

Lecture 9
April 20, 2012

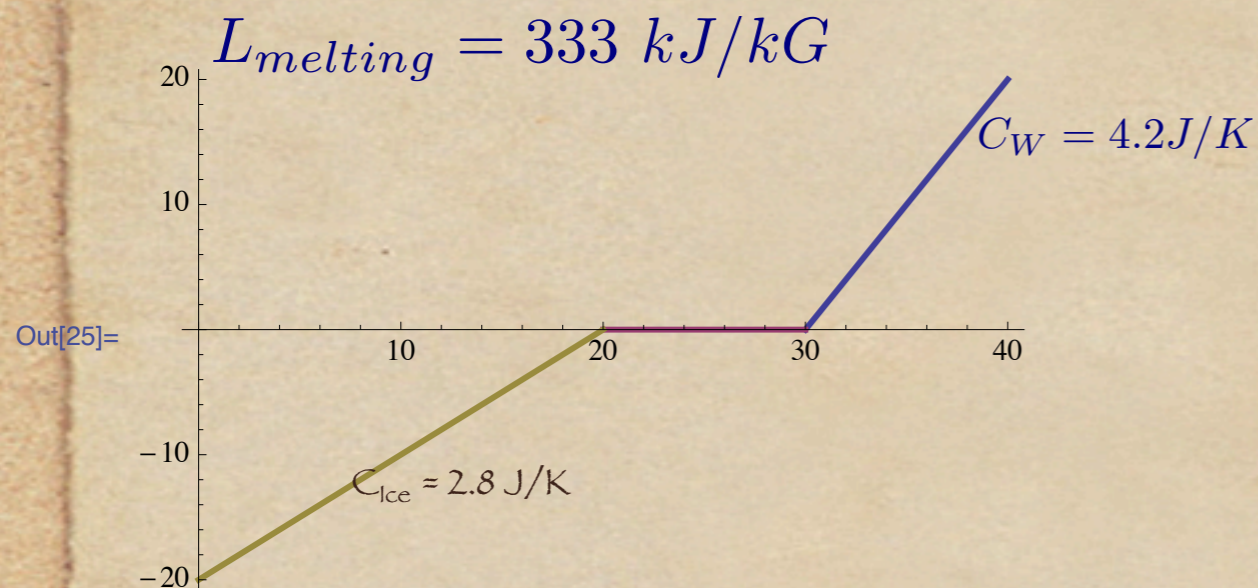
Latent heat is associated with melting and also with vaporizing
(boiling)
also sublimation

$$\Delta Q = M L$$

Melting of ice: endothermic
(needs heat)

Defines a new and important number:
The latent heat L

L is the heat necessary to change the
phase per unit mass
at the
phase transition temperature



Boiling of water into Steam!
also endothermic

$$L_{vapourizing} = 2.25 \text{ MJ/kg}$$

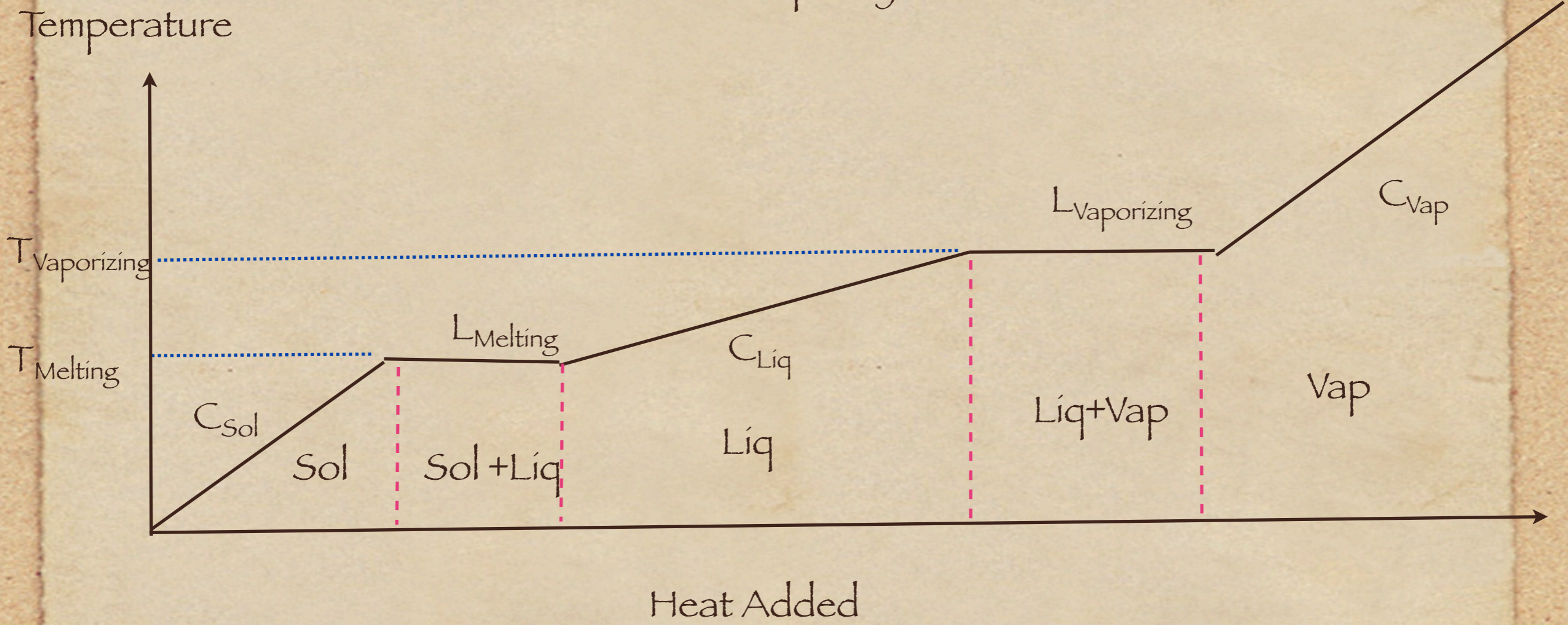
Mixing problems:

Energy is conserved
Phase changes (transitions)
Latent heat and heat capacity

$$\Delta Q = c M \Delta T \quad (\text{Specific Heat})$$

$$\Delta Q = M L \quad (\text{Latent Heat})$$

Heat change = Heat due to change of temperature
+ Heat due to phase change



Examples

$$\Delta Q = M L$$

$$L_{\text{melting}} = 333 \text{ kJ/kg}$$

a) 5 kG water freezes: how much heat does it generate in the process? and what is the temperature after freezing?

Using given formula: $\Delta Q = 5 \text{ kG} \times 333 \text{ kJ/kg} = 1665 \text{ kJ} = 1.665 \text{ MJ}$

b) 10 kG ice melts: How much heat does it absorb from the environment?

Answer = 3.333 MJ

c) 10 kG water boils: how much heat does it require?

$$L_{\text{vapourizing}} = 2.25 \text{ MJ/kg}$$

Answer = 22.5 MJ (Note the much bigger scale)

Summarizing the difference between
Specific heat versus Latent Heat

$$\Delta Q = M c \Delta T$$

(State is fixed but T changes)

$$\Delta Q = M L$$

(T is fixed but state changes)

Example combining the two

Find the heat needed to heat 10 kG water at 90°C to steam at 110°C

- A) There is heating of water from 90 to 100 C,
- B) change of state to steam at 100 C
- C) heating of steam from 100 C to 110 C

Data given: Latent heat for boiling 2.25 MJ/kg
Specific heat of water 4.2 kJ/kg
Specific heat of steam 1.996 kJ/kg
Specific heat of ice 2.18 kJ/kg

$$\Delta Q = Q_a + Q_b + Q_c$$

$$Q_a = 420 \text{ kJ}, \quad Q_b = 22.5 \text{ MJ}, \quad Q_c = 199.6 \text{ kJ}$$

Nice demonstration of ice water equilibrium and effect of salt at the URL:

<http://antoine.frostburg.edu/chem/senese/101/solutions/faq/why-salt-melts-ice.shtml>

A) An unknown amount of water at 20 C is mixed with 6 ice cubes at 0C, each with weight 30 grams. The mixture becomes cold water at 5 C. what is the weight of the total mixture?

B) A shot of lead of unknown mass is dropped into 1 litre of water at 30 C and is just hot enough to convert the water to steam at 120 C in equilibrium with the shot. Calculate the mass of the shot.
Specific heat of lead = .13 kJ/kG

Process:

- 1) Locate the appropriate formulas- make sure you have all the needed ones.
- 2) Identify the object required for answering the question and give it a symbolic name - e.g. "x" kGs in the above problems.
- 3) Using "x" in the formulas, set up an equation where the unknown is on the LHS and the rest on RHS. Here you have to use (1)
- 4) Solve for x!! :-)

Q-1 One kg of ice is melted by absorbing heat from 20 kg of water in a chamber surrounding the ice, initially at 50°C. What is the final temperature of the water in the chamber, assuming that the melted ice runs off at 0°C (i.e. does not absorb further heat)

Solution:

- $L=333 \text{ kJ/kg}$

Hence 1 kg ice releases 333 MJ

- Use $\Delta Q= Mc \Delta T$ to calculate heating of water

- $M = 20 \text{ kg}$, $c = 4.2 \times 10^3 \text{ J/(kg } ^\circ\text{C)}$

- $\Delta T = 333 \times 10^3 \text{ J} \times \text{kg } ^\circ\text{C} / (20 \text{ kg} \times 4.2 \times 10^3 \text{ J}) = 3.96 \text{ } ^\circ\text{C}$

- $T_{\text{final}} = 46^\circ\text{C}$

Q- 2 What happens with 1 kg water rather than 20 kg?

- $\Delta T = 3.96 \times 20 = 79.2 \text{ } ^\circ\text{C}$

- We are in trouble since $79.2 + 50 = 129.2 \text{ } ^\circ\text{C}$, i.e. higher than

- boiling point

- Some water would evaporate.

- How much water evaporates? HW