} n_p^{(0)}}. \quad (3.14)$$

The integrals on the right, as given in Eq. (3.6), lead to

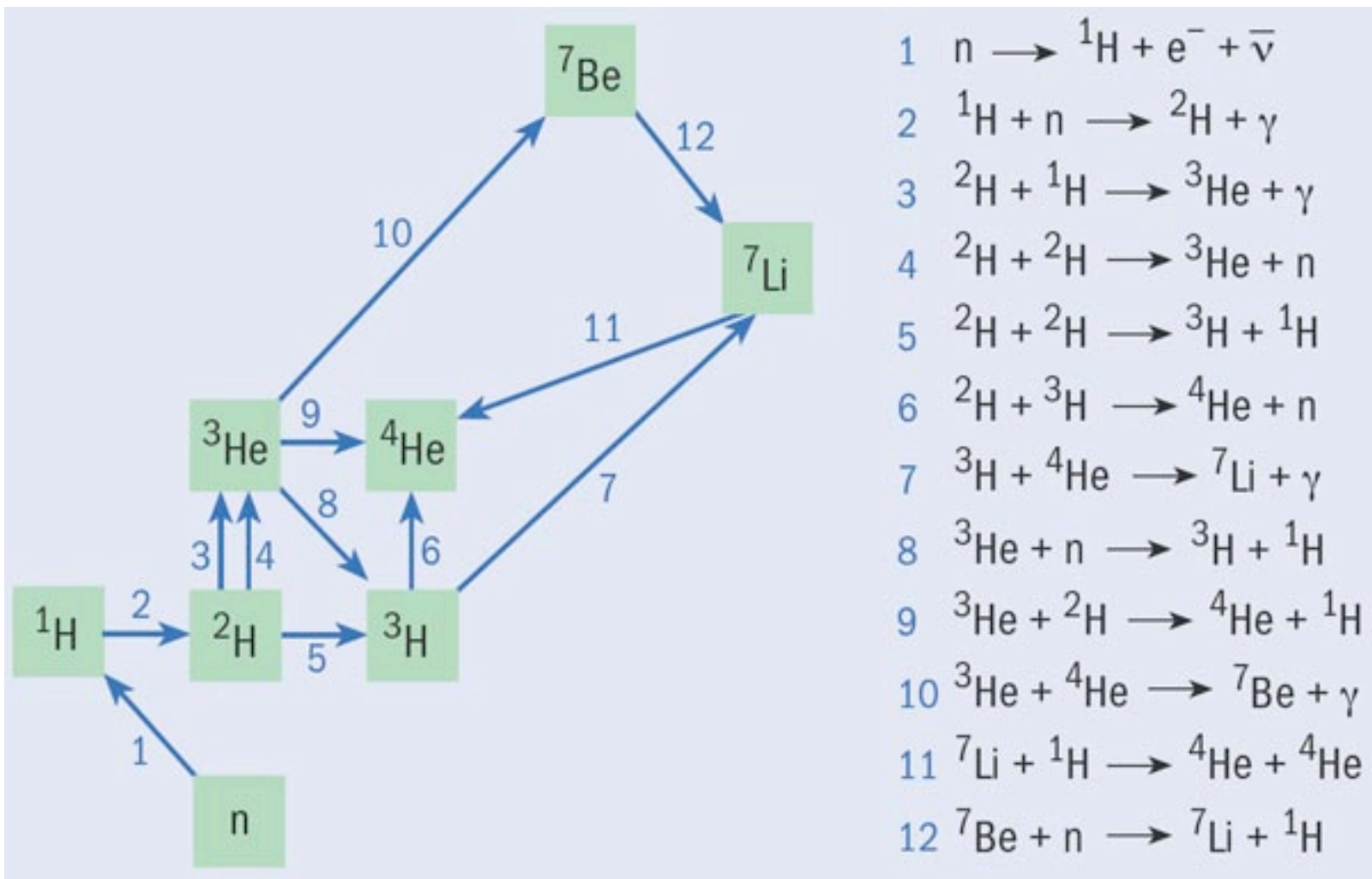
$$\frac{n_D}{n_n n_p} = \frac{3}{4} \left(\frac{2\pi m_D}{m_n m_p T} \right)^{3/2} e^{[m_n + m_p - m_D]/T}, \quad (3.15)$$

the factor of 3/4 being due to the number of spin states (3 for D and 2 each for p and n). In the prefactor, m_D can be set to $2m_n = 2m_p$, but in the exponential the small difference between $m_n + m_p$ and m_D is important: indeed the argument of the exponential is by definition equal to the binding energy of deuterium, $B_D = 2.22$ MeV. Therefore, as long as equilibrium holds,

$$\frac{n_D}{n_n n_p} = \frac{3}{4} \left(\frac{4\pi}{m_p T} \right)^{3/2} e^{B_D/T}. \quad (3.16)$$

Both the neutron and proton density are proportional to the baryon density, so roughly,

$$\frac{n_D}{n_b} \sim \eta_b \left(\frac{T}{m_p} \right)^{3/2} e^{B_D/T}. \quad (3.17)$$



Deuterium nuclei (${}^2\text{H}$) were produced by collisions between protons and neutrons, and further nuclear collisions led to every neutron grabbing a proton to form the most tightly bound type of light nucleus: ${}^4\text{He}$. This process was complete after about five minutes, when the universe became too cold for nuclear reactions to continue. Tiny amounts of deuterium, ${}^3\text{He}$, ${}^7\text{Li}$, and ${}^7\text{Be}$ were produced as by-products, with the ${}^7\text{Be}$ undergoing beta decay to form ${}^7\text{Li}$. Almost all of the protons that were not incorporated into ${}^4\text{He}$ nuclei remained as free particles, and this is why the universe is close to 25% ${}^4\text{He}$ and 75% H by mass. The other nuclei are less abundant by several orders of magnitude.

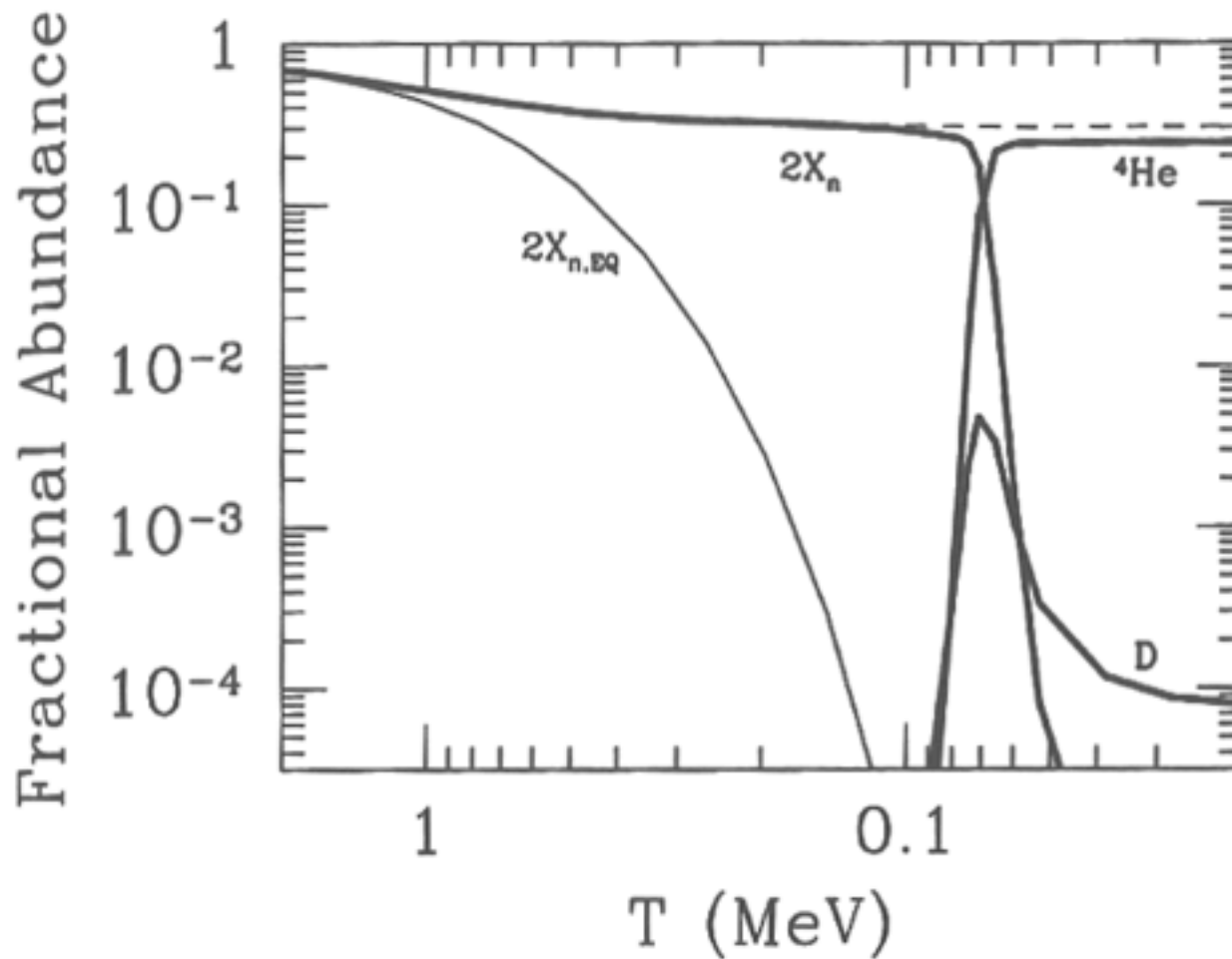
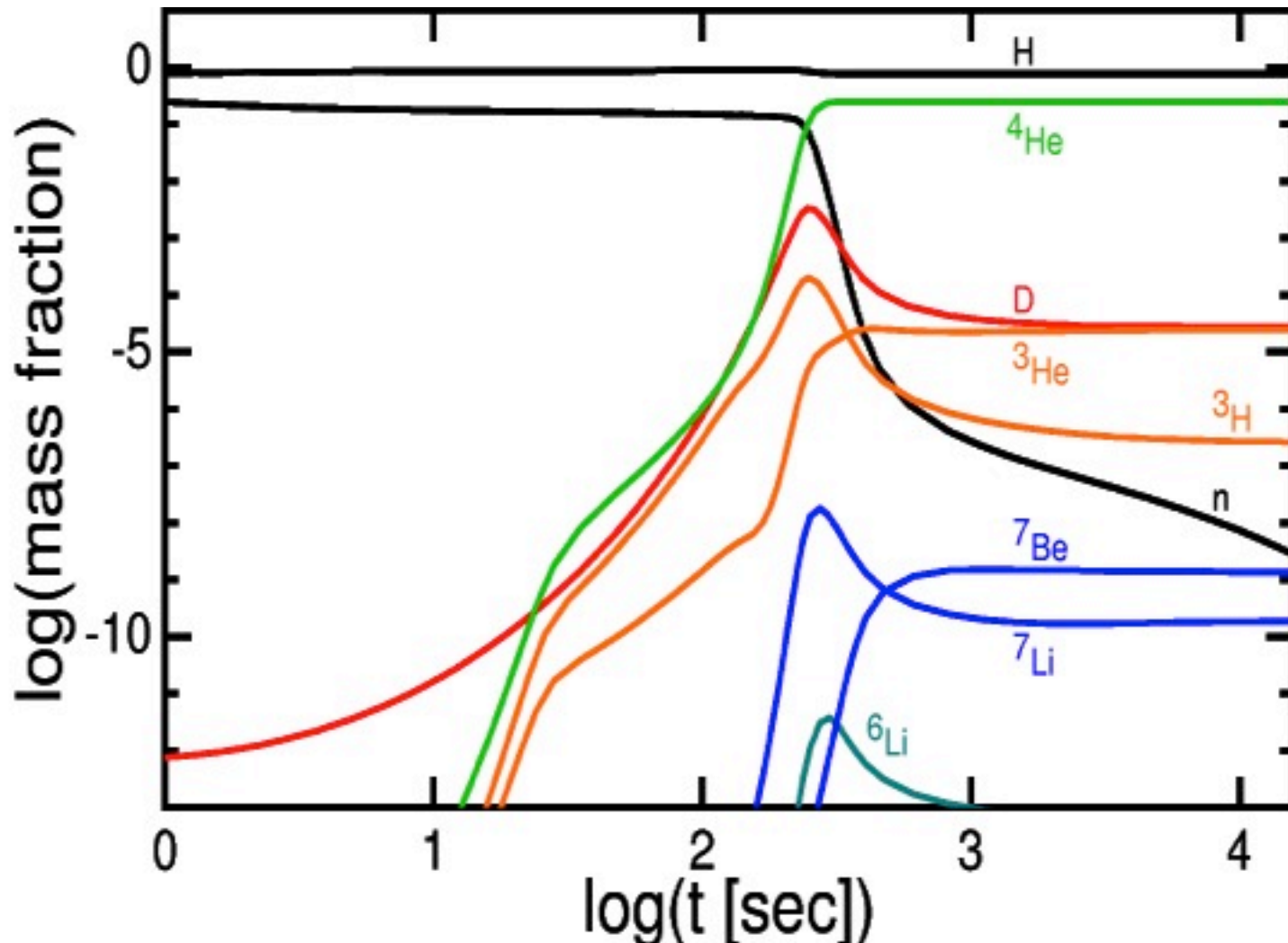


Figure 3.2. Evolution of light element abundances in the early universe. Heavy solid curves are results from Wagoner (1973) code; dashed curve is from integration of Eq. (3.27); light solid curve is twice the neutron equilibrium abundance. Note the good agreement of Eq. (3.27) and the exact result until the onset of neutron decay. Also note that the neutron abundance falls out of equilibrium at $T \sim \text{MeV}$.

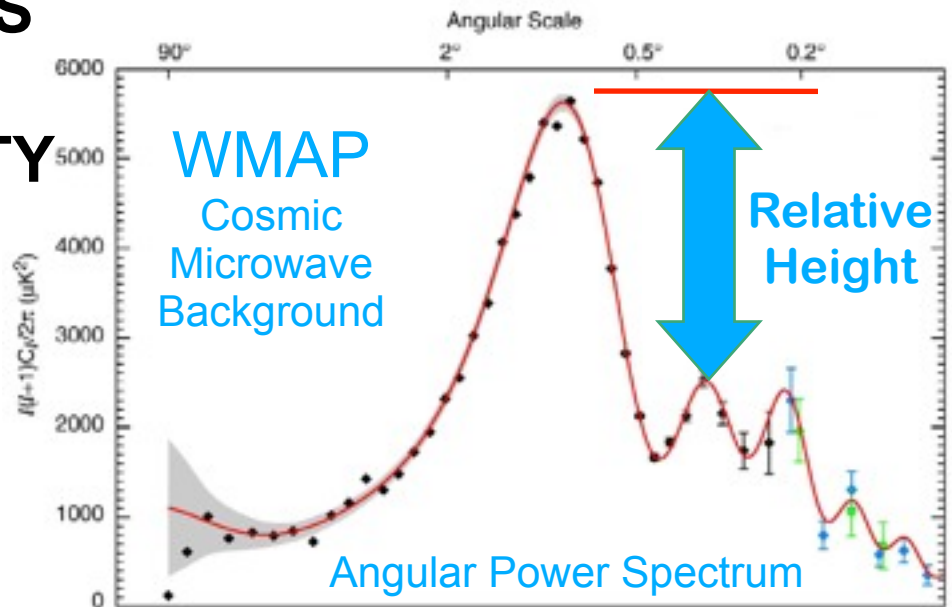
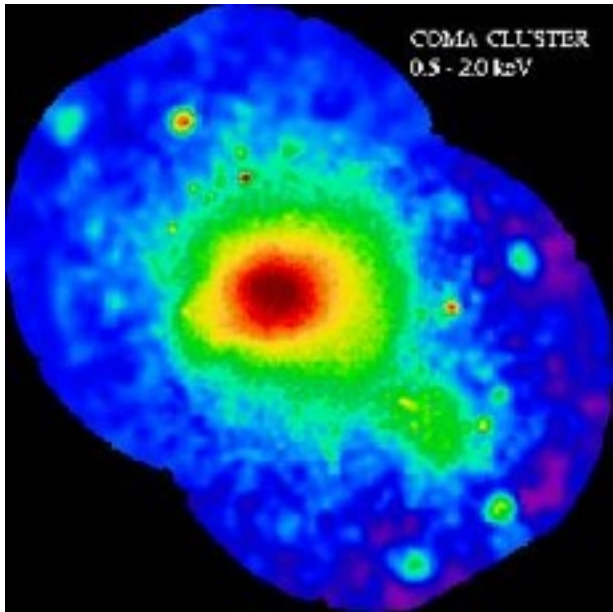


The detailed production of the lightest elements out of protons and neutrons during the first three minutes of the universe's history. The nuclear reactions occur rapidly when the temperature falls below a billion degrees Kelvin. Subsequently, the reactions are shut down, because of the rapidly falling temperature and density of matter in the expanding universe.

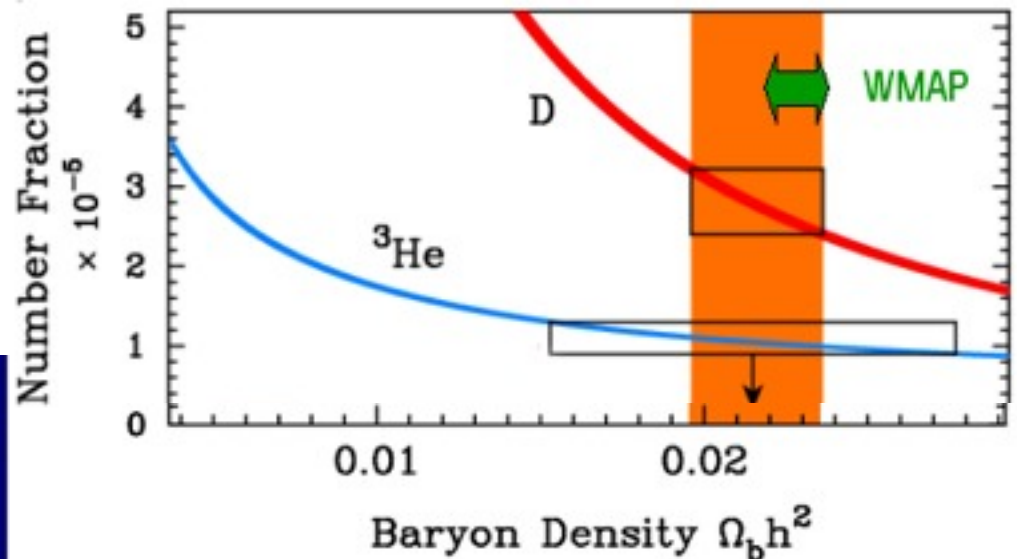
Ken Kawano's (1992) BBN code is available at <http://www-thphys.physics.ox.ac.uk/users/SubirSarkar/bbn.html>

5 INDEPENDENT MEASURES AGREE: ATOMS ARE ONLY 4% OF THE COSMIC DENSITY

Galaxy Cluster in X-rays

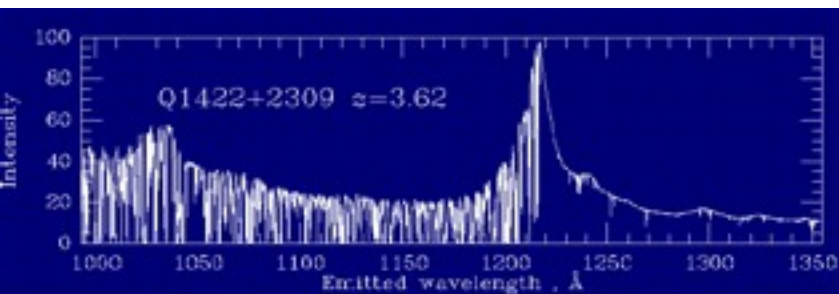


Deuterium Abundance
+ Big Bang Nucleosynthesis



& WIGGLES IN GALAXY $P(k)$

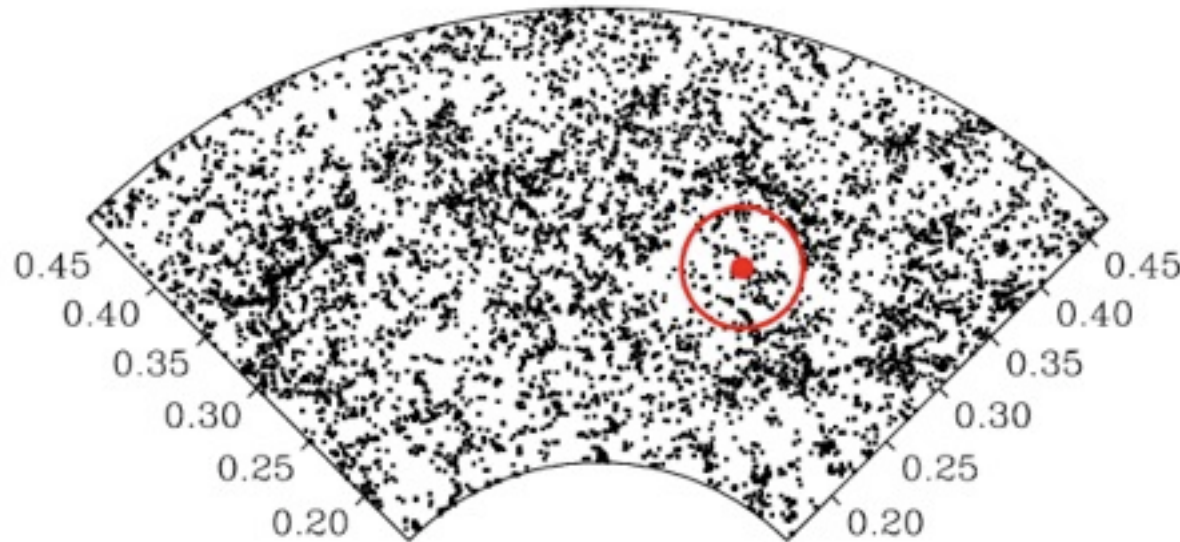
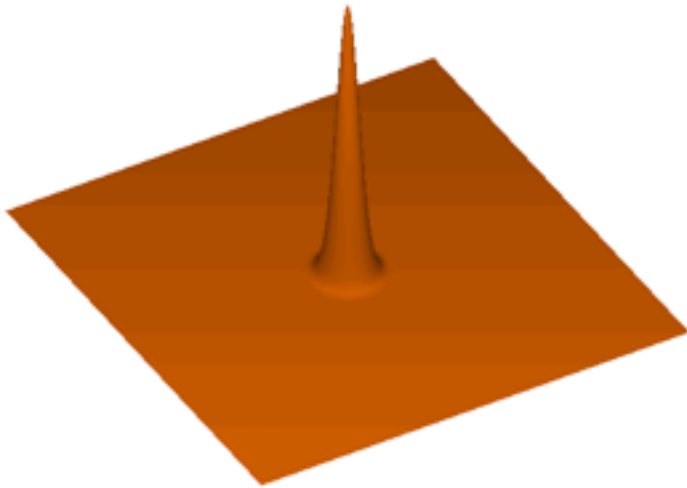
Absorption of Quasar Light



BAO WIGGLES IN GALAXY P(k)

Sound waves that propagate in the opaque early universe imprint a characteristic scale in the clustering of matter, providing a “standard ruler” whose length can be computed using straightforward physics and parameters that are tightly constrained by CMB observations. Measuring the angle subtended by this scale determines a distance to that redshift and constrains the expansion rate.

The detection of the acoustic oscillation scale is one of the key accomplishments of the SDSS, and even this moderate signal-to-noise measurement substantially tightens constraints on cosmological parameters. Observing the evolution of the BAO standard ruler provides one of the best ways to measure whether the dark energy parameters changed in the past.



M. White lectures 08

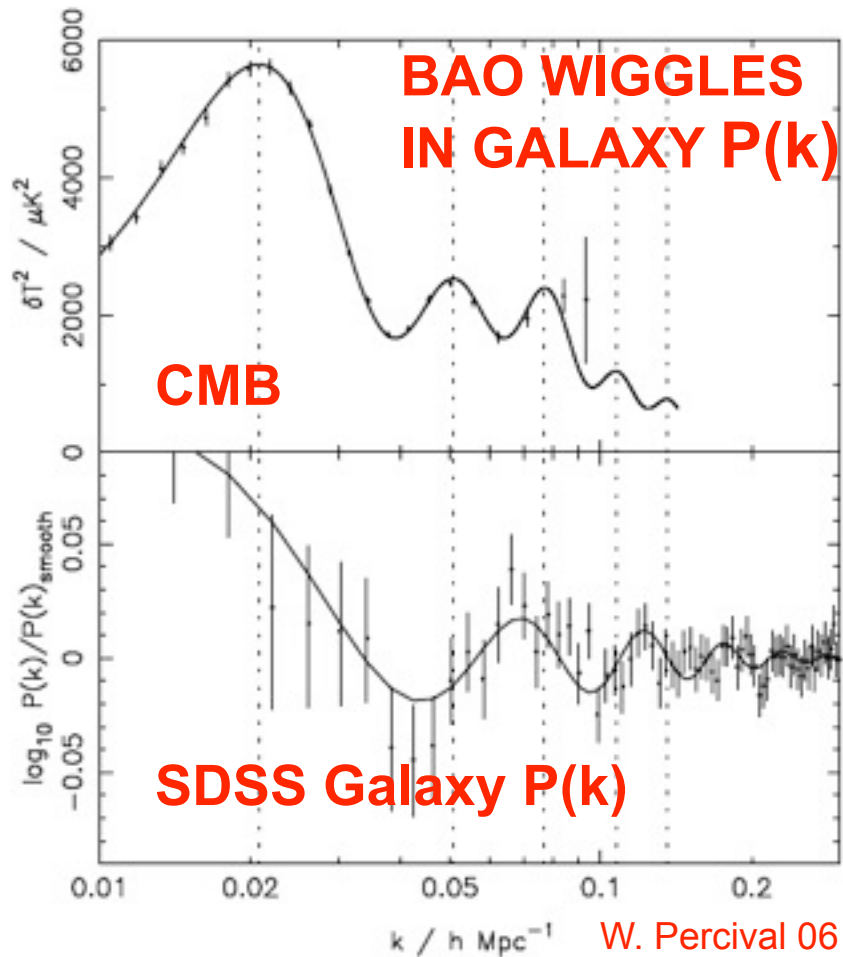
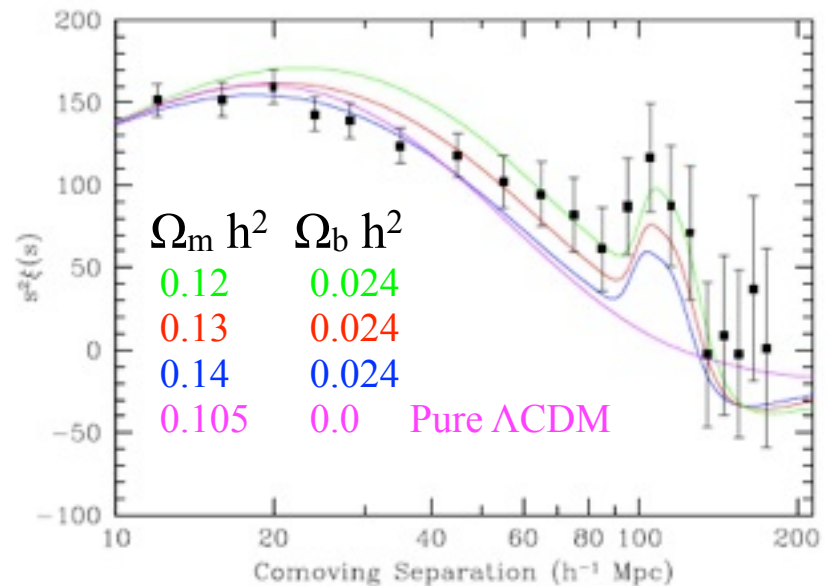
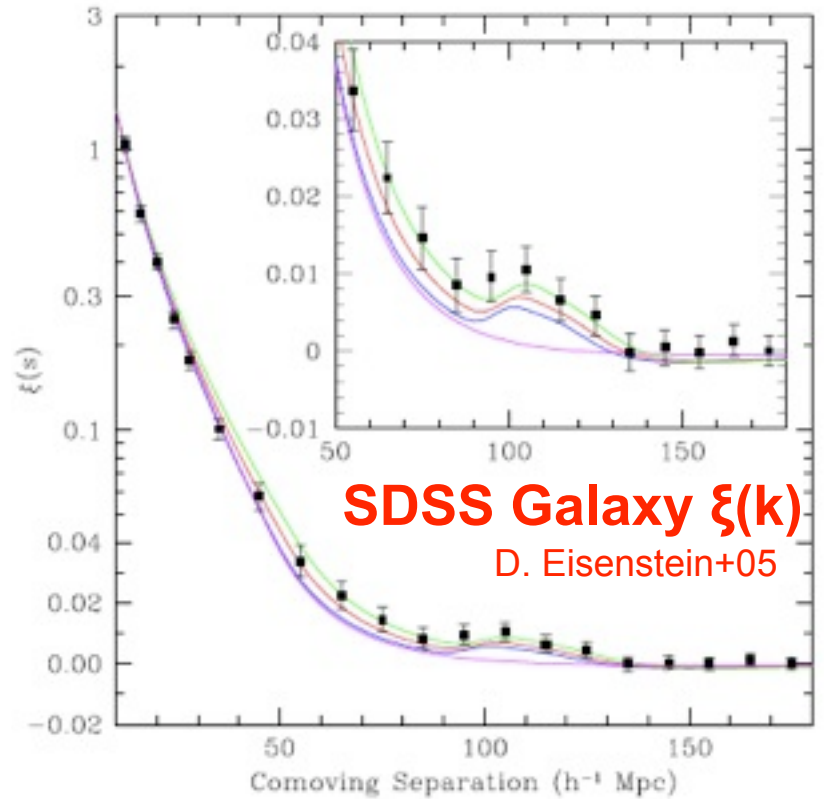
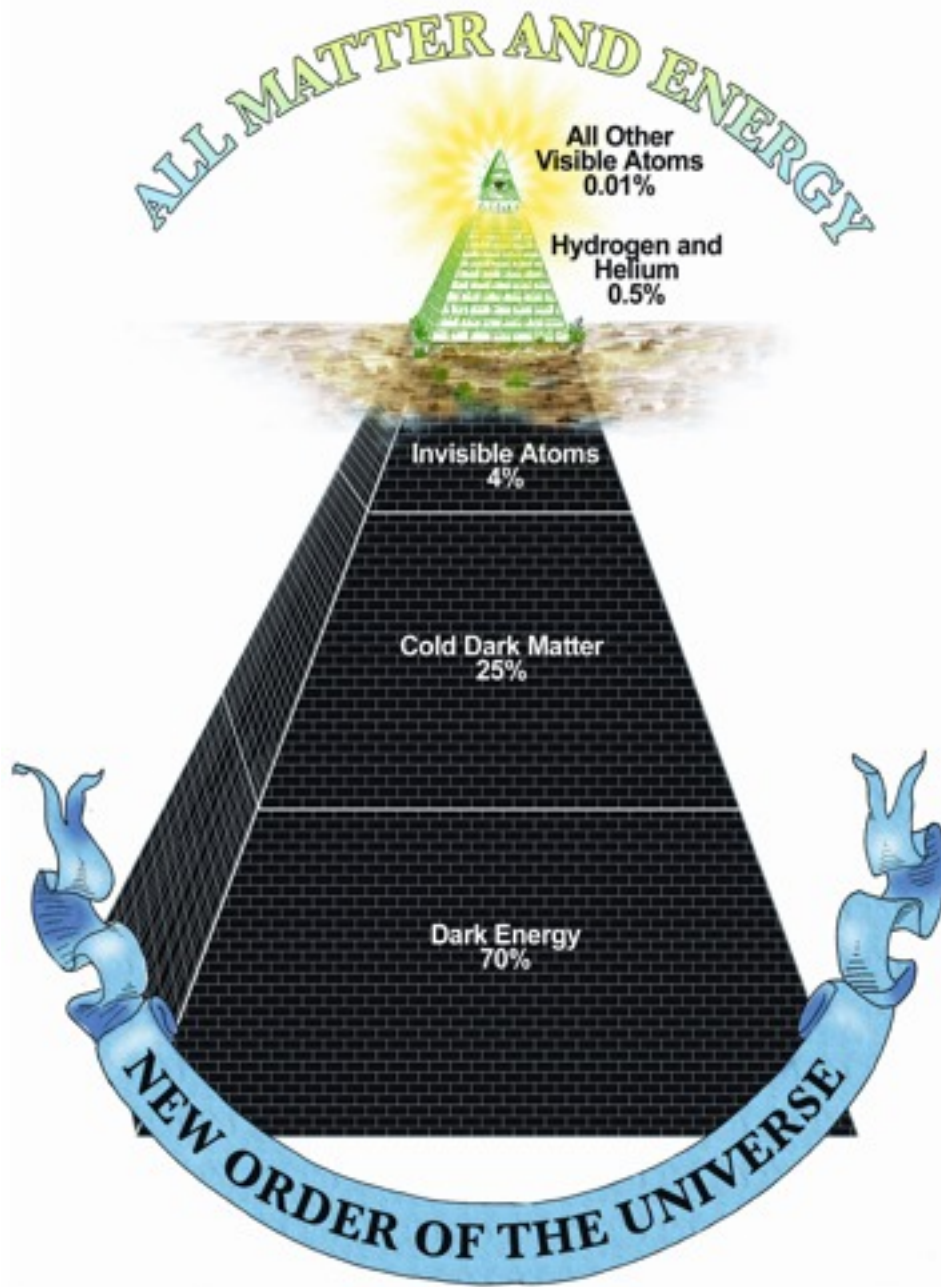


Fig. 3. Upper panel: The TT power spectrum recovered from the 3-year WMAP data (Hinshaw et al. 2006), projected into comoving space assuming a cosmological model with $\Omega_m = 0.25$ and $\Omega_V = 0.75$. For comparison, in the lower panel we plot the baryon oscillations calculated by dividing the SDSS power spectrum with a smooth cubic spline fit (Percival et al. 2007a). Vertical dotted lines show the positions of the peaks in the CMB power spectrum. As can be seen, there is still a long way to go before low redshift observations can rival the CMB in terms of the significance of the acoustic oscillation signal.





Periodic Table of the Elements

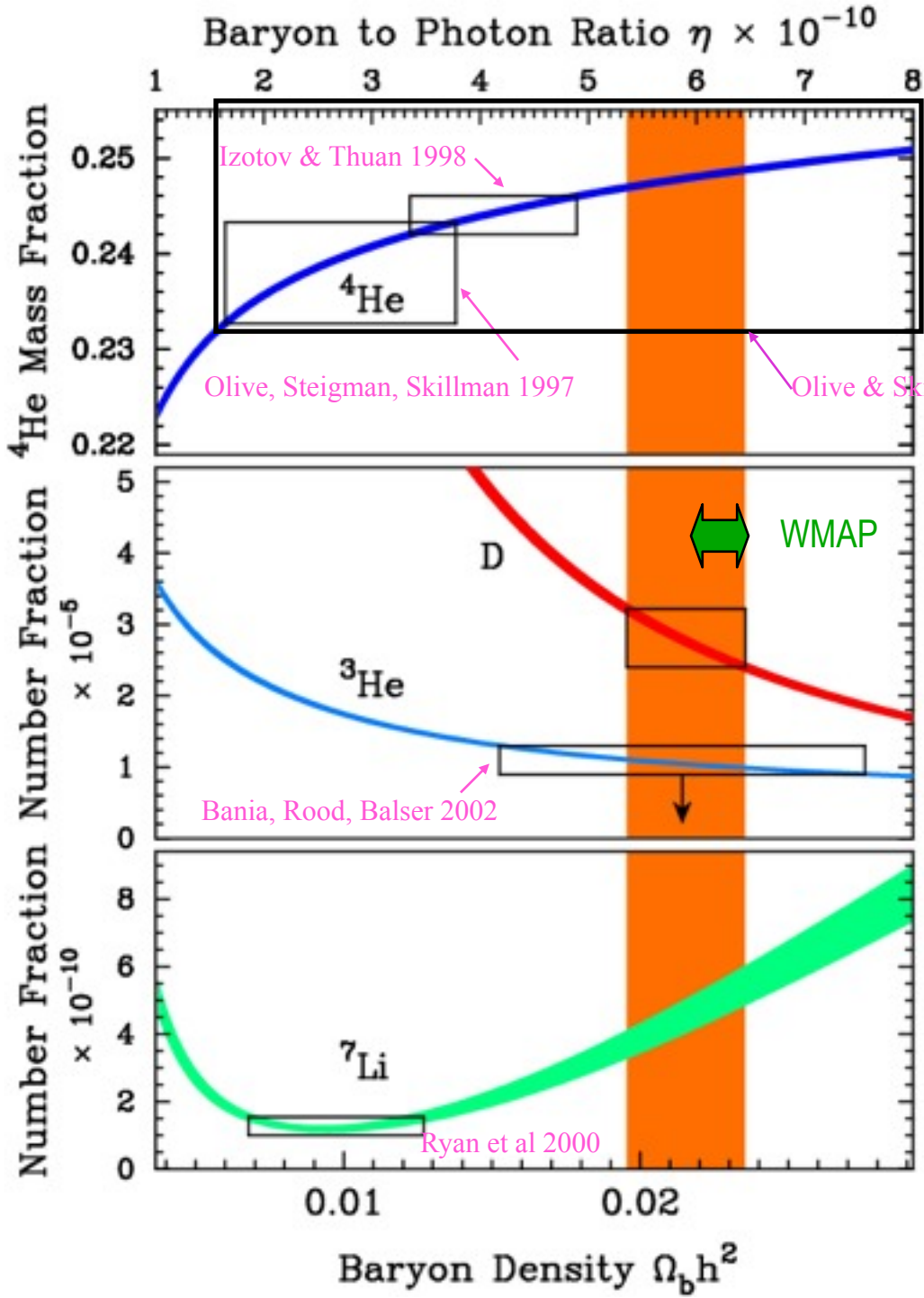
H																	He
Li	Be											B	C	N	O	F	Ne
Na	Mg											Al	Si	P	S	Cl	Ar
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe
Cs	Ba	La	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn
Fr	Ra	Ac	Rf	Db	Sg	Bh	Hs	Mt	Ds	Rg	Cn						
		Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu		
		Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr		

Light blue - Big Bang
 Pink - Small Stars
 Purple - Supernovae
 Green - Cosmic Rays
 Blue - Large Stars
 Dull gray - Made in Lab



BBN
 Predicted
 vs.
 Measured
 Abundance
 s of D, ^3He ,
 ^4He , and ^7Li

^7Li IS NOW
 DISCORDANT
 unless stellar
 diffusion
 destroys ^7Li



Izotov & Thuan 2004:
 $\Omega_b h^2 = 0.012 \pm 0.0025$

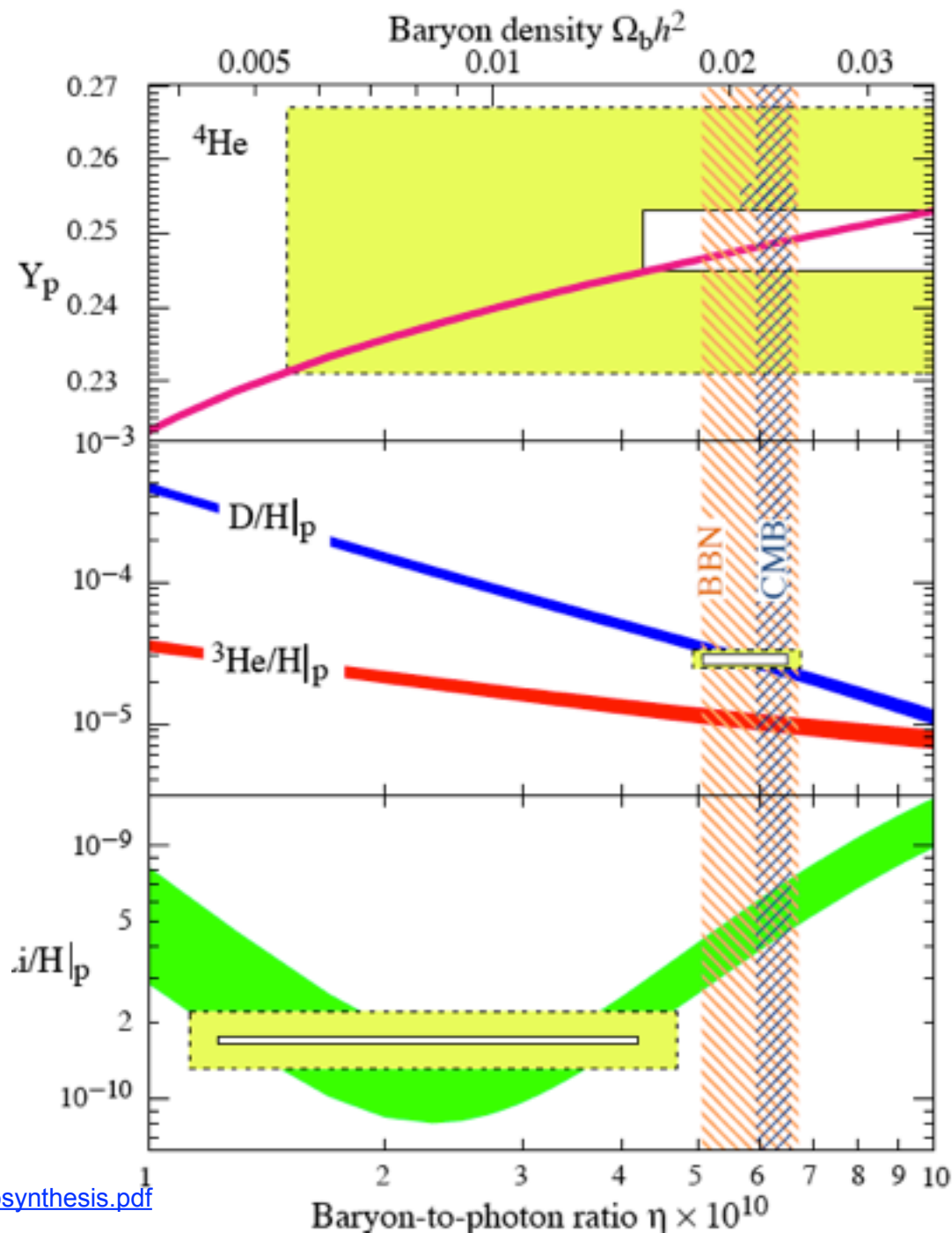
WMAP (Spergel et al. 2003) says that
 $\Omega_b h^2 = 0.0224 \pm 0.0009$
 (with their running spectral index model)

BBN predictions are from Burles, Nollett, & Turner 2001

D/H is from Kirkman, Tytler, Suzuki, O'Meara, & Lubin 2004, giving
 $\Omega_b h^2 = 0.0214 \pm 0.0020$

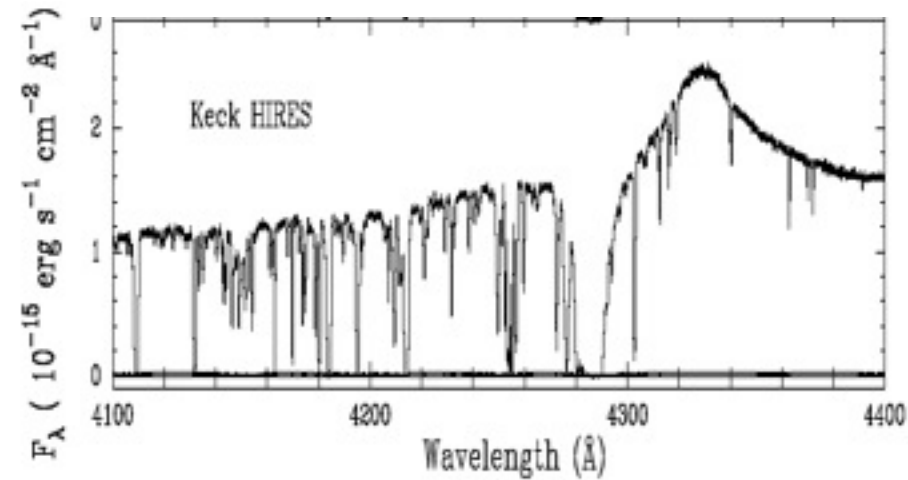
The abundances of ^4He , D, ^3He , and ^7Li as predicted by the standard model of Big-Bang nucleosynthesis – the bands show the 95% CL range. Boxes indicate the observed light element abundances (smaller boxes: $\pm 2\sigma$ statistical errors; larger boxes: $\pm 2\sigma$ statistical *and* systematic errors). The narrow vertical band indicates the CMB measure of the cosmic baryon density, while the wider band indicates the BBN concordance range (both at 95% CL).

Particle Data Group 20. BBN by B. D. Fields and S. Sarker 2009



<http://pdg.lbl.gov/2010/reviews/rpp2010-rev-bbang-nucleosynthesis.pdf>

Deuterium absorption at redshift 2.525659 towards Q1243+3047



The detection of Deuterium and the modeling of this system seem convincing. This is just a portion of the evidence that the Tytler group presented in this paper. They have similarly convincing evidence for several other Lyman alpha clouds in quasar spectra.

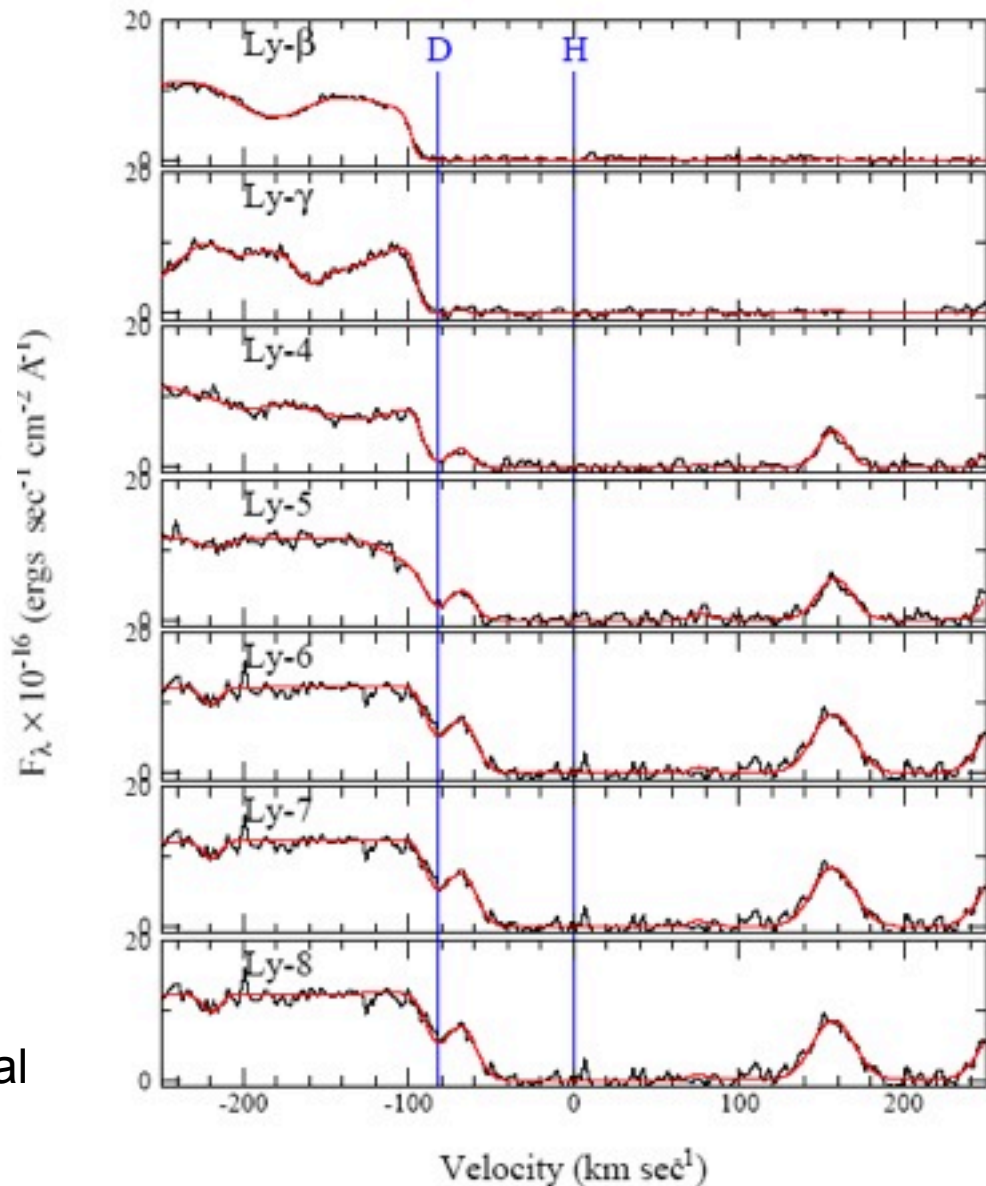
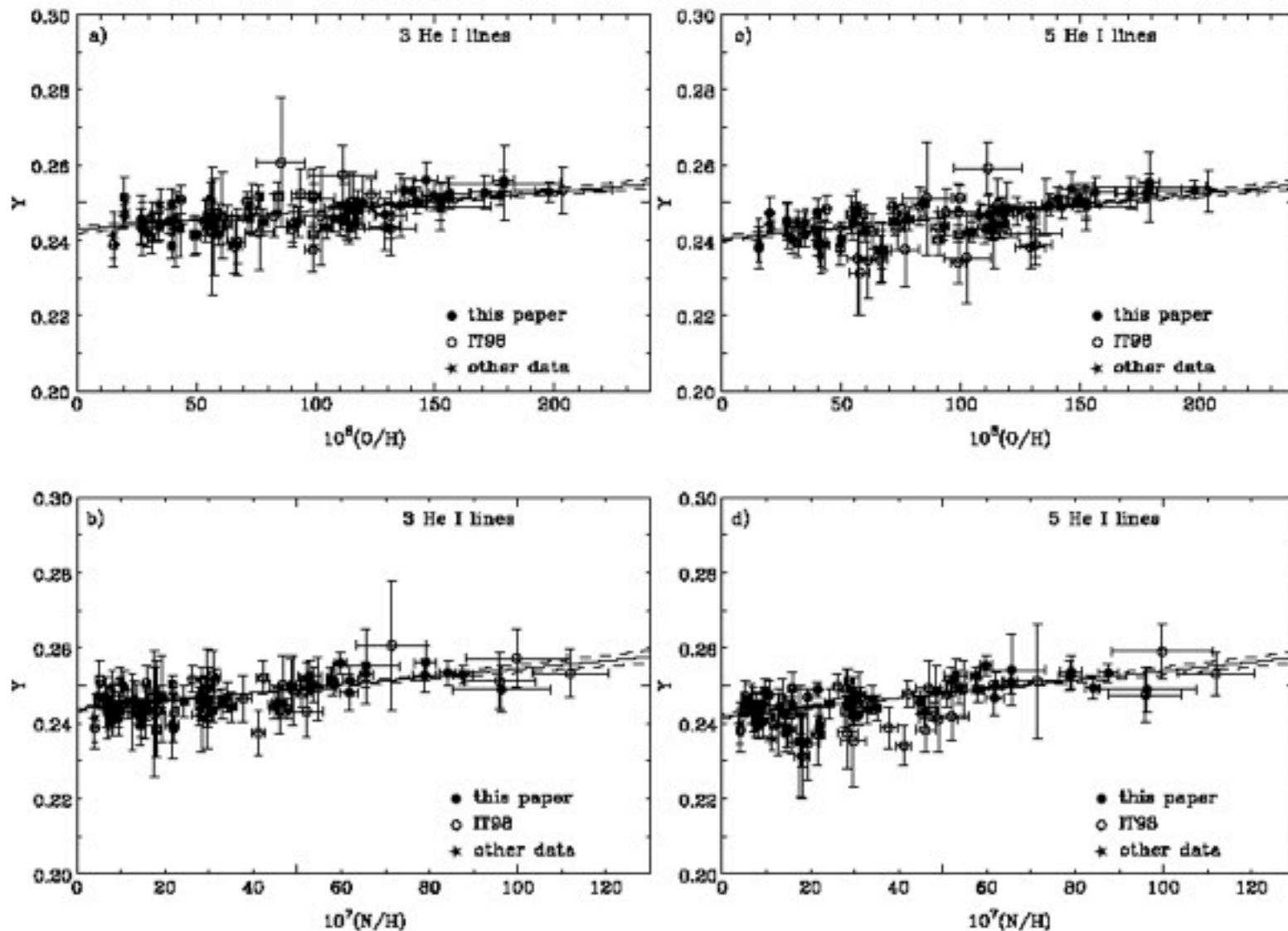


FIG. 7.— The HIRES spectrum of Ly-2 to 8, together with our model of the system, as given in Table 3.

Kirkman, Tytler, Suzuki, O'Meara, & Lubin 2004

Determination of primordial He^4 abundance Y_p by linear regression



$Y = M(^4\text{He})/M(\text{baryons})$, Primordial $Y \equiv Y_p = \text{zero intercept}$

Note: BBN plus $\text{D}/\text{H} \Rightarrow Y_p = 0.247 \pm 0.001$

Izotov & Thuan 2004

The Li abundance disagreement with BBN may indicate new physics

Did Something Decay, Evaporate, or Annihilate during Big Bang Nucleosynthesis?

Karsten Jedamzik [Phys.Rev. D70 \(2004\) 063524](#)

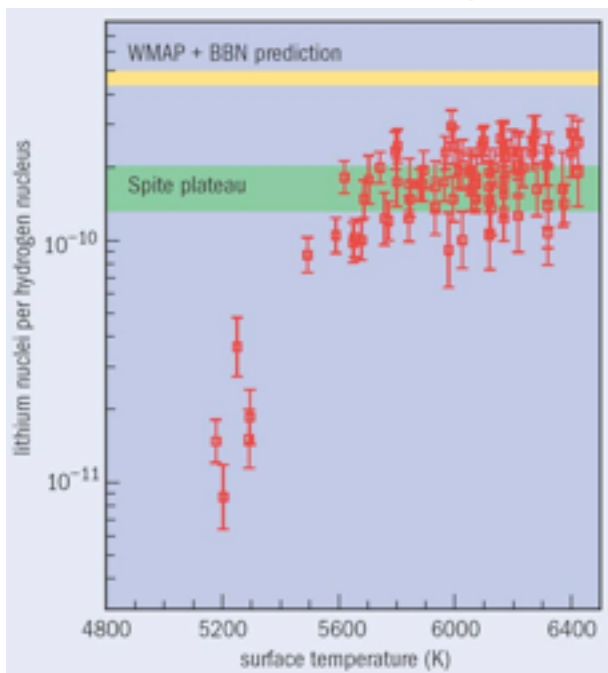
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Results of a detailed examination of the cascade nucleosynthesis resulting from the putative hadronic decay, evaporation, or annihilation of a primordial relic during the Big Bang nucleosynthesis (BBN) era are presented. It is found that injection of energetic nucleons around cosmic time 10^3 sec may lead to an observationally favored reduction of the primordial ${}^7\text{Li}/\text{H}$ yield by a factor 2 – 3. Moreover, such sources also generically predict the production of the ${}^6\text{Li}$ isotope with magnitude close to the as yet unexplained high ${}^6\text{Li}$ abundances in low-metallicity stars. The simplest of these models operate at fractional contribution to the baryon density $\Omega_b h^2 \gtrsim 0.025$, slightly larger than that inferred from standard BBN. Though further study is required, such sources, as for example due to the decay of the next-to-lightest supersymmetric particle into GeV gravitinos or the decay of an unstable gravitino in the TeV range of abundance $\Omega_{\tilde{G}} h^2 \sim 5 \times 10^{-4}$ show promise to explain both the ${}^6\text{Li}$ and ${}^7\text{Li}$ abundances in low metallicity stars.

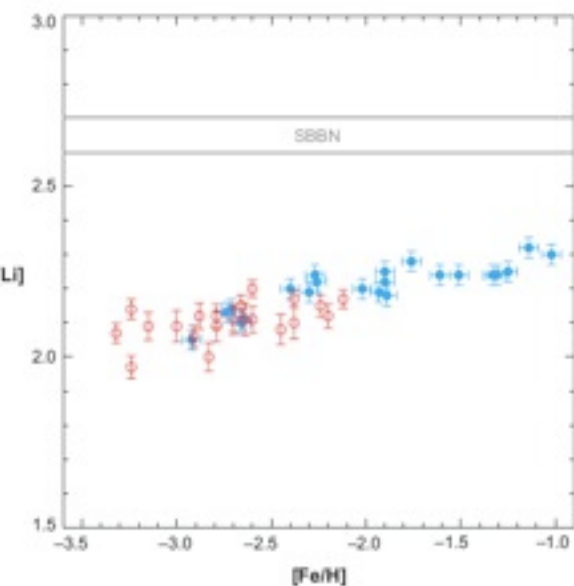
See also “Supergravity with a Gravitino LSP” by Jonathan L. Feng, Shufang Su, Fumihiko Takayama [Phys.Rev. D70 \(2004\) 075019](#)

“Gravitino Dark Matter and the Cosmic Lithium Abundances” by Sean Bailly, Karsten Jedamzik, Gilbert Moulta, [arXiv:0812.0788](#)

The Li abundance disagreement with BBN may be caused by stellar diffusion

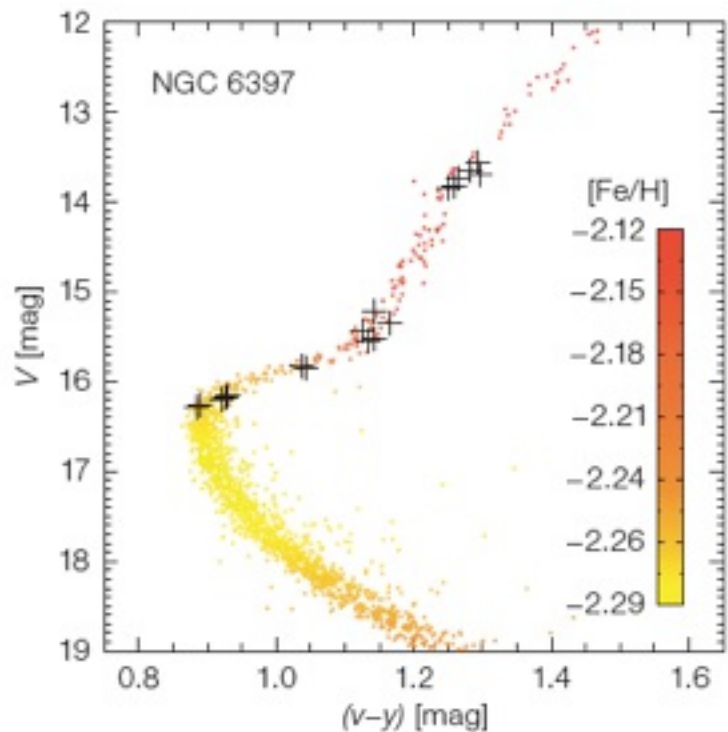


Lithium abundance in very old stars that formed from nearly primordial gas. The amount of ${}^7\text{Li}$ in these "Spite-plateau" stars (green) is much less than has been inferred by combining BBN with measurements of the cosmic microwave background made using WMAP (yellow band). Our understanding of stellar astrophysics may be at fault. Those Spite-plateau stars that have surface temperatures between 5700 and 6400 K have uniform abundances of ${}^7\text{Li}$ because the shallow convective envelopes of these warm stars do not penetrate to depths where the temperature exceeds that for ${}^7\text{Li}$ to be destroyed ($T_{\text{destruct}} = 2.5 \times 10^6$ K). The envelopes of cooler stars (data points towards the left of the graph) do extend to such depths, so their surfaces have lost ${}^7\text{Li}$ to nuclear reactions. **If the warm stars gradually circulate ${}^7\text{Li}$ from the convective envelope to depths where $T > T_{\text{destruct}}$, then their surfaces may also slowly lose their ${}^7\text{Li}$.** From <http://physicsworld.com/cws/article/print/30680>



Lithium abundances, $[\text{Li}] \equiv 12 + \log(\text{Li}/\text{H})$, versus metallicity (on a log scale relative to solar) from (red) S. Ryan et al. 2000, ApJ, 530, L57; (blue) M. Asplund et al. 2006, ApJ, 644, 229. Figure from G. Steigman 2007, ARAA 57, 463. **Korn et al. 2006 find that both lithium and iron have settled out of the atmospheres of these old stars, and they infer for the unevolved abundances, $[\text{Fe}/\text{H}] = -2.1$ and $[\text{Li}] = 2.54 \pm 0.10$, in excellent agreement with SBBN.**

The most stringent constraint on a mixing model is that it must maintain the observed tight bunching of plateau stars that have the same average ${}^7\text{Li}$ abundance. In a series of papers that was published between 2002 and 2004, Olivier Richard and collaborators at the Université de Montréal in Canada proposed such a mixing model that has since gained observational support. It suggests that all nuclei heavier than hydrogen settle very slowly out of the convective envelope under the action of gravity. In particular, the model makes specific predictions for settling as a star evolves, which are revealed as variations of surface composition as a function of mass in stars that formed at the same time.



Korn et al. The Messenger 125 (Sept 2006);
Korn et al. 2006, Nature 442, 657.

By spring 2006, Andreas Korn of Uppsala University in Sweden and colleagues had used the European Southern Observatory's Very Large Telescope (VLT) in Chile to study 18 chemically primitive stars in a distant globular cluster called NGC 6397 that were known to have the same age and initial composition. From this Korn et al. showed that the iron and lithium abundances in these stars both varied according to stellar mass as predicted by Richard's model. In fact, the model indicated that the observed stars started out with a ${}^7\text{Li}$ abundance that agrees with the WMAP data. Corroboration of these results is vital because **if the result stands up to scrutiny based on a wide range of data, then we have solved the lithium problem.**

A probable stellar solution to the cosmological lithium discrepancy

A Korn et al.

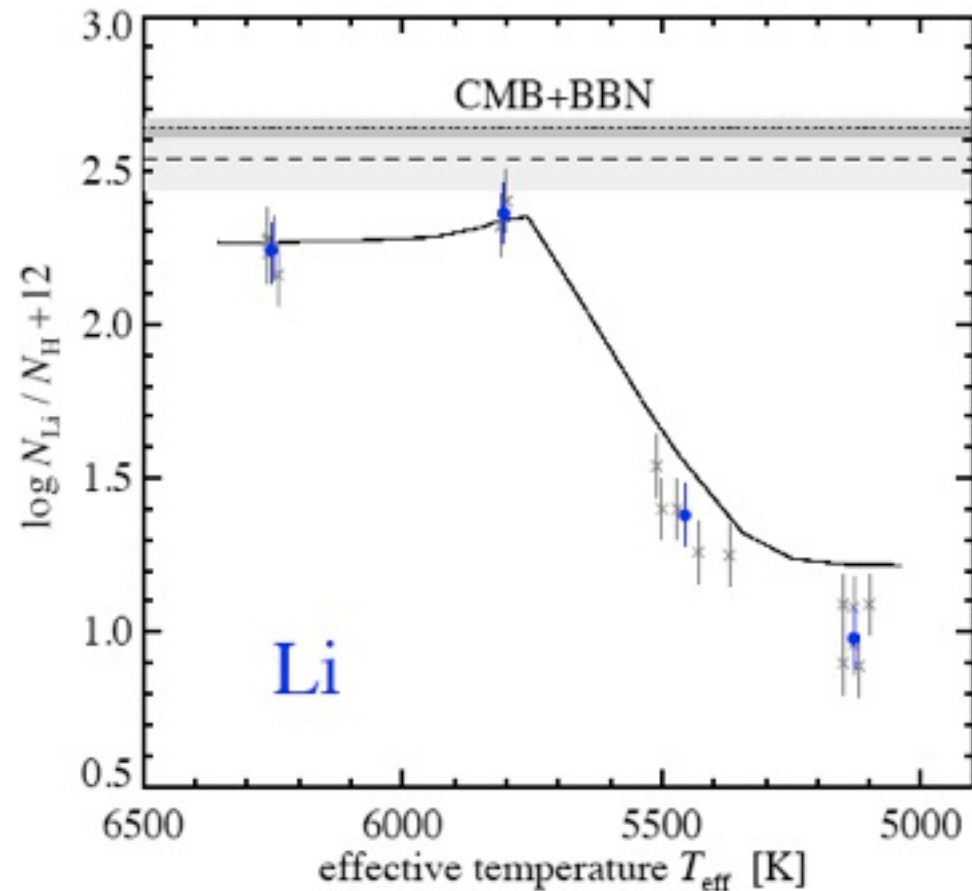
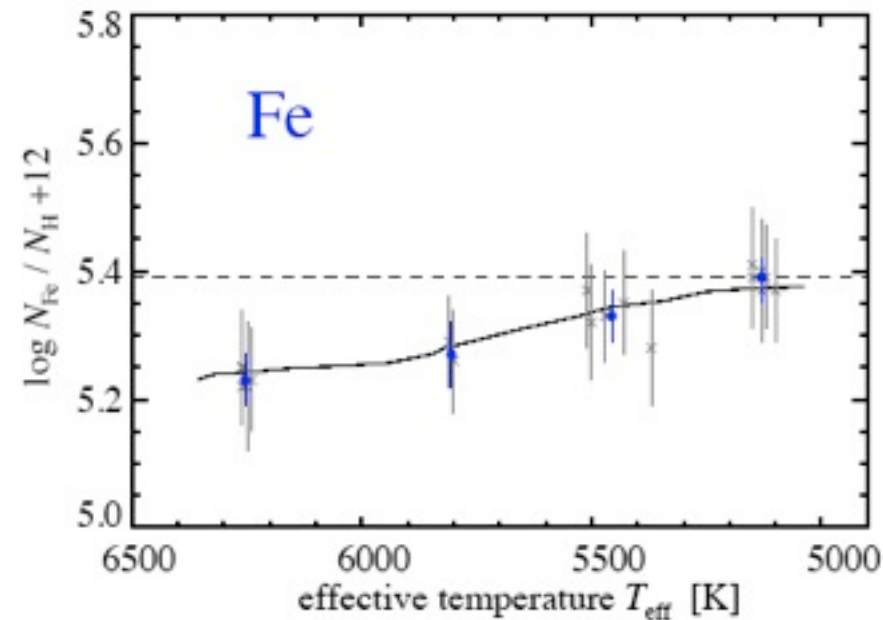


Figure 1: Trends of iron and lithium as a function of the effective temperatures of the observed stars compared to the model predictions. The grey crosses are the individual measurements, while the bullets are the group averages. The solid lines are the predictions of the diffusion model, with the original abundance given by the dashed line. In *b*, the grey-shaded area around the dotted line indicates the 1σ confidence interval of CMB + BBN¹: $\log[\epsilon(\text{Li})] = \log(N_{\text{Li}}/N_{\text{H}}) + 12 = 2.64 \pm 0.03$. In *a*, iron is treated in non-equilibrium²⁰ (non-LTE), while in *b*, the equilibrium (LTE) lithium abundances are plotted, because the combined effect of 3D and non-LTE corrections was found to be very small²⁹. For iron, the error bars are the line-to-line scatter of Fe I and Fe II (propagated into the mean for the group averages), whereas for the absolute lithium abundances 0.10 is adopted. The 1σ confidence interval around the inferred primordial lithium abundance ($\log[\epsilon(\text{Li})] = 2.54 \pm 0.10$) is indicated by the light-grey area. We attribute the modelling shortcomings with respect to lithium in the bRGB and RGB stars to the known need for extra mixing³⁰, which is not considered in the diffusion model.

Another way to determine the amount of ${}^7\text{Li}$ destroyed in stars is to observe the element's other, less stable, isotope: ${}^6\text{Li}$. ${}^6\text{Li}$ is not made in detectable quantities by BBN but instead comes from spallation: collisions between nuclei in cosmic rays and in the interstellar gas. Since ${}^6\text{Li}$ is even more easily destroyed than ${}^7\text{Li}$, detecting it allows us to place limits on the destruction of ${}^7\text{Li}$.

In 2006 Martin Asplund and co-workers at the Mount Stromlo Observatory in Australia made extensive observations of ${}^6\text{Li}$ in plateau stars using the VLT. In each of the nine stars where they found ${}^6\text{Li}$, roughly 5% of the lithium consisted of this isotope – which was larger than expected although at the limit of what was detectable with the equipment. This has huge implications not only for BBN but also for the history of cosmic rays in the galaxy and for stellar astrophysics. For example, the production of such large amounts of ${}^6\text{Li}$ must have required an enormous flux of cosmic rays early in the history of our galaxy, possibly more than could have been provided by known acceleration mechanisms. Moreover, if the plateau stars have truly destroyed enough ${}^7\text{Li}$ to bring the WMAP prediction of the mean baryon density into agreement with that obtained with the observed Spite plateau, the greater fragility of ${}^6\text{Li}$ implies that the stars initially contained ${}^6\text{Li}$ in quantities comparable to the observed ${}^7\text{Li}$ plateau.

All of these facts make the ${}^6\text{Li}$ observations an uncomfortable fit for BBN, stellar physics and models of cosmic-ray nucleosynthesis – particularly since the production of large amounts of ${}^6\text{Li}$ via cosmic rays has to be accompanied by a similar production of ${}^7\text{Li}$. Although ${}^6\text{Li}$ can be produced in some exotic particle-physics scenarios, it is vital that we independently confirm Asplund's results. Indeed, the hunt for primordial lithium (of both isotopes) is currently ongoing at the VLT, as well as at the Keck Observatory and the Japanese Subaru Telescope, although such observations are right at the limit of what can be achieved.

Observational signatures for depletion in the Spite plateau: solving the cosmological Li discrepancy?

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Abstract. We present Li abundances for 73 stars in the metallicity range $-3.5 < [\text{Fe}/\text{H}] < -1.0$ using improved IRFM temperatures (Casagrande et al. 2010) with precise $E(B-V)$ values obtained mostly from interstellar NaI D lines, and high-quality equivalent widths ($\sigma_{EW} \sim 3\%$). At all metallicities we uncover a fine-structure in the Li abundances of Spite plateau stars, which we trace to Li depletion that depends on both metallicity and mass. Models including atomic diffusion and turbulent mixing seem to reproduce the observed Li depletion assuming a primordial Li abundance $A_{\text{Li}} = 2.64$ dex (MARCS models) or 2.72 (Kurucz overshooting models), in good agreement with current predictions ($A_{\text{Li}} = 2.72$) from standard BBN. We are currently expanding our sample to have a better coverage of different evolutionary stages at the high and low metallicity ends, in order to verify our findings.

Recent references on BBN and Lithium

M Asplund et al. 2006, “Lithium isotopic abundances in metal-poor halo stars” *ApJ* 644 229–259

A Korn et al. 2006 “A probable stellar solution to the cosmological lithium discrepancy” *Nature* 442, 657–659; 2007 “Atomic Diffusion and Mixing in Old Stars. I. Very Large Telescope FLAMES-UVES Observations of Stars in NGC 6397” *ApJ* 671, 402

C Charbonnel 2006, “Where all the lithium went” *Nature* 442, 636-637

K Nollett 2007, “Testing the elements of the Big Bang” physicsworld.com

R H Cyburt, B D Fields, K A Olive 2008, “An update on the big bang nucleosynthesis prediction for ${}^7\text{Li}$: the problem worsens” *JCAP* 11, 12 (also [arXiv:0808.2818](http://arxiv.org/abs/0808.2818))

A J Korn 2008 “Atomic Diffusion in Old Stars --- Helium, Lithium and Heavy Elements” *ASPC* 384, 33

J Melendez et al. 2010 “Observational Signatures for Depletion in the Spite Plateau: Solving the Cosmological Li Discrepancy?” *IAU Symposium* 268, 211

M Proselov and J Pradler 2010 “Big Bang Nucleosynthesis as a Probe of New Physics” *Annual Reviews of Nuclear and Particle Physics* (also on astro-ph)

B Fields 2011 “The Primordial Li Problem” *Annual Reviews of Nuclear and Particle Science* (also on astro-ph)

BBN is a Prototype for Hydrogen Recombination and DM Annihilation

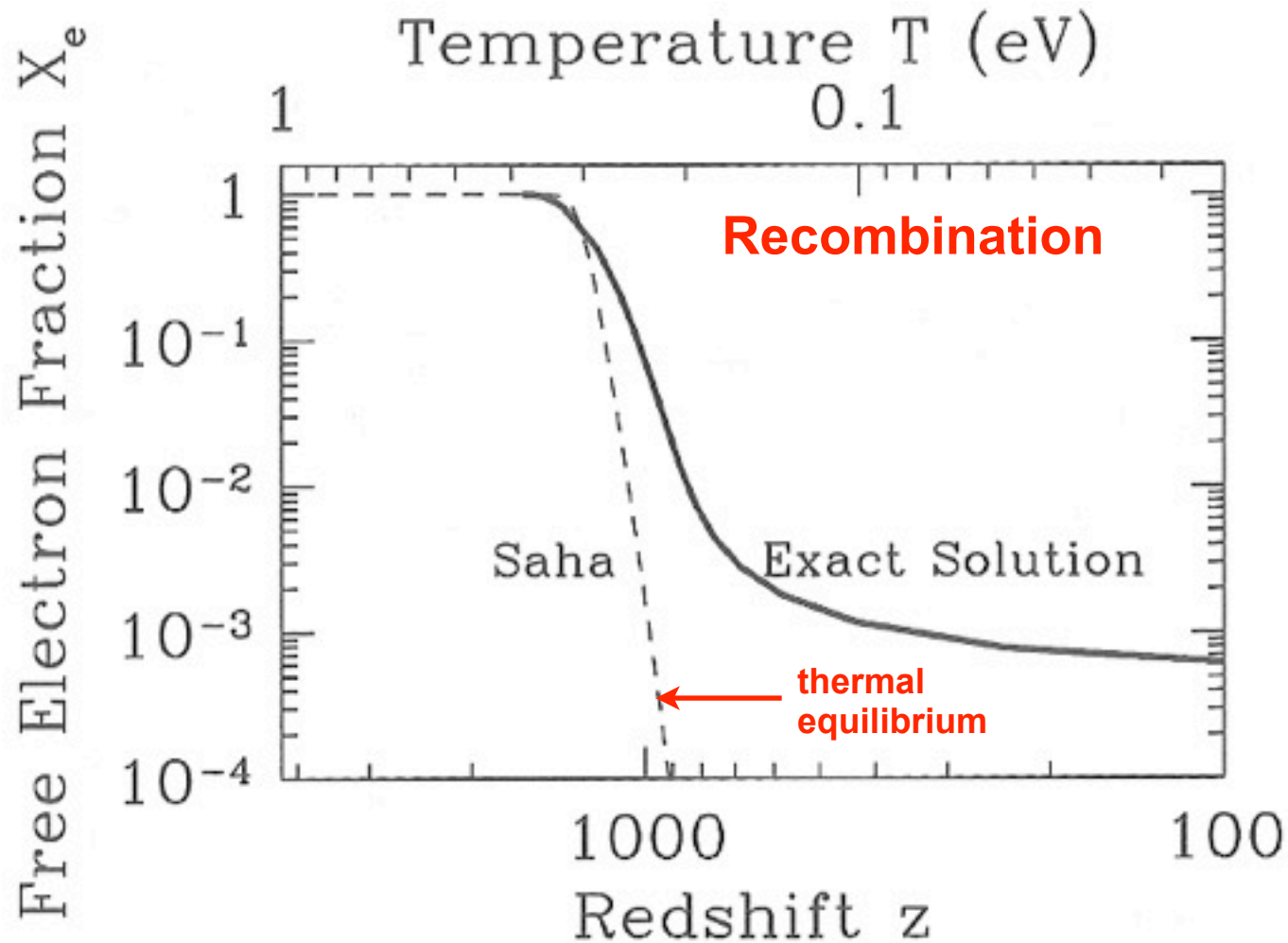


Figure 3.4. Free electron fraction as a function of redshift. Recombination takes place suddenly at $z \sim 1000$ corresponding to $T \sim 1/4$ eV. The Saha approximation, Eq. (3.37), holds in equilibrium and correctly identifies the redshift of recombination, but not the detailed evolution of X_e . Here $\Omega_b = 0.06$, $\Omega_m = 1$, $h = 0.5$.

Dodelson, *Modern Cosmology*, p. 72

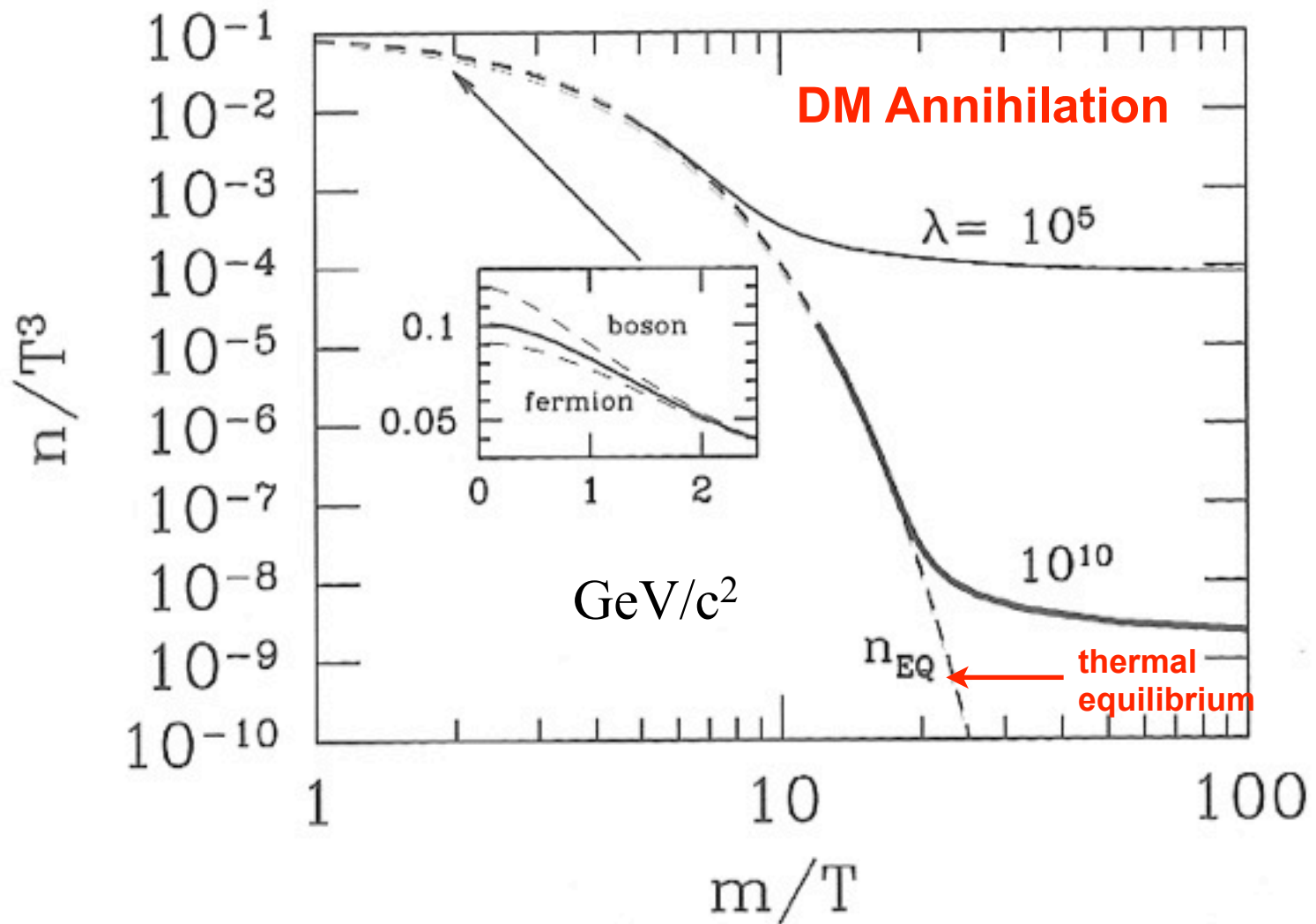


Figure 3.5. Abundance of heavy stable particle as the temperature drops beneath its mass. Dashed line is equilibrium abundance. Two different solid curves show heavy particle abundance for two different values of λ , the ratio of the annihilation rate to the Hubble rate. Inset shows that the difference between quantum statistics and Boltzmann statistics is important only at temperatures larger than the mass.

Dodelson, *Modern Cosmology*, p. 76