

Lecture 11  
 April 27, 2012

Some occasionally used special energy units

<p><b>Toe</b>          Tonne equivalent of energy obtained by burning 1 metric tonne of a standard crude.          1000 MToe = 40 Quads</p>	<p>1 Toe</p>	<p>41.87 Giga Joule          or  <math>40 \times 10^6</math> BTU</p>
<p><b>Therm</b>          Unit used e.g. in power and utilities bills for homes.</p>	<p>1 Therm</p>	<p><math>10^5</math> BTU = 29.3 KWh</p>

PG&E Bills

Electricity Usage (March 2012) = 489 Kwh (16/day)

Charges: \$92.47 (@) \$.185 / Kwh

Gas charges = 93 Therms (3/day)

Charges: \$110.19 @\$1.18/Therm

If we calculate cost of one therm after converting to electricity charges:

$$1 \text{ Therm cost} = 29.3(\text{KWh}) \times .185 (\text{Dollar/KWh}) \times = 5.4 \text{ Dollars}$$

Compared to 1.18 \$/Therm for gas itself.

Question:

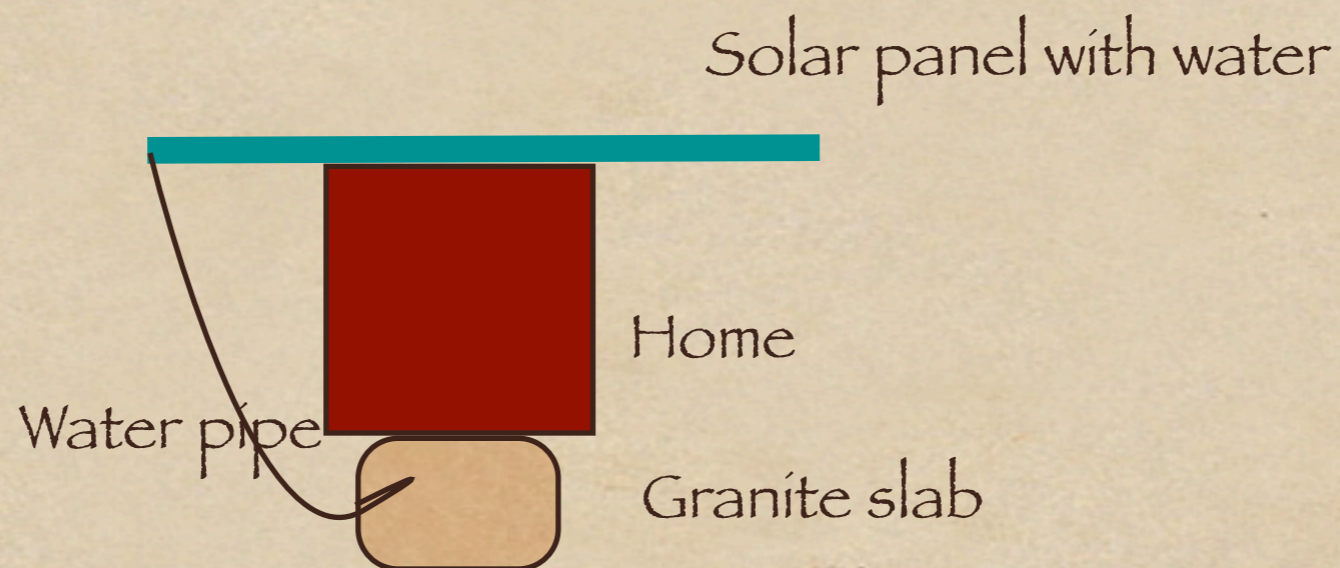
How many KWh electricity per day do you consume?

And how many therms gas?

A few instructive problems on material so far:

A Heat Storage device from Granite

When water in panel reaches  $50^{\circ}\text{C}$ , pump it through rock at bottom.



Problem: How big should the granite slab be, so that it can store enough energy to heat the house for a whole month?

Given that a whole month of heating is estimated to be at the rate of 24 kWh each day.

Assume house is maintained at  $15^{\circ}\text{C}$  ( $= 59^{\circ}\text{F}$ ).

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To solve this design issue we will equate the energy need to the energy capacity of granite in broad terms. In details this goes as follows:

1) Energy need:

Since we need energy for a month, the total needed is found by taking the rate (24 kWh/day) times 30 days = 720 kWh

This is expressible in Joules by looking up  $1 \text{ kWh} = 3.6 \times 10^6 \text{ J}$ .

(This can also be found from the definitions:  $1 \text{ kWh} = 1000\text{W}/\text{Hour}$  and since  $1 \text{ Hour} = 3600 \text{ Secs}$ ,  $1 \text{ kWh} = 1000 \times 3600 \times \text{Joule} = 3.6 \times 10^6 \text{ J}$  (recall  $1 \text{ Joule} = 1 \text{ Watt} \times 1 \text{ Second}$ )).

Thus energy requirement  $\Delta E = 720 \text{ kWh} \times 3.6 \times 10^6 \text{ Joules/kWh} = 2.592 \times 10^9 \text{ J}$

2) Storage calculation from specific heat.

$$\Delta Q = c m \Delta T$$

$m =$  (unknown) mass of granite,  
 $c$  its specific heat =  $820 \text{ J/kg/K}$

Heat stored in the rock is found from the usual formula. We need to know the temperature difference. Since the home is at  $15^{\circ}\text{C}$ , the granite block is also at that temperature. The hot water is at  $50^{\circ}\text{C}$ , so that the temperature difference corresponding to the heating of the granite block is  $35^{\circ}\text{C}$ .

$$\Delta Q = 820J/(kG \times^0 K) \times m(kG) \times (35 \times^0 K) = 2.87 \times 10^4 \times m \text{ (Joules)}$$

Here m is in kG's.

We now equate the storage with the requirement

$$\Delta Q = \Delta E$$

$$(2.87 \times 10^4 \times m(kG)) \text{ (Joules)} = (2.592 \times 10^9) \text{ (Joules)}$$

Solving for m we get:

$$m = [2.592 \times 10^9] / [2.87 \times 10^4] = 9.03 \times 10^4(kG)$$

Since density  $\rho = m/V$ , we can find V given the density of granite using  $V = m/\rho$

$$\rho = 2750kG/m^3$$

$$V = 36m^3 = 6 \times 6 \times 1m^3$$

Answer: Granite slab is appxly 18ft x18ft x3 ft

A coal burning power plant burns coal at  $706\text{ }^{\circ}\text{C}$  and exhausts heat into a river with average temperature  $19\text{ }^{\circ}\text{C}$ . What is the minimum possible rate of thermal pollution (i.e. heat exhausted into the river) if the station generates 125 MW of electricity?

In solving this problem, a few simple ideas are at play.

We notice that we are given the power rating (i.e. rate of energy production) of the plant, rather than the energy produced by itself. The required answer also asks for the rate of thermal pollution.

So the question is can we write the efficiency also in terms of the rates of energy or heat.

The answer is yes. To see further assuming a Carnot machine, this let us assume a unit of time  $\Delta t$ . To fix ideas we can say that  $\Delta t = 1$  day, but the final answer does not depend upon this choice.

Therefore within the time interval of  $\Delta t$ , we will write

the heat absorbed from the coal burning as  $\Delta Q_H$ , (hence the rate of absorption is  $\Delta Q_H / \Delta t$ )

the heat rejected into the river as  $\Delta Q_L$  (hence the rate of rejection is  $\Delta Q_L / \Delta t$ )

and the energy output as  $\Delta E$ . (power output is  $\Delta E / \Delta t$ )

If we double  $\Delta t$ , these energies will also double, and that is why the value of  $\Delta t$  is finally immaterial.

Let us now express the Carnot efficiency:

$$\eta = \frac{\Delta Q_H - \Delta Q_L}{\Delta Q_H} \text{ or}$$

$$\eta = \frac{(\Delta Q_H / \Delta t) - (\Delta Q_L / \Delta t)}{(\Delta Q_H / \Delta t)}$$

Thus we can express the efficiency in terms of the rates

as well. Solving this we get:

$$(\Delta Q_L / \Delta t) = (\Delta Q_H / \Delta t) \times (1 - \eta)$$

The first calculation we need to do is to figure the efficiency of this engine. Since the operating temperatures ( $T_H$ ,  $T_L$ ) are given as

$$T_H = 706^\circ C = 979^\circ K$$

$$T_L = 19^\circ C = 292^\circ K$$

$$\eta = \frac{T_H - T_L}{T_H} = 0.702$$

Now we saw on the last page that

From the first law (energy conservation) we also get

$$(\Delta Q_L / \Delta t) = (\Delta Q_H / \Delta t) \times (1 - \eta)$$

$$\Delta E / \Delta t = (\Delta Q_H - \Delta Q_L) / \Delta t$$

We can eliminate  $\Delta Q_H$  in favor of  $\Delta Q_L$  and  $\eta$  to obtain:

$$\Delta Q_L / \Delta t = (1 - \eta) / \eta \times \Delta E / \Delta t$$

Since the power station produces power at the rate of 125 MW, we infer that  $\Delta E / \Delta t = 125 \text{ MJ} / \Delta t$ . Substituting we get

$$\text{Therefore } \Delta Q_L / \Delta t = \Delta E / \Delta t (1 - \eta) / \eta = 53.1 \text{ MJ} / \Delta t.$$

This is the amount of heat discharged by the plant, in a time interval  $\Delta t$ , and hence the rate of pollution is 53.1 MW.

2. A jeweller needs to melt a .5 kg block of silver at 20 °C, in order to pour into her molds. How much heat is needed to achieve this in kJ?

We view this in two stages:

First stage is to heat silver to its melting temperature  $T_M = 960.8$  °C from 20°C, using the known heat capacity of silver  $C = .235$  kJ/kg °C,

Second stage to melt it using the latent heat of fusion (melting) 88.3 kJ/kg.

Then add these

$$\Delta Q_{\text{Heating}} = C m \Delta T \qquad \Delta Q_{\text{melting}} = L_{\text{melting}} m$$

$$\Delta Q = \Delta Q_{\text{Heating}} + \Delta Q_{\text{Melting}}$$

Plugging in the various values, we find in units of kilo Joules

$$Q = 0.5 \text{ kg} \times 88.3 \text{ kJ/kg} + .235 \text{ kJ/(kg °C)} \times 0.5 \text{ kg} \times 940.8^\circ\text{C} = 155 \text{ kJ.}$$